

# The modern day blacksmith

Gareth Conduit

Theory of Condensed Matter group

Neural network algorithm to

Train from **sparse** datasets

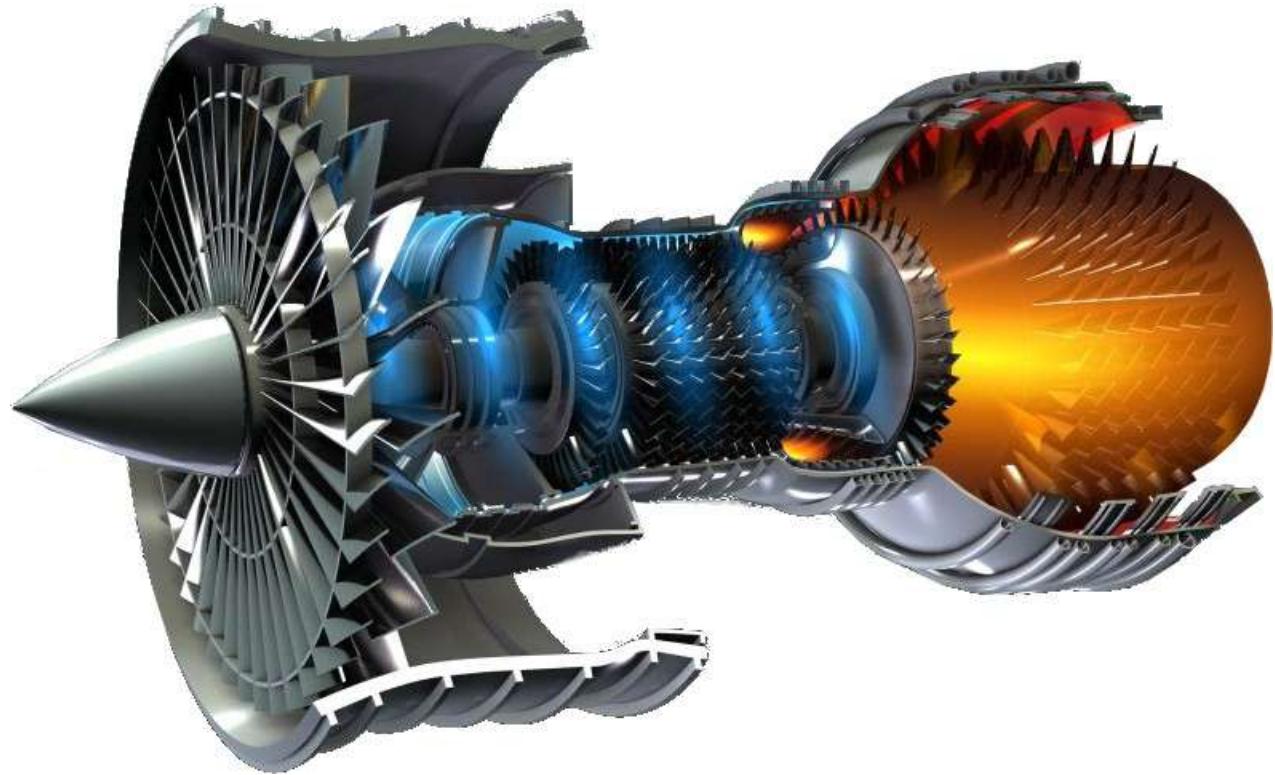
**Merge** simulations, physical laws, and experimental data

**Reduce** the need for expensive experimental development

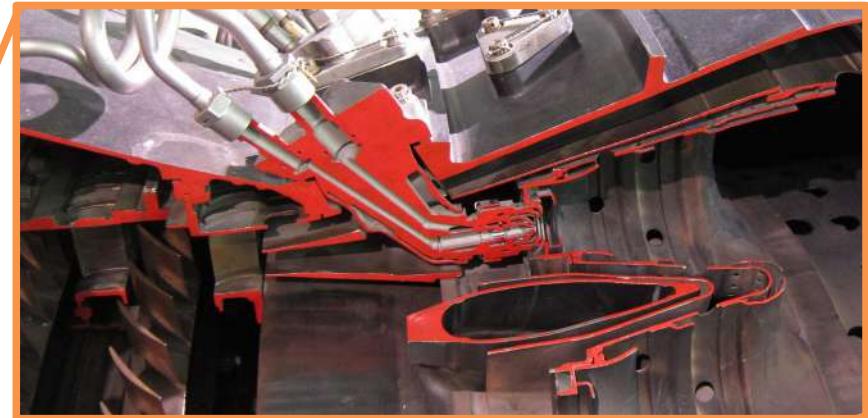
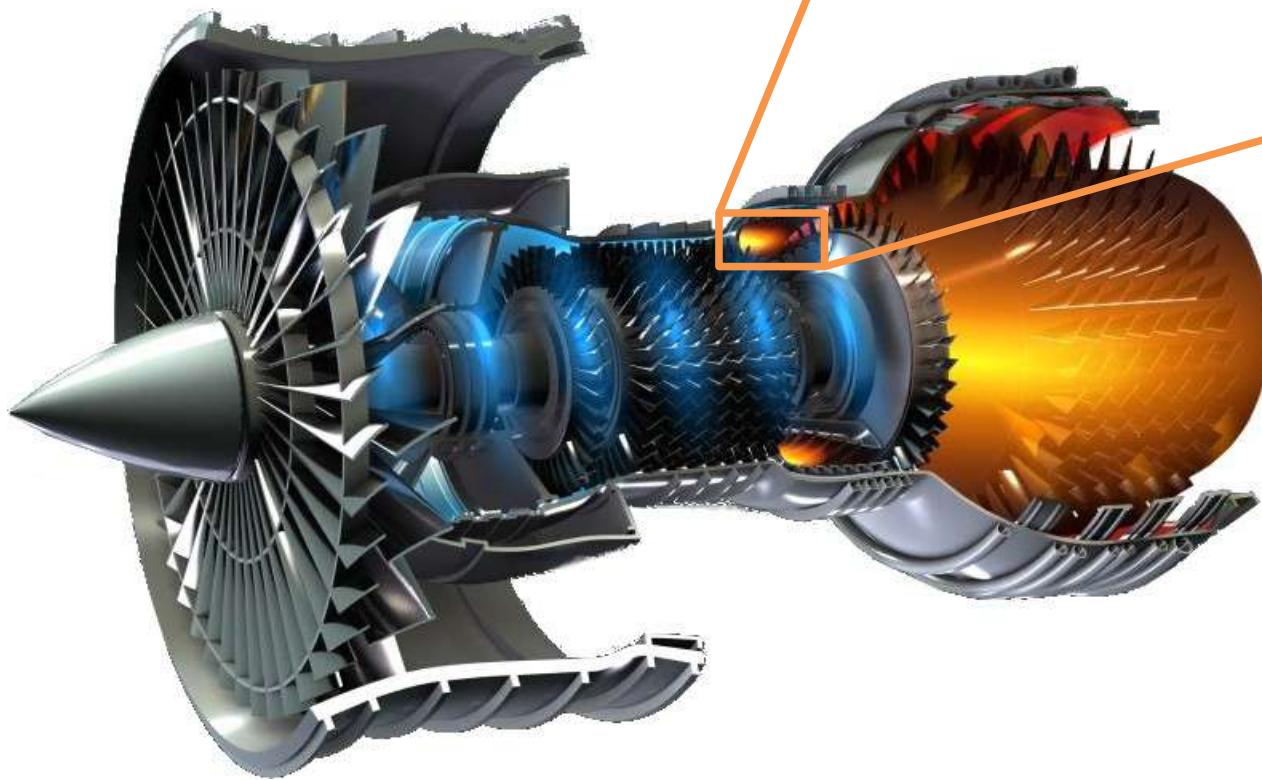
**Accelerate** materials and drugs discovery

**Generic** with **proven** applications in materials discovery and drug design

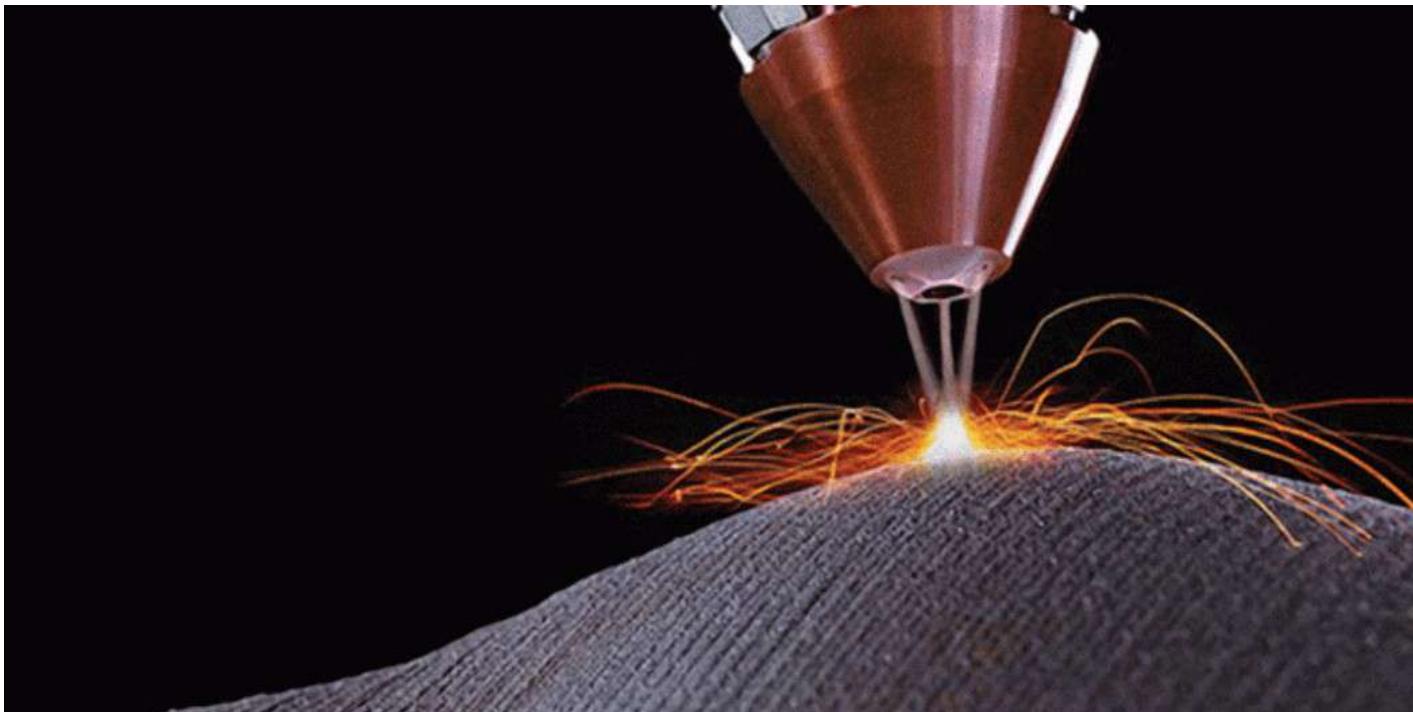
# Schematic of a jet engine



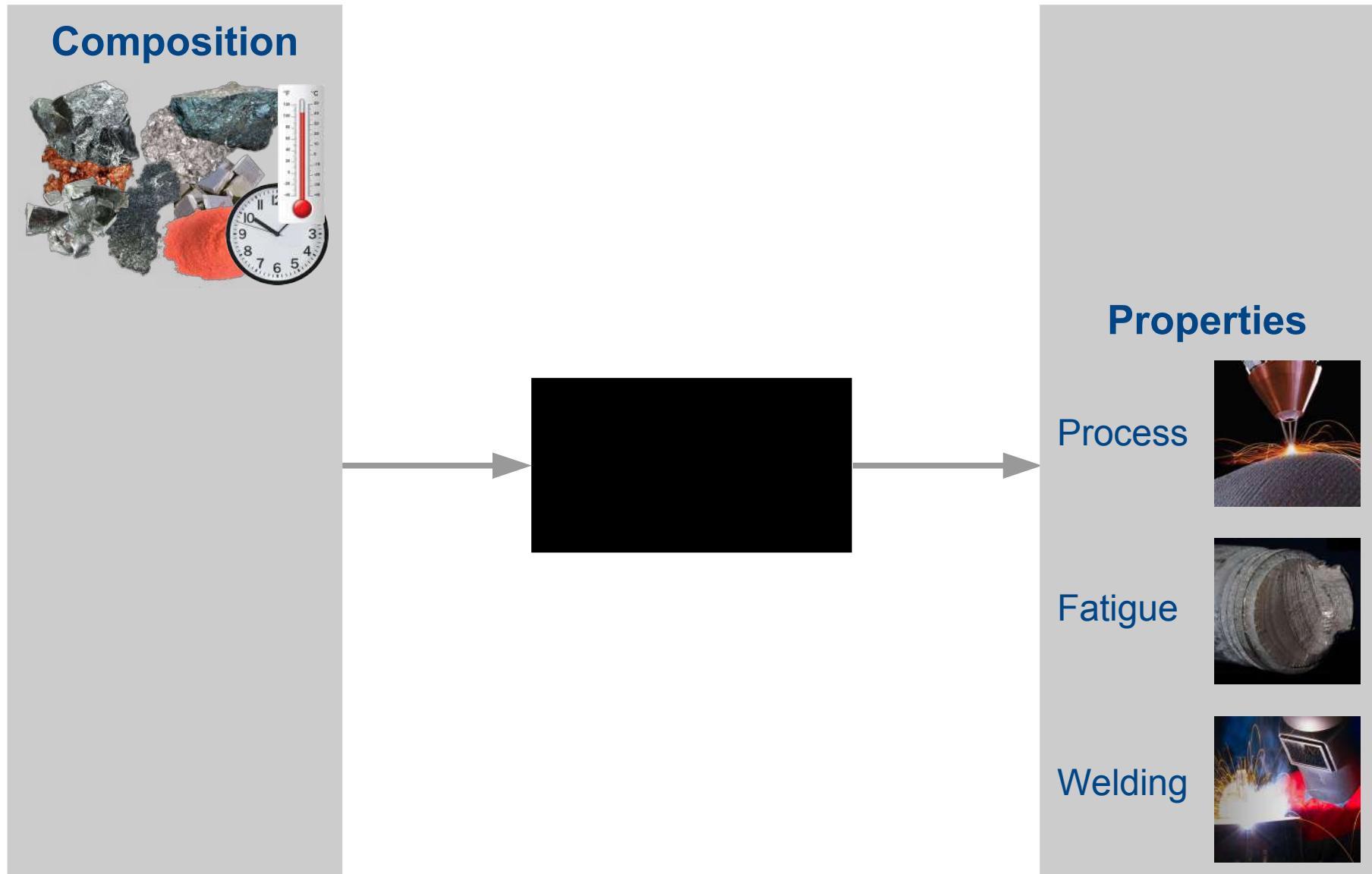
# Combustor in a jet engine



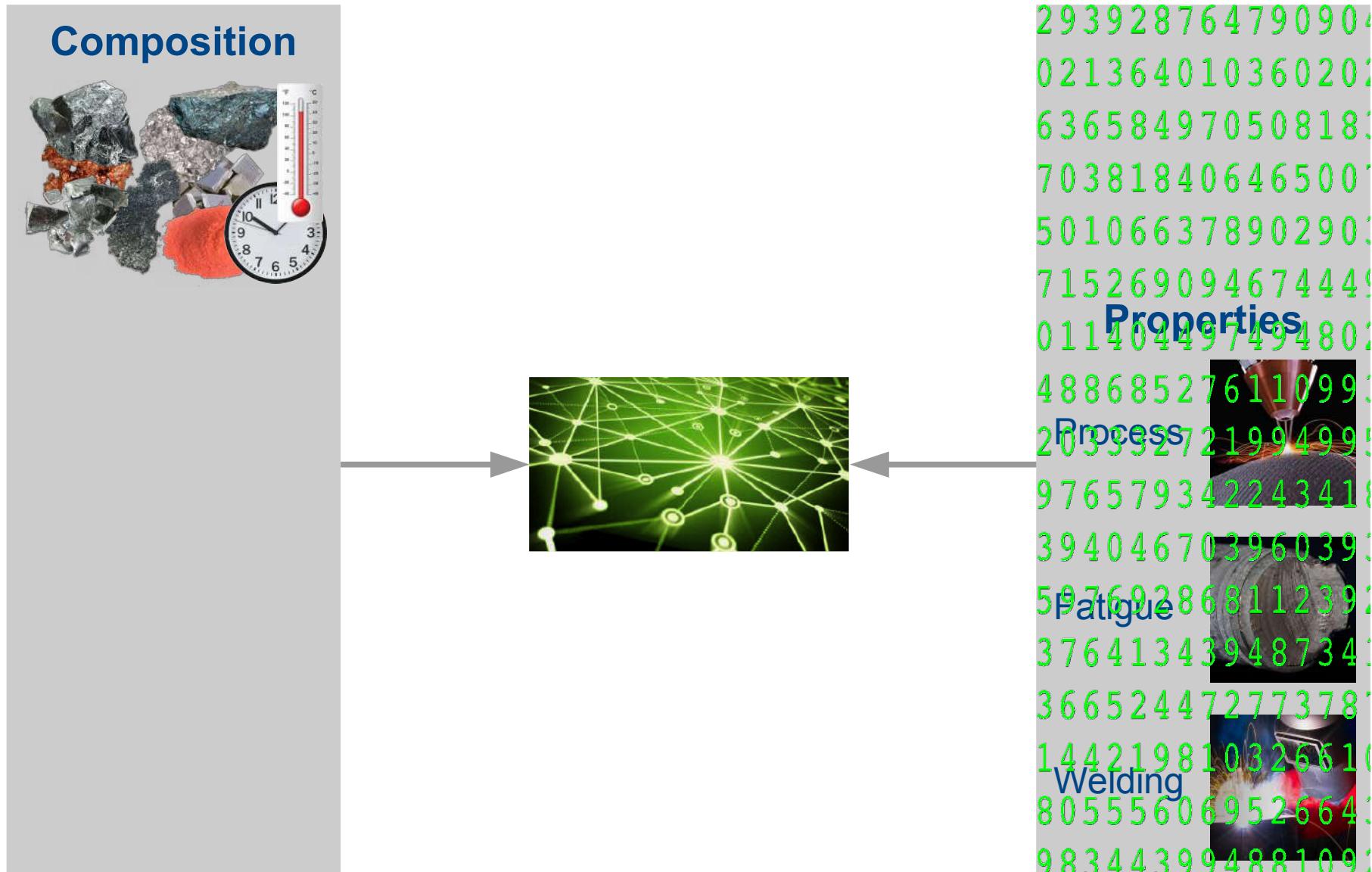
# Direct laser deposition requires new alloys



# Neural networks for materials design



# Neural networks for materials design



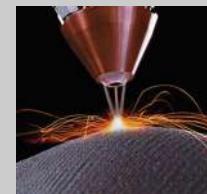
# Neural networks for materials design

## Composition



## Properties

### Process



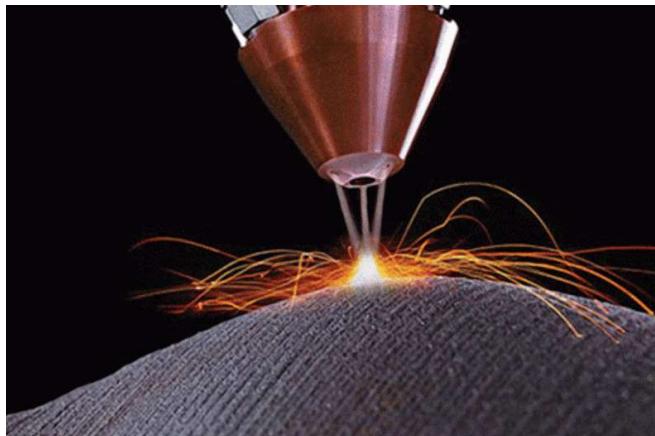
### Fatigue



### Welding



# Neural networks for materials design

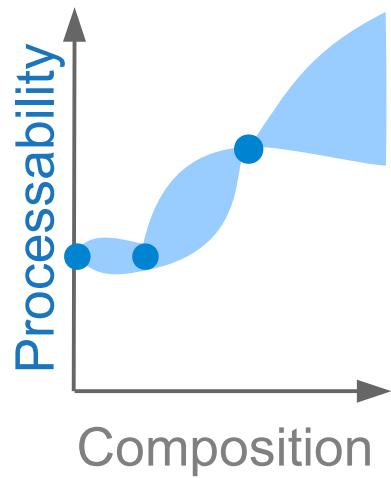


Laser

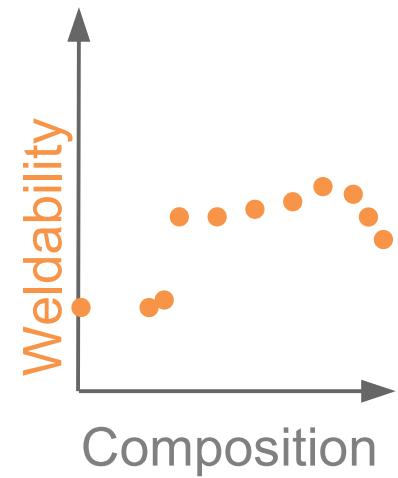


Electricity

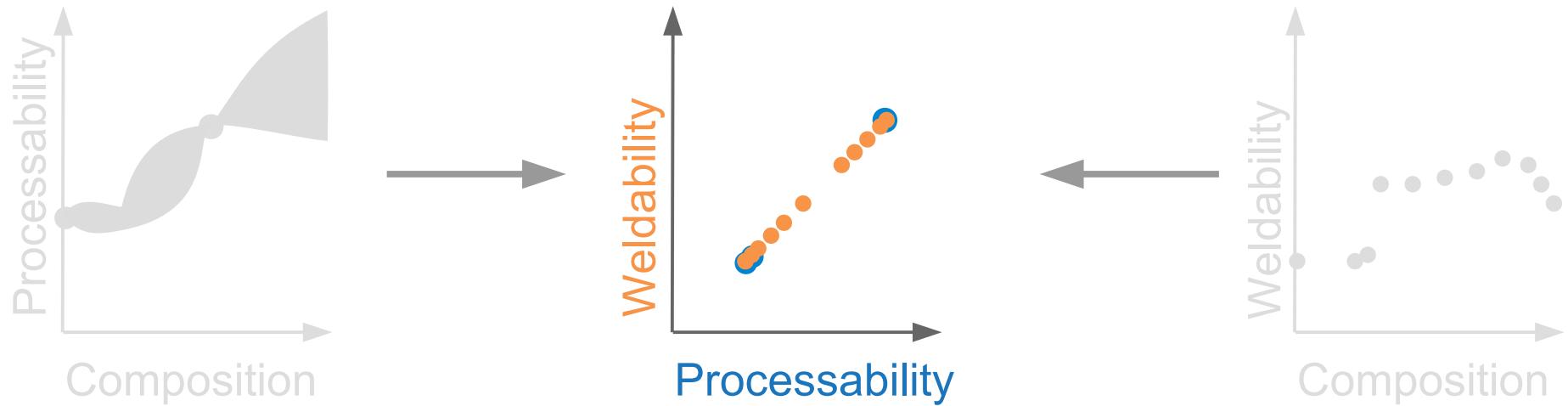
# Insufficient data for processability



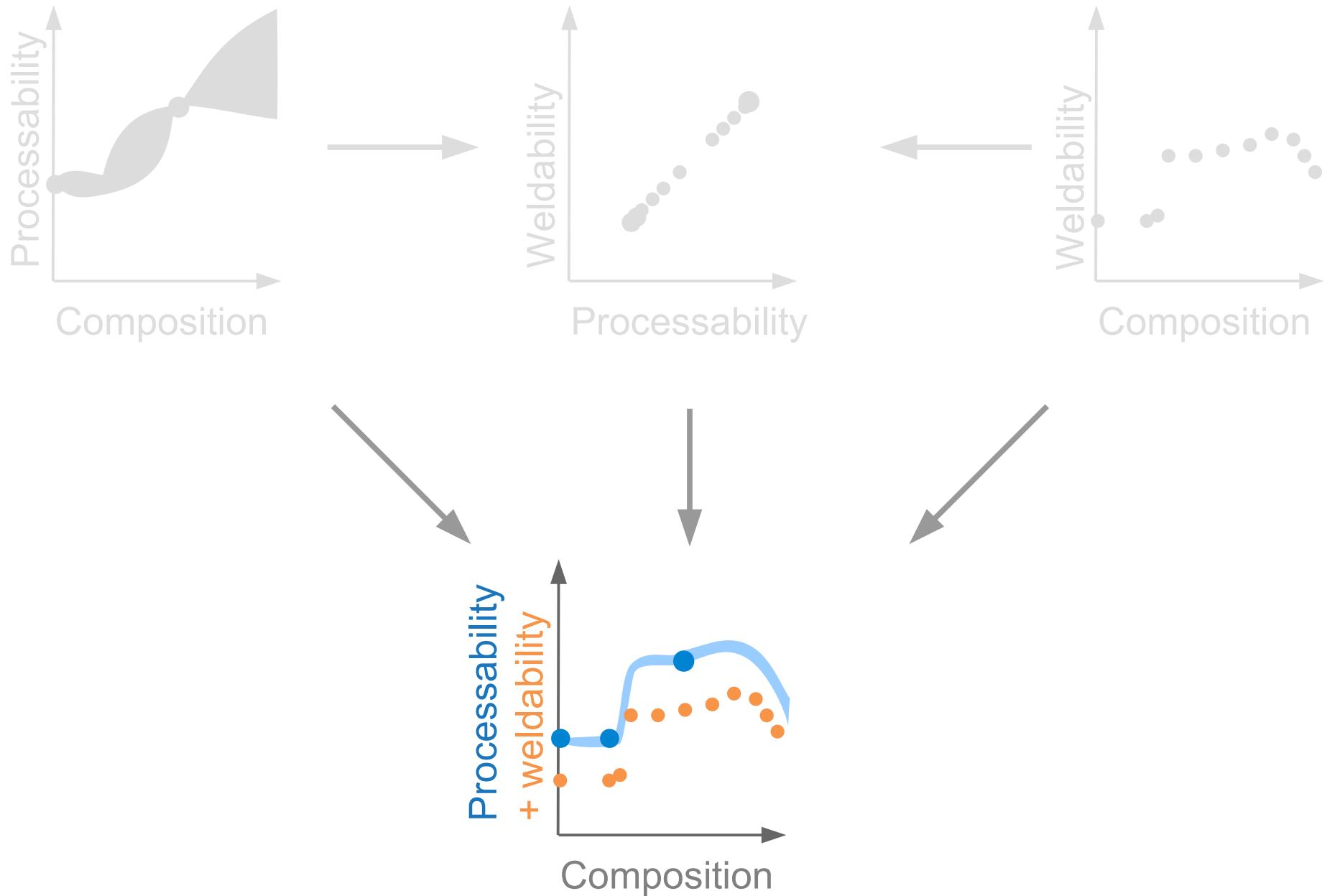
# Welding is analogous to direct laser deposition



# Simple processability-welding relationship



# Merging properties with the neural network



# Neural networks for materials design

## Composition



## Properties

### Process



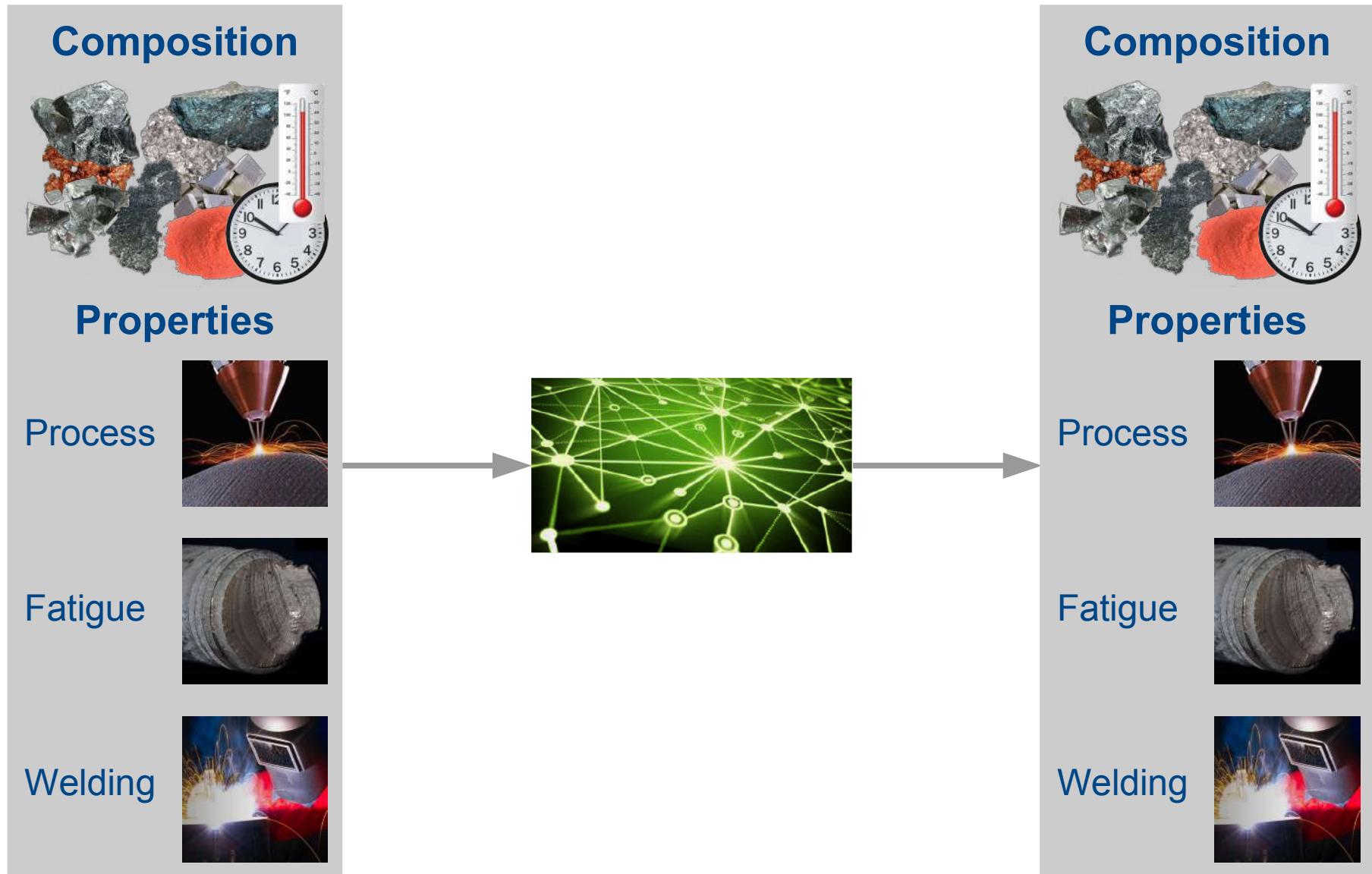
### Fatigue



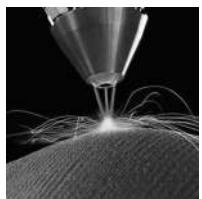
### Welding



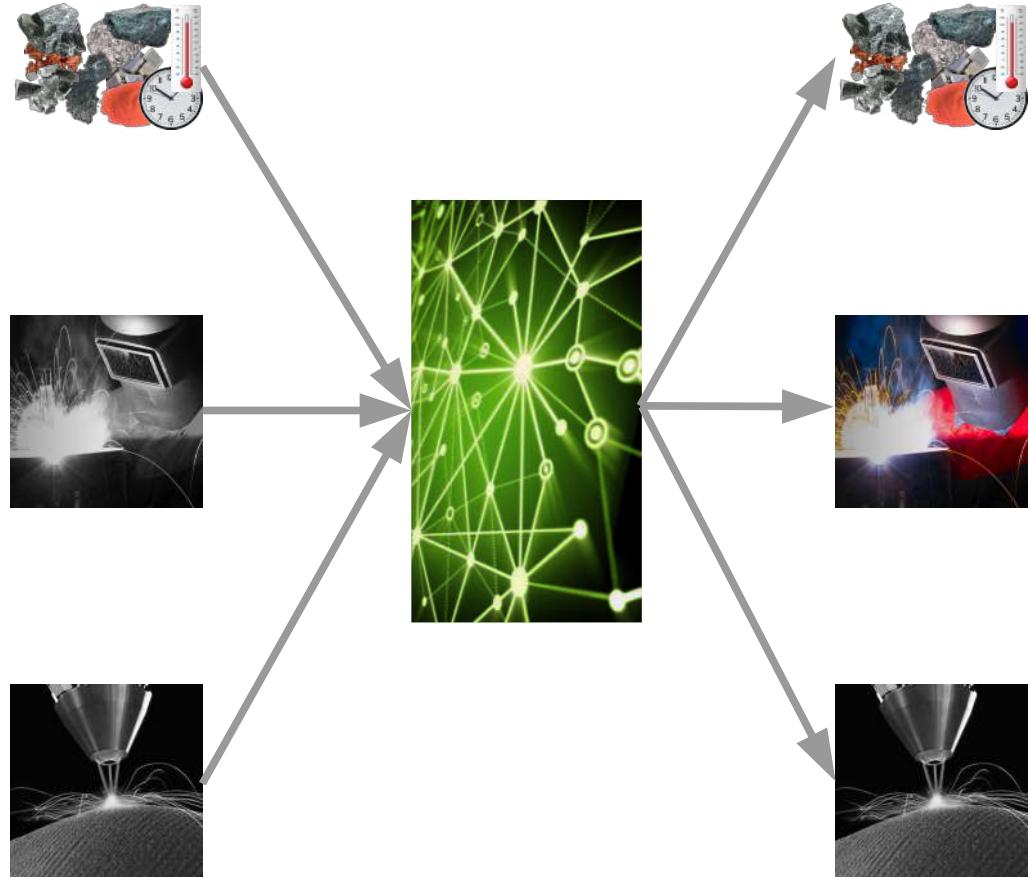
# Neural networks for materials design



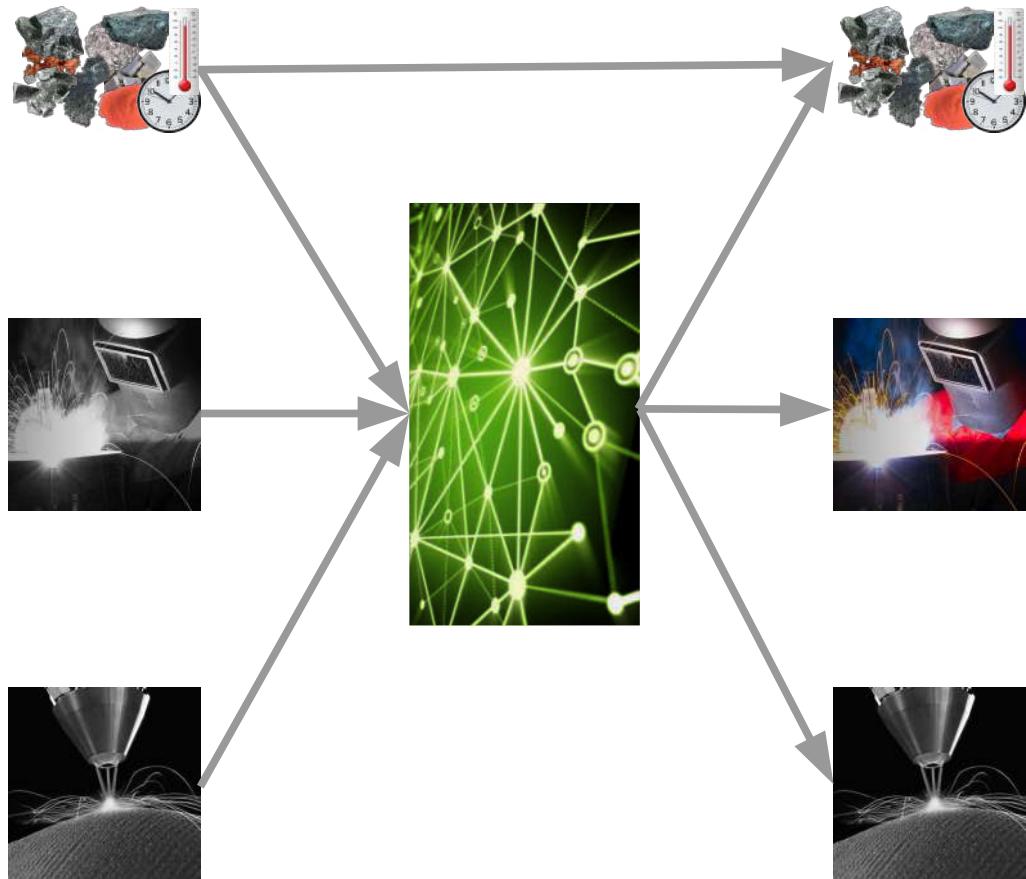
# Filling in missing values



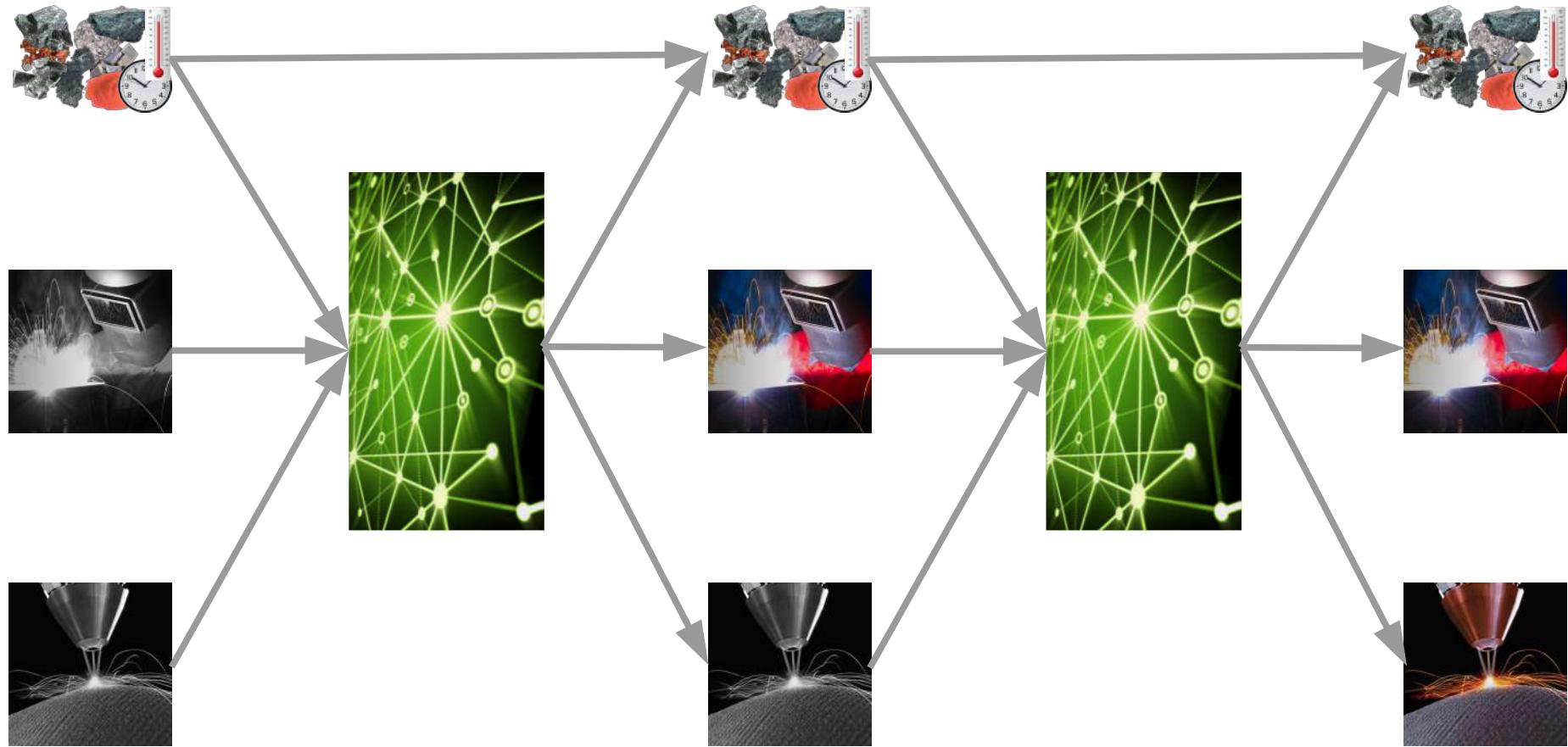
# Filling in missing values



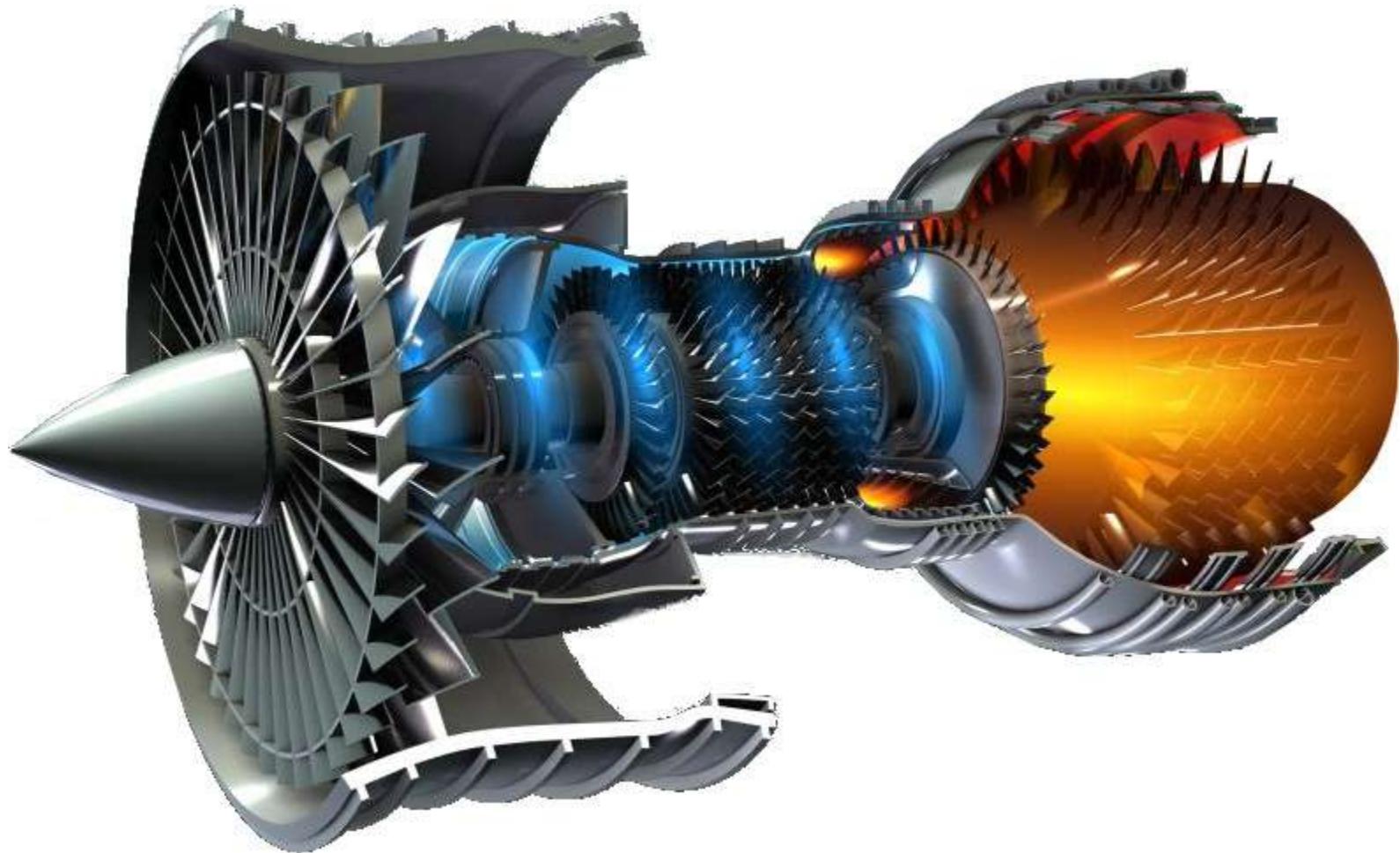
# Pass through present value



# Second pass to fill in missing values



# Schematic of a jet engine



# Target properties

Elemental cost < 25 \$kg<sup>-1</sup>

Density < 8500 kgm<sup>-3</sup>

$\gamma'$  content < 25 wt%

Oxidation resistance < 0.3 mgcm<sup>-2</sup>

Processability < 0.15% defects

Phase stability > 99.0 wt%

$\gamma'$  solvus > 1000°C

Thermal resistance > 0.04 KΩ<sup>-1</sup>m<sup>-3</sup>

Yield stress at 900°C > 200 MPa

Tensile strength at 900°C > 300 MPa

Tensile elongation at 700°C > 8%

1000hr stress rupture at 800°C > 100 MPa

Fatigue life at 500 MPa, 700°C > 10<sup>5</sup> cycles

# Composition

Cr: 19%



Co: 4%



Mo: 4.9%



W: 1.2%



Zr: 0.05%



Nb: 3%



Al: 2.9%



C: 0.04%



B: 0.01%



Ni



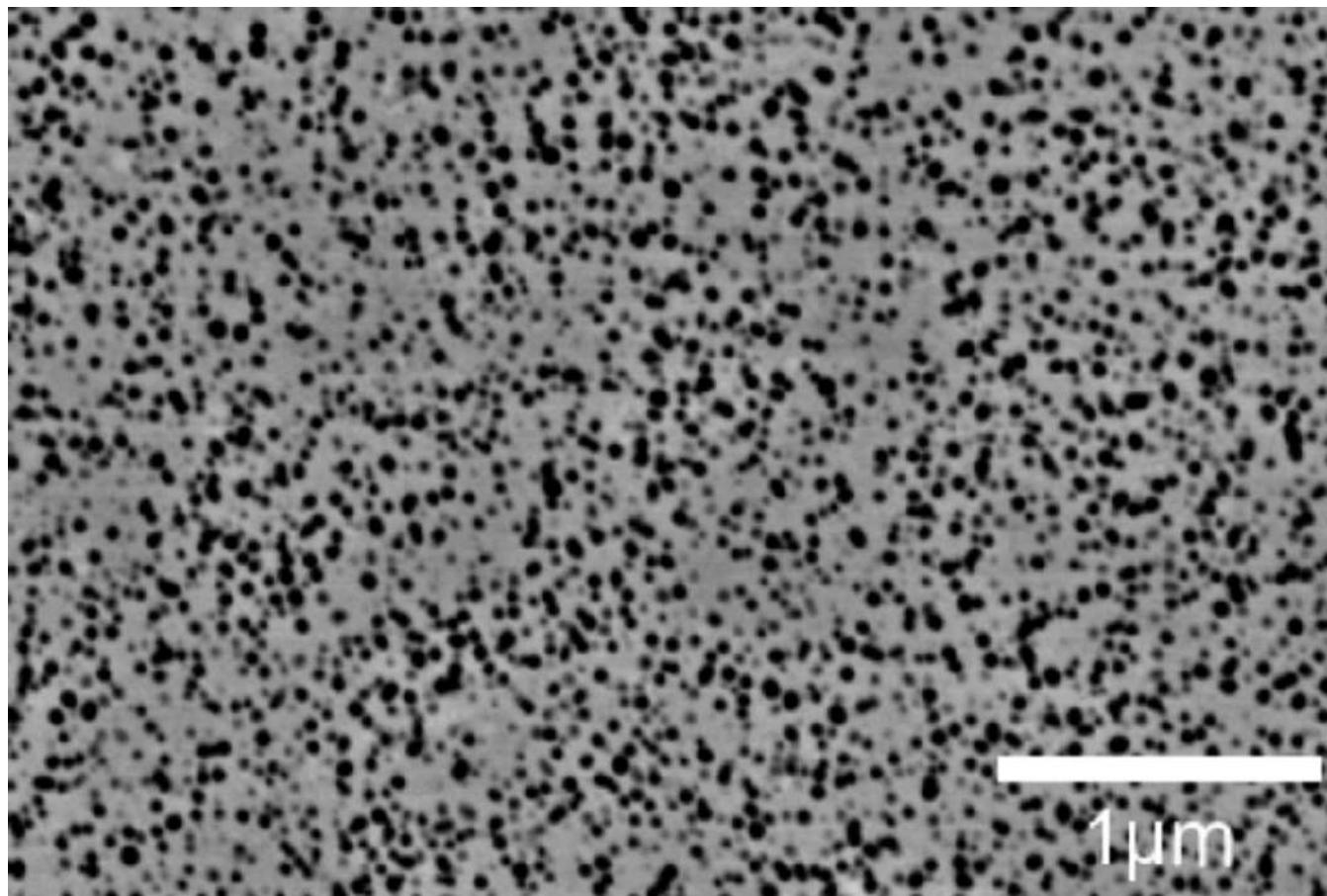
Expose 0.8



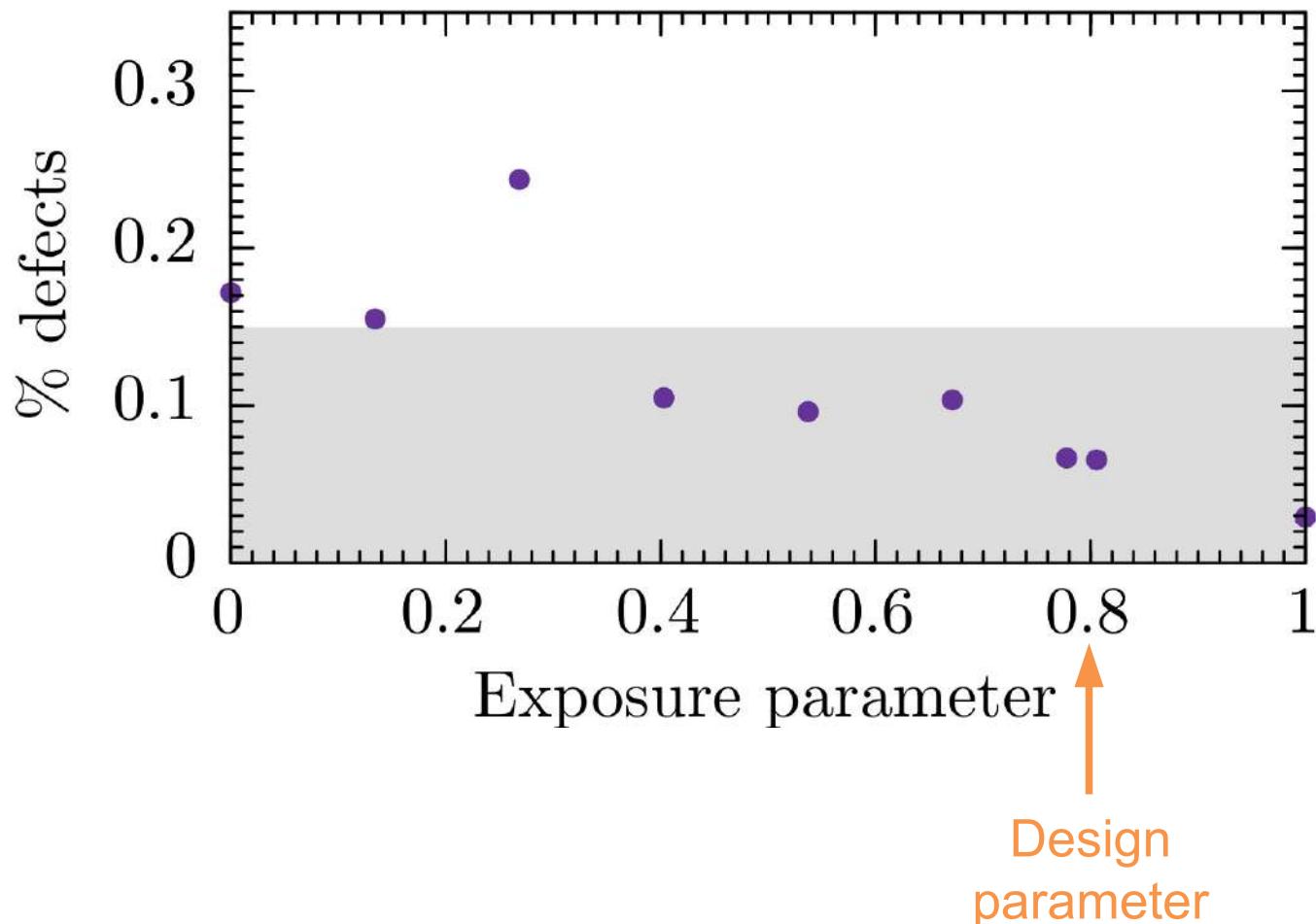
$T_{HT}$  1300°C



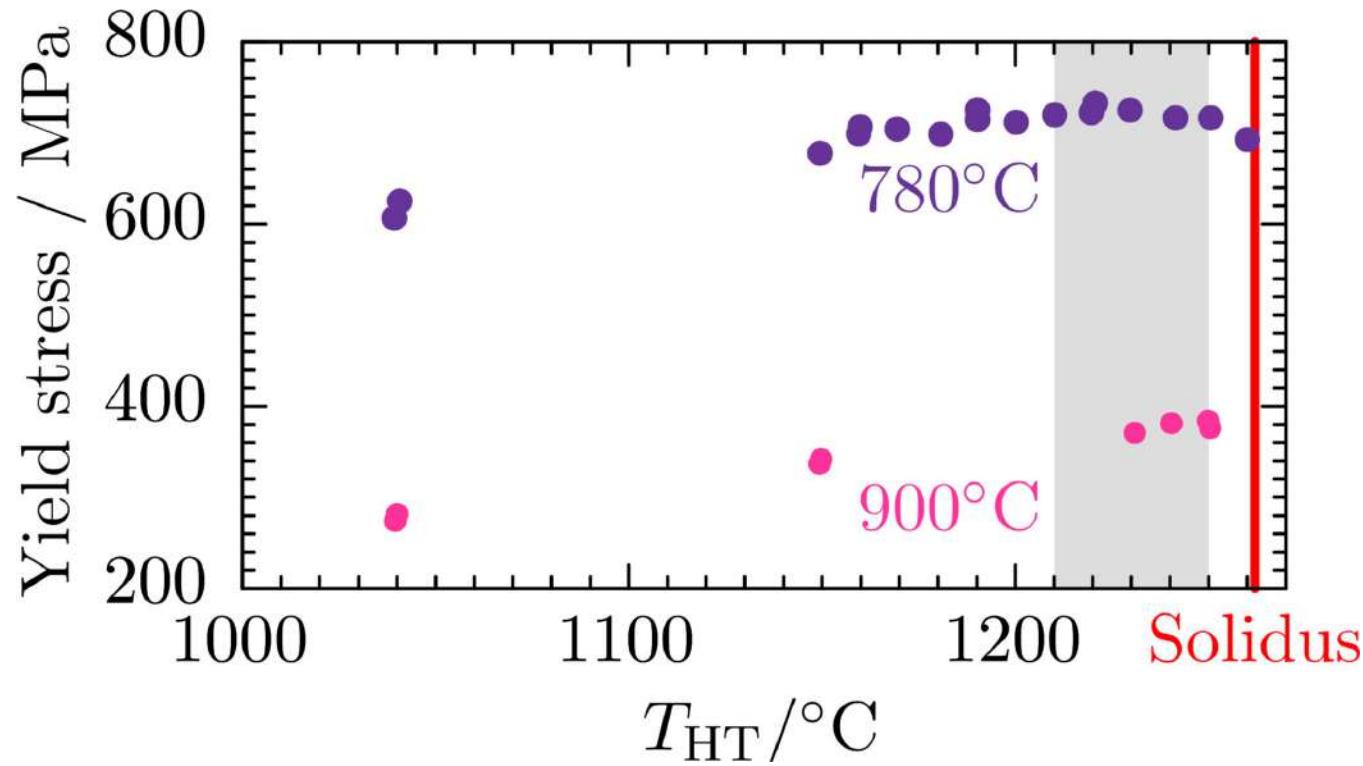
# Microstructure



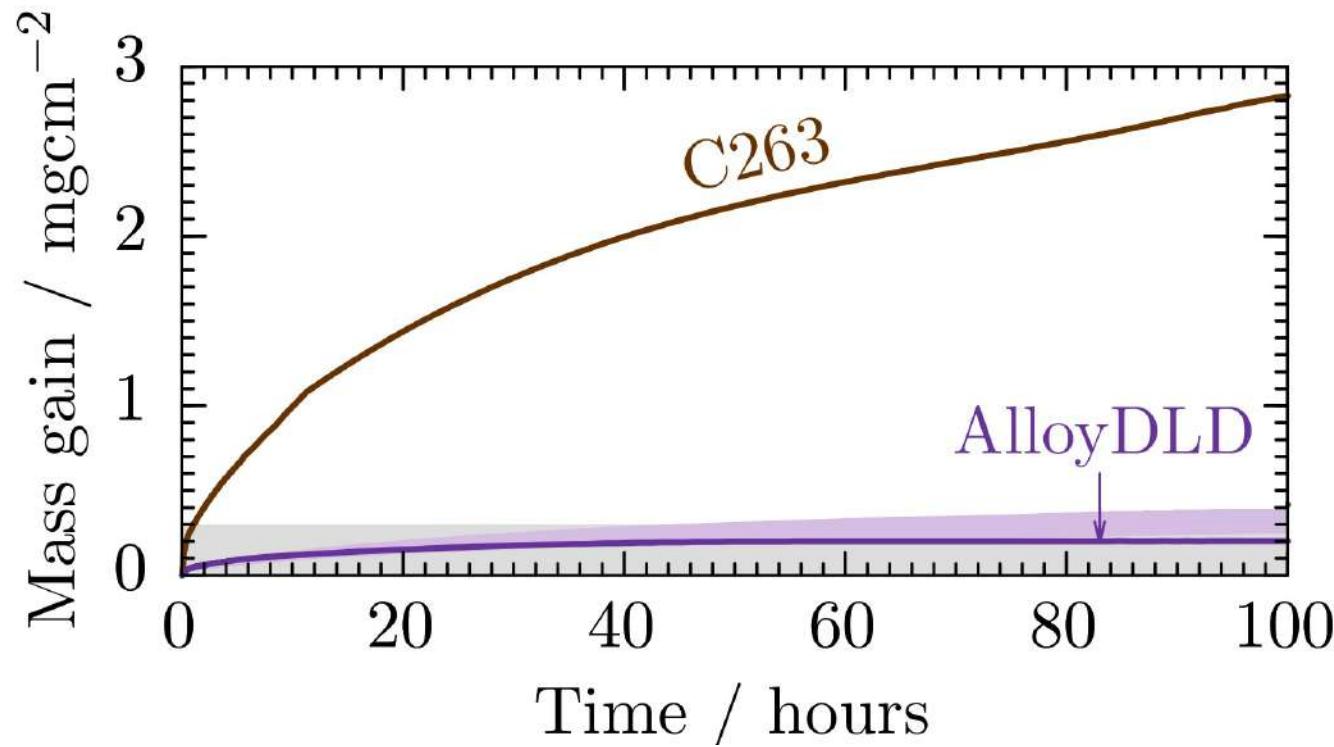
# Testing the processability: horizontal printing



# Testing the processability: horizontal printing



# Testing the oxidation resistance



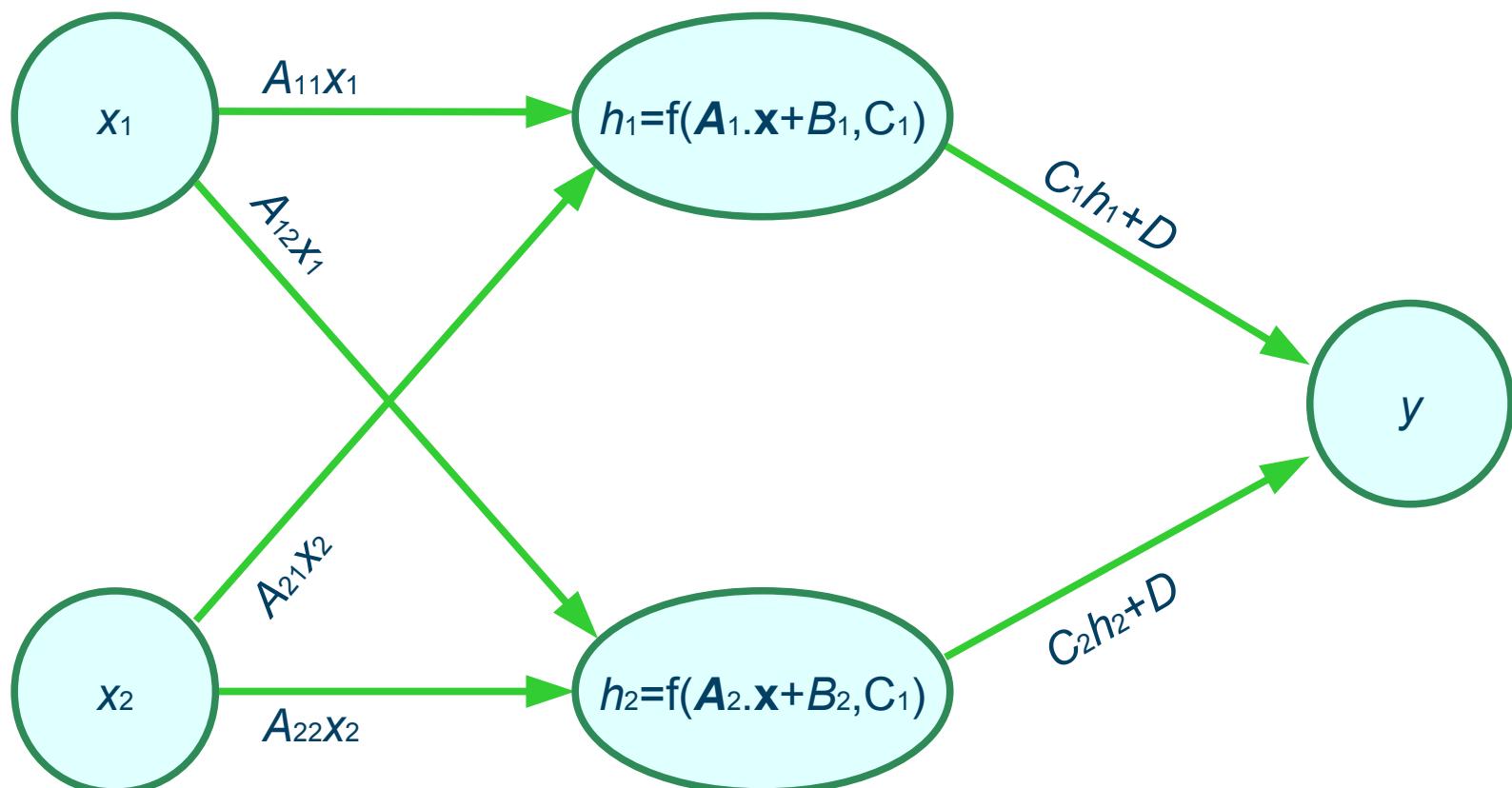
# Printing components for an engine



Materials  
Solutions



# Underlying neural network



# Neural network of multiple variables

$$y = D + C \frac{\vec{A} \cdot \vec{x} + B}{|\vec{A} \cdot \vec{x} + B| + |C|}$$

# Taylor expand the neural network

$$y = D + C \frac{\vec{A} \cdot \vec{x} + B}{|\vec{A} \cdot \vec{x} + B| + |C|}$$
$$= \begin{cases} D + \vec{A} \cdot \vec{x} + B & |\vec{A} \cdot \vec{x} + B| \ll |C| \\ D + C \operatorname{sign}(\vec{A} \cdot \vec{x} + B) & |\vec{A} \cdot \vec{x} + B| \gg |C| \end{cases}$$

# Physical formulae with multiplication

$$\mu = \frac{\tau_i}{3\sigma_y}$$

$$\kappa = \frac{6E_d' h \sigma_d}{E_s' H^2}$$

$$i_L = \frac{ZFDL}{\delta}$$

$$E = \frac{1}{2} kx^2$$

$$\sigma = \frac{3FL}{2bd^2}$$

$$V = IR$$

$$PV = nk_B T$$

$$\rho = \frac{AR}{L}$$

$$\lambda = \left( \frac{m}{ne^2 \mu_0} \right)^{1/2}$$

# Physical formulae with addition and multiplication

$$\mu = \frac{\tau_i}{3\sigma_y}$$

$$\kappa = \frac{6E_d'h\sigma_d}{E_s'H^2}$$

$$i_L = \frac{ZFD C}{\delta}$$

$$E = \frac{1}{2} kx^2$$

$$\sigma = \frac{3FL}{2bd^2}$$

$$\omega = \left( \frac{k(m_1+m_2)}{m_1 m_2} \right)^{1/2}$$

$$i_A = i_0 \exp\left(\frac{azF\eta}{RT}\right)$$

$$V = IR$$

$$PV = n k_B T$$

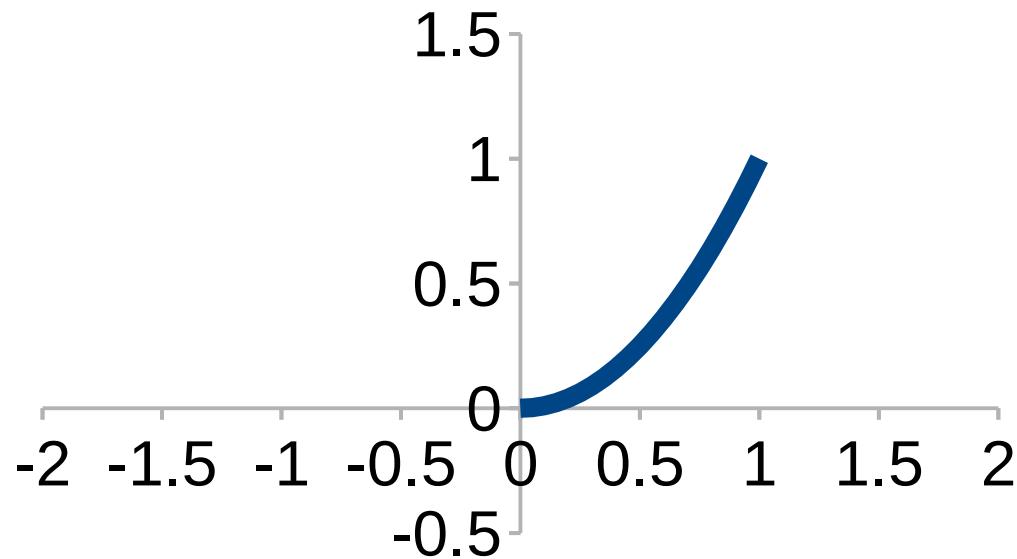
$$\rho = \frac{AR}{L}$$

$$V = I(R_1 + R_2)$$

$$\epsilon = A \sigma^n \exp(-Q/RT)$$

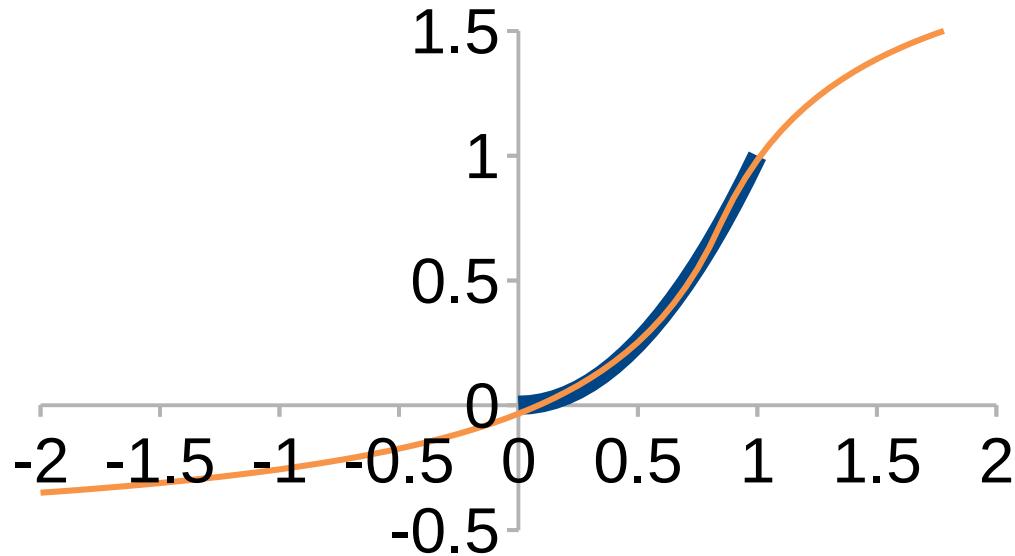
$$\lambda = \left( \frac{m}{n e^2 \mu_0} \right)^{1/2}$$

# Training data to enable multiplication



# Neural network to replicate the parabola

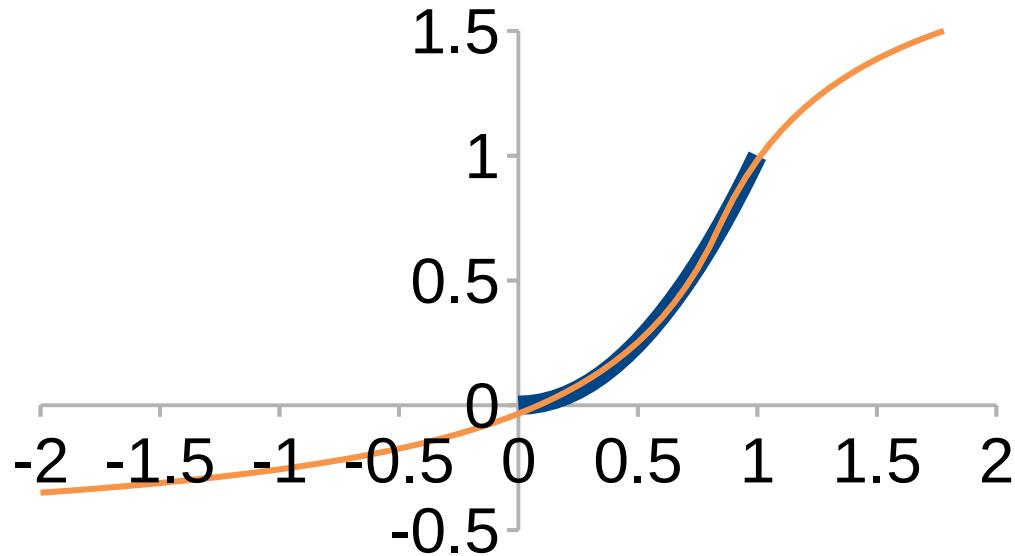
1) Shift the activation function into squared region



$$y = 0.57 + \frac{1.2(2.01x - 1.85)}{|2.01x - 1.85| + 1.2}$$

# Neural network to replicate multiplication

1) Shift the activation function into squared region



$$y = 0.57 + \frac{1.2(2.01x - 1.85)}{|2.01x - 1.85| + 1.2}$$

2) Combine two activation functions in the square region

$$y = \underbrace{\left( \frac{x_1}{2} + \frac{x_2}{2} \right)^2}_{\text{Node 1}} - \underbrace{\left( \frac{x_1}{2} - \frac{x_2}{2} \right)^2}_{\text{Node 2}} = x_1 x_2$$

# Can we do better with logarithms?

$$\log y = \underbrace{(\log x_1 + \log x_2)}_{\text{Node 1}} = \log(x_1 x_2)$$

$$y = x_1 x_2$$

Becomes tricky when  $x < 0$ , and cannot recover addition

# Blend addition and multiplication into one kernel

$$y = D + \bar{\alpha} \bar{y} + \sum_i \frac{\alpha_i C_i (\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i)}{|\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i| + |C_i|}$$

# Blend addition and multiplication into one kernel

$$y = D + \bar{\alpha} \bar{y} + \sum_i \frac{\alpha_i C_i (\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i)}{|\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i| + |C_i|}$$
$$- \left[ \prod_j \text{sign}(x_j) \right] \sum_i \frac{(1 - \alpha_i) C_i B_i \prod_j |x_j|^{A_{ij}}}{|B_i| \prod_j |x_j|^{A_{ij}} + |C_i|}$$

## Recover addition

$$y = D + \bar{\alpha} \bar{y} + \sum_i \frac{\alpha_i C_i (\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i)}{|\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i| + |C_i|}$$
$$- \left[ \prod_j \text{sign}(x_j) \right] \sum_i \frac{(1 - \alpha_i) C_i B_i \prod_j |x_j|^{A_{ij}}}{|B_i| \prod_j |x_j|^{A_{ij}} + |C_i|}$$

When  $\alpha=1$  and for small  $x$  recover addition

$$y = D + \bar{y} + \sum_i [\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i]$$

# Recover multiplication

$$y = D + \bar{\alpha} \bar{y} + \sum_i \frac{\alpha_i C_i (\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i)}{|\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i| + |C_i|}$$
$$- \left[ \prod_j \text{sign}(x_j) \right] \sum_i \frac{(1 - \alpha_i) C_i B_i \prod_j |x_j|^{A_{ij}}}{|B_i| \prod_j |x_j|^{A_{ij}} + |C_i|}$$

When  $\alpha=0$  and for small  $x \geq 0$  recover multiplication

$$y = D - \sum_i B_i \prod_j x_j^{A_{ij}}$$

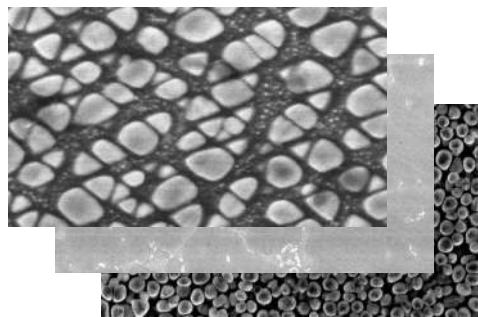
# Addition-multiplication merging improves performance

$$y = D + \bar{\alpha} \bar{y} + \sum_i \frac{\alpha_i C_i (\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i)}{|\vec{A}_i \cdot (\vec{x} - \vec{\bar{x}}) + B_i| + |C_i|}$$
$$- \left[ \prod_j \text{sign}(x_j) \right] \sum_i \frac{(1 - \alpha_i) C_i B_i \prod_j |x_j|^{A_{ij}}}{|B_i| \prod_j |x_j|^{A_{ij}} + |C_i|}$$

Addition-product merging improves performance by ~**50%**

# Materials designed

Nickel and molybdenum



Experiment and DFT for batteries

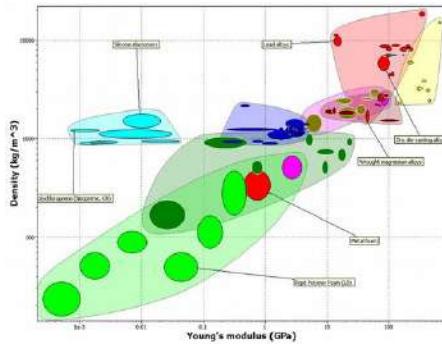


Steel for welding



# More materials

Identified and corrected errors in materials database



**GRANTA**  
MATERIAL INSPIRATION

Lubricants with molecular dynamics and experiments

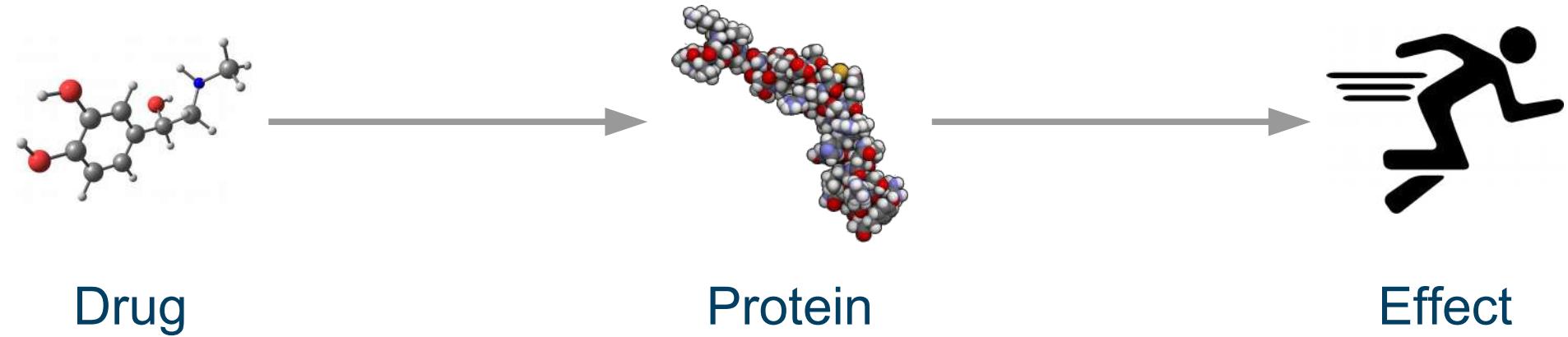


Drug design



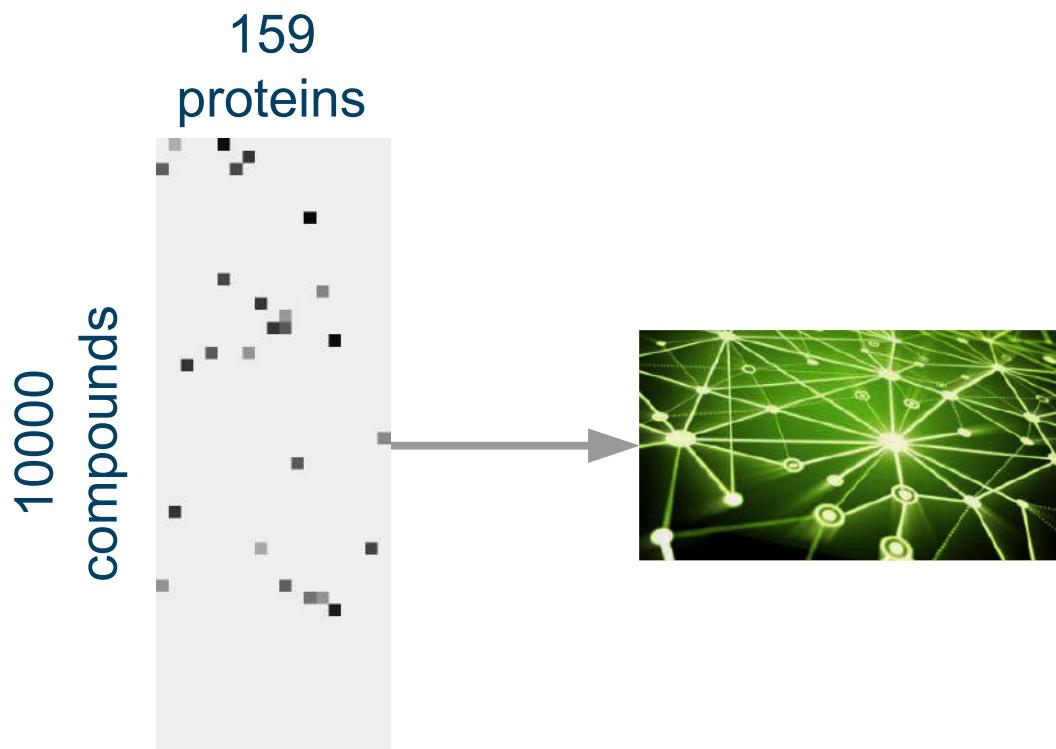
e-therapeutics  
**optibrium**  
**Takeda**

# Action of a drug



# Novartis dataset to benchmark machine learning

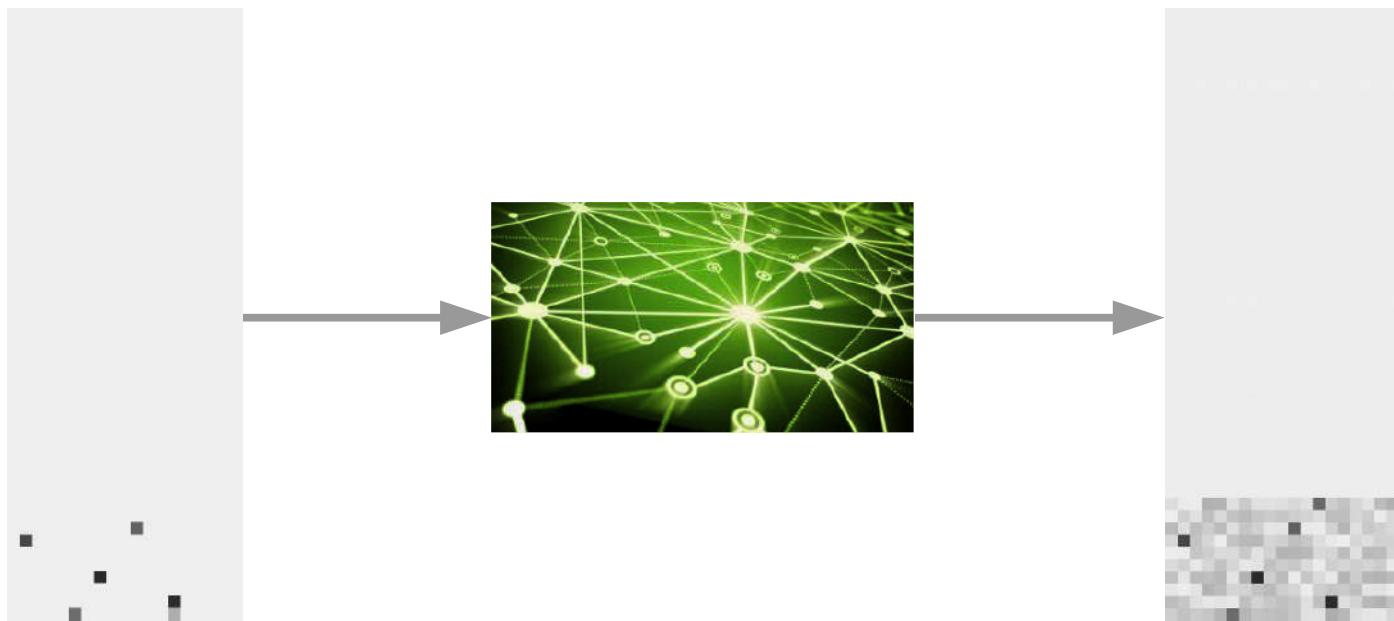
159 kinase proteins, 10000 compounds, data 5% complete



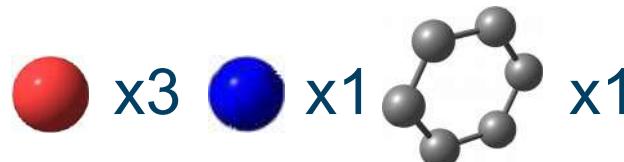
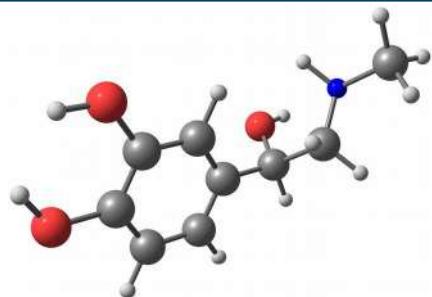
Data from ChEMBL  
Martin, Polyakov, Tian, and Perez,  
J. Chem. Inf. Model. 57, 2077 (2017)

# Impute missing entries to validate

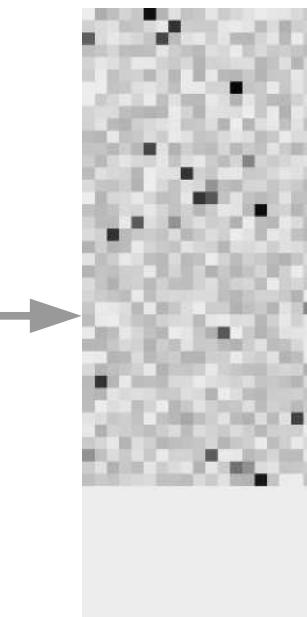
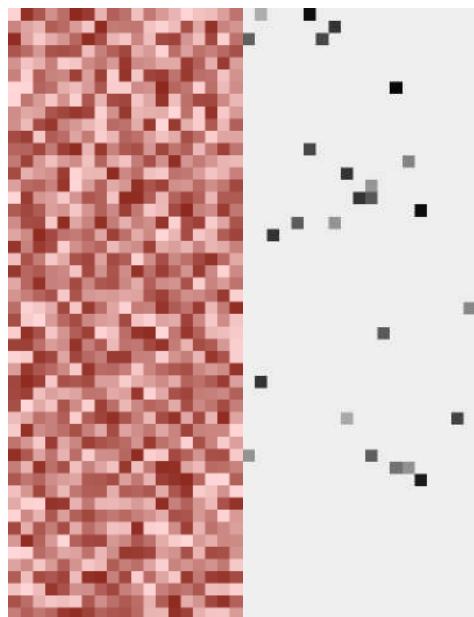
Validate using a realistically split holdout data set, extrapolate to new chemical space



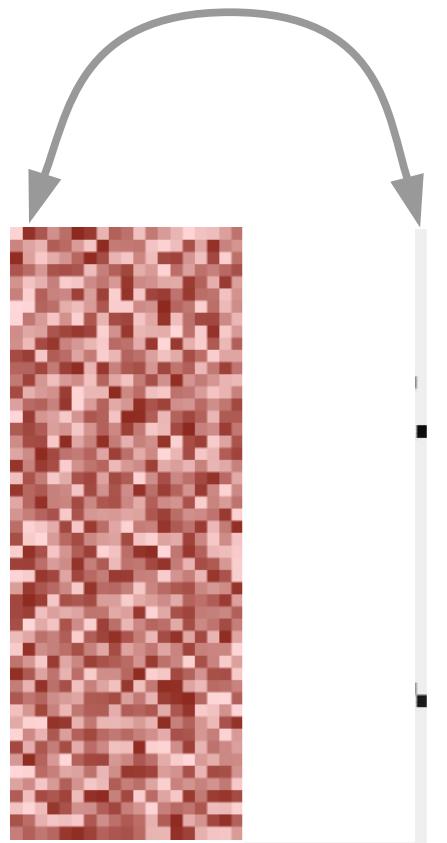
# Quantitative structure-activity relationships



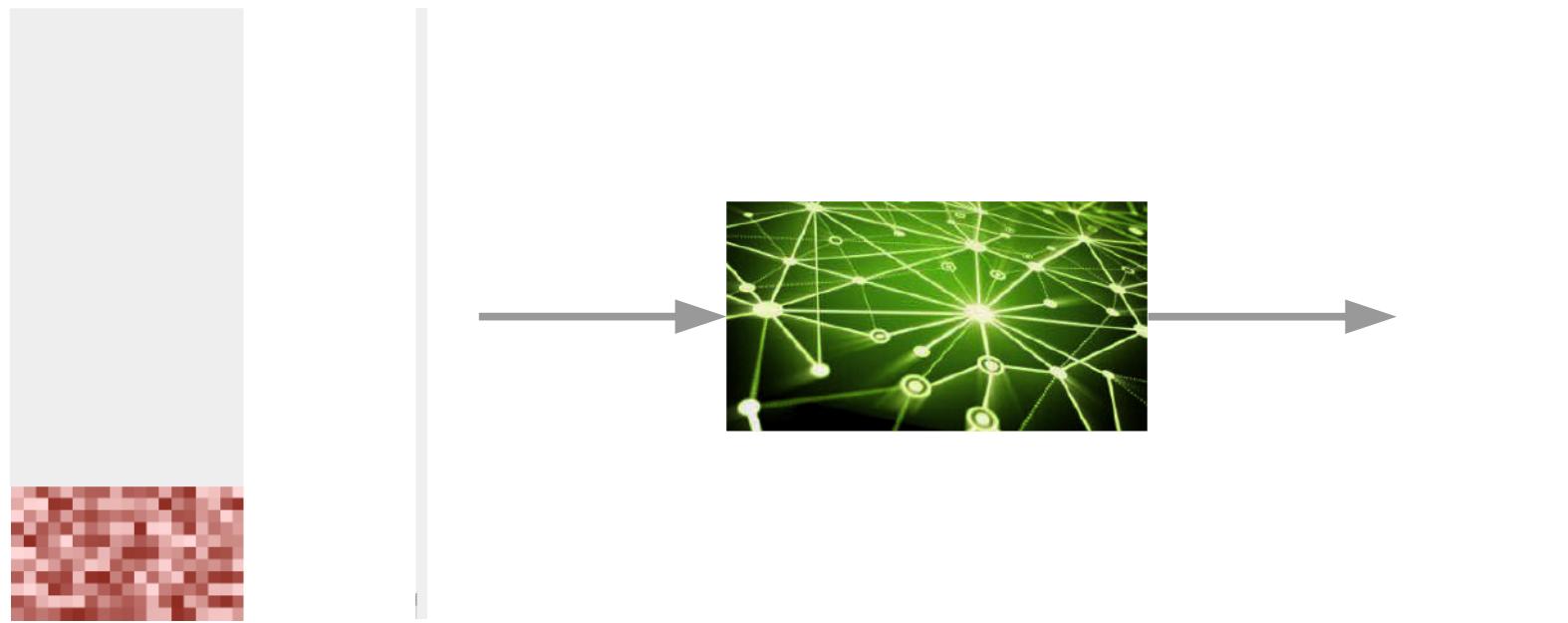
Molecular weight=183 Da



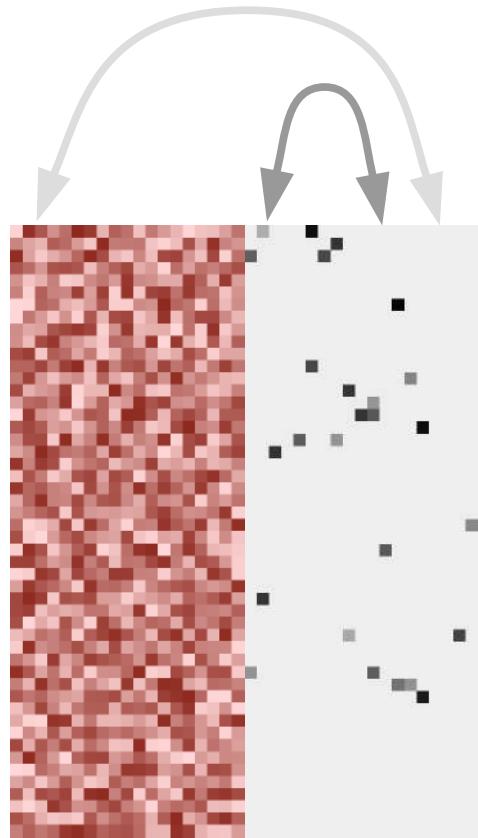
# Quantitative structure-activity relationships



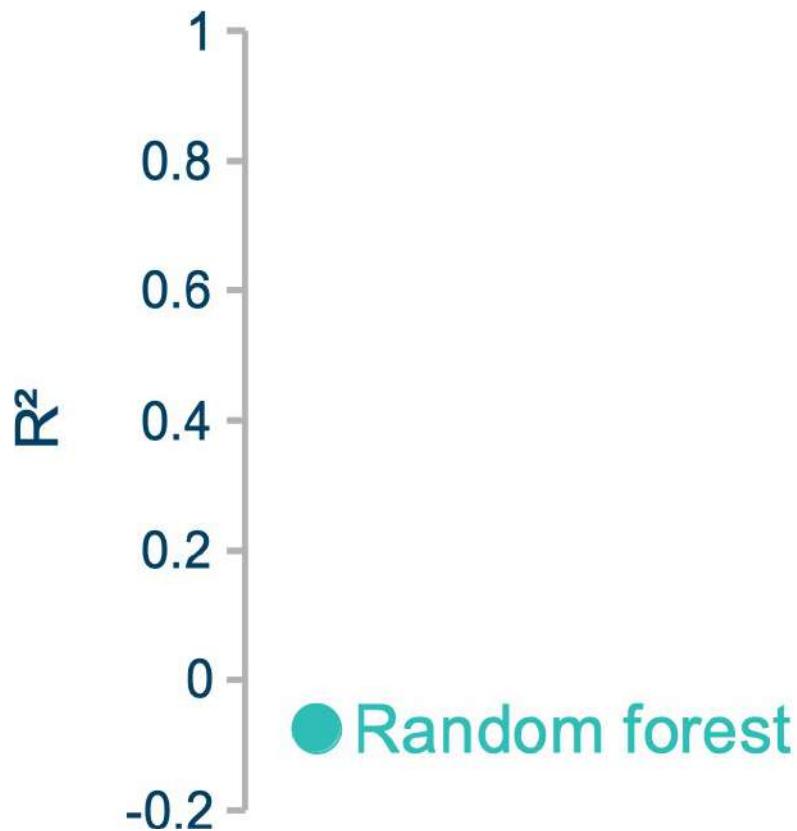
# Predict one column at a time



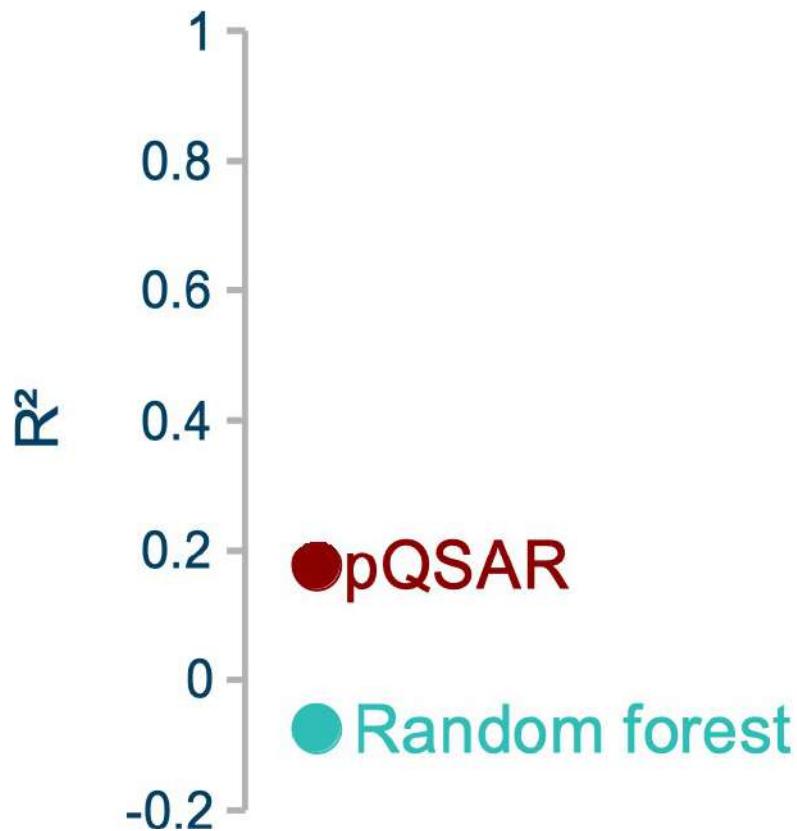
# Learn protein-protein correlations



# Random forest

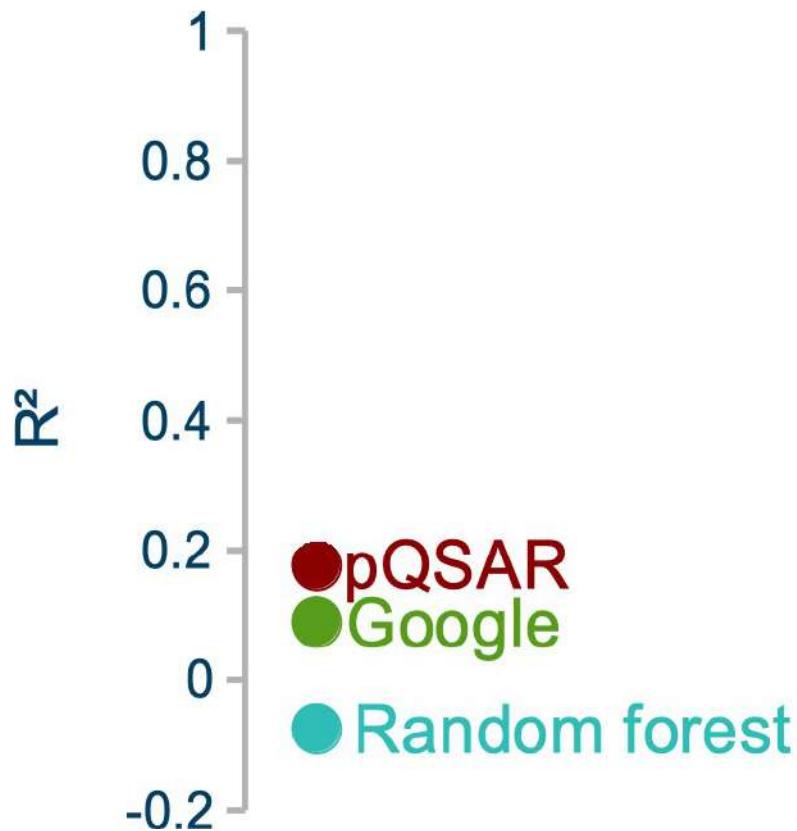


# Predictions from pQSAR

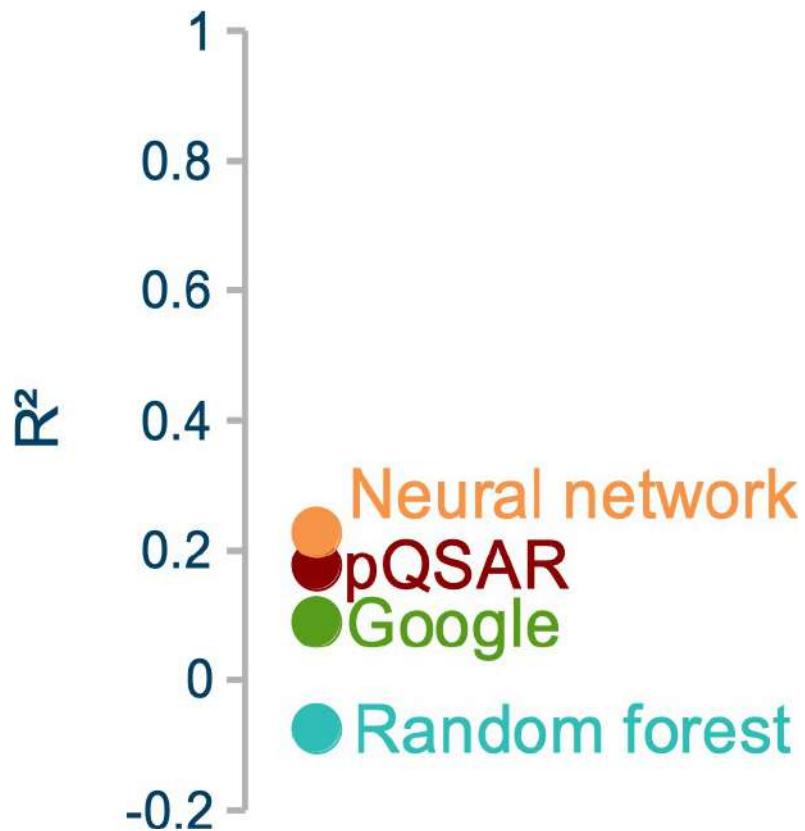


Martin, Polyakov, Tian, and Perez,  
J. Chem. Inf. Model. 57, 2077 (2017)

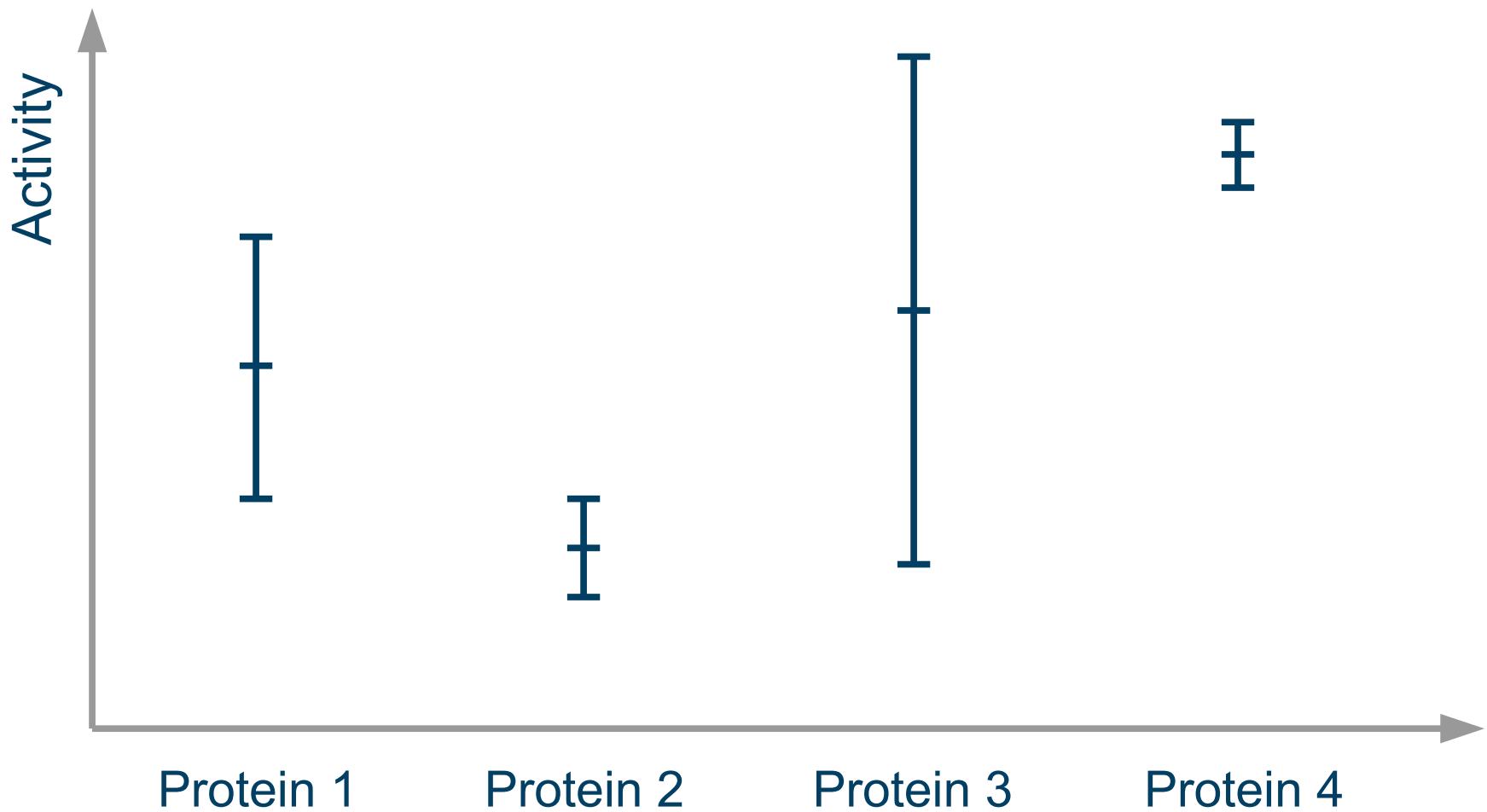
# Google's attempt



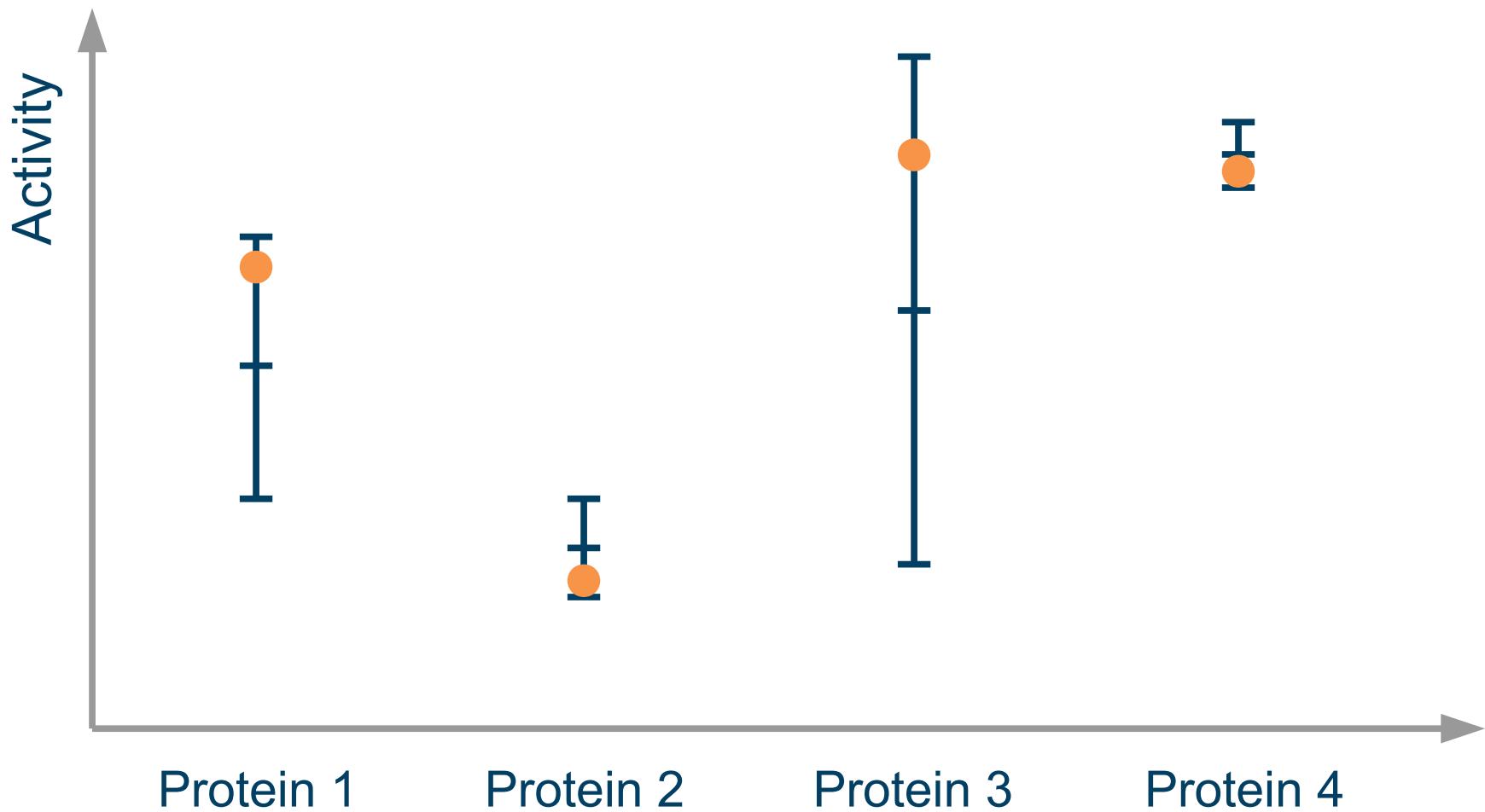
# Neural network with missing data



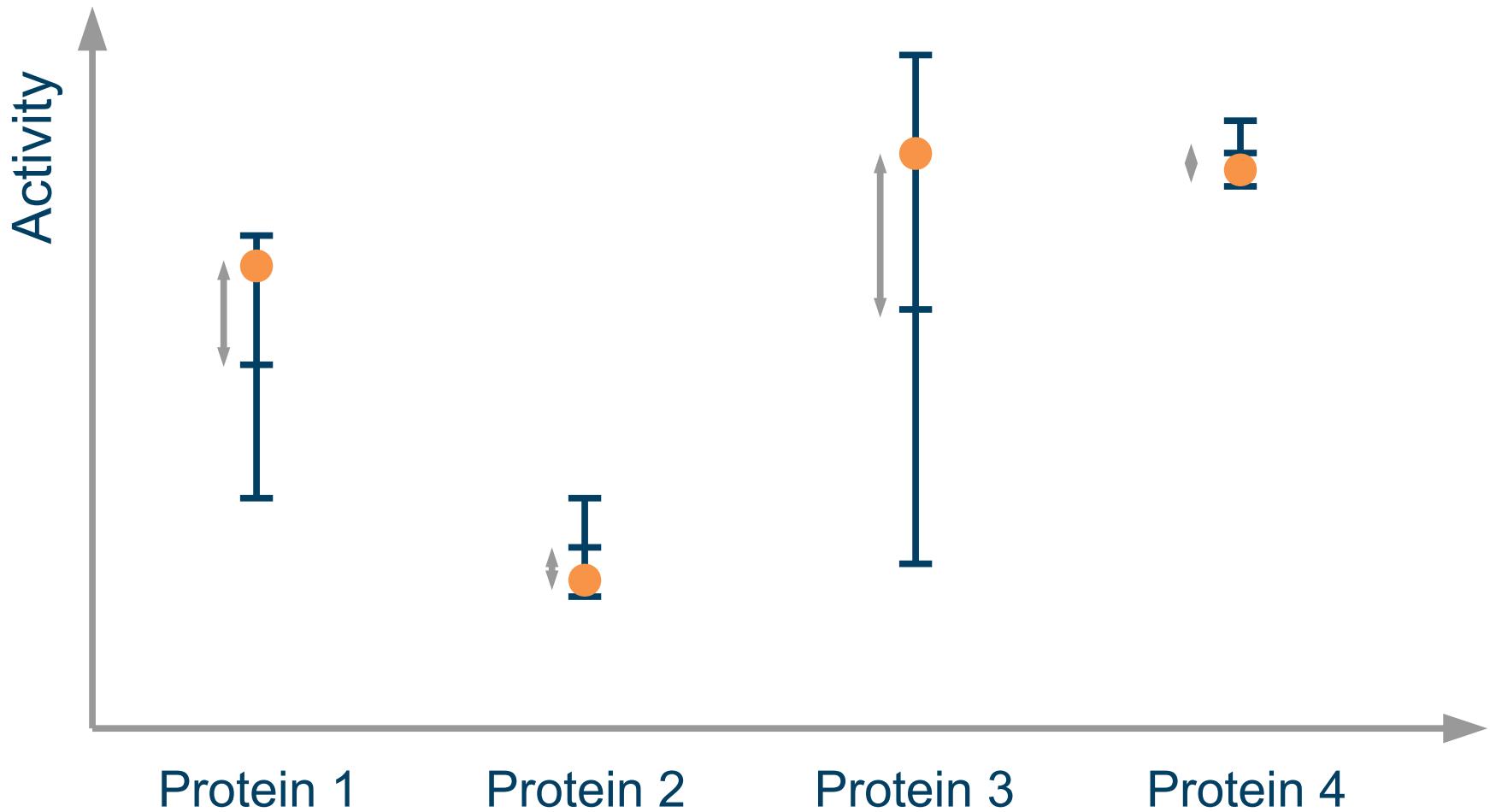
# Predictions have an uncertainty



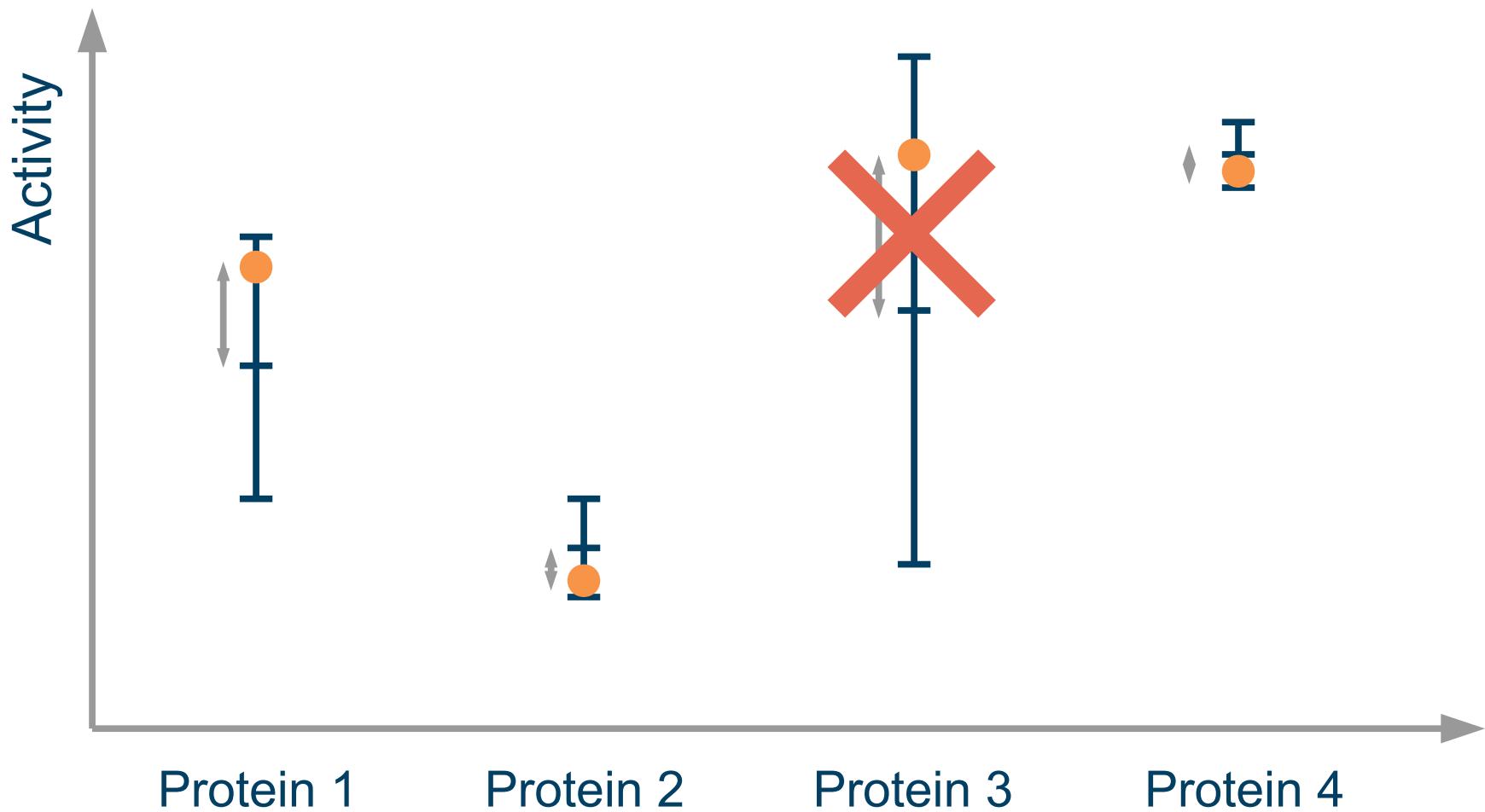
# Validation data typically within one standard deviation



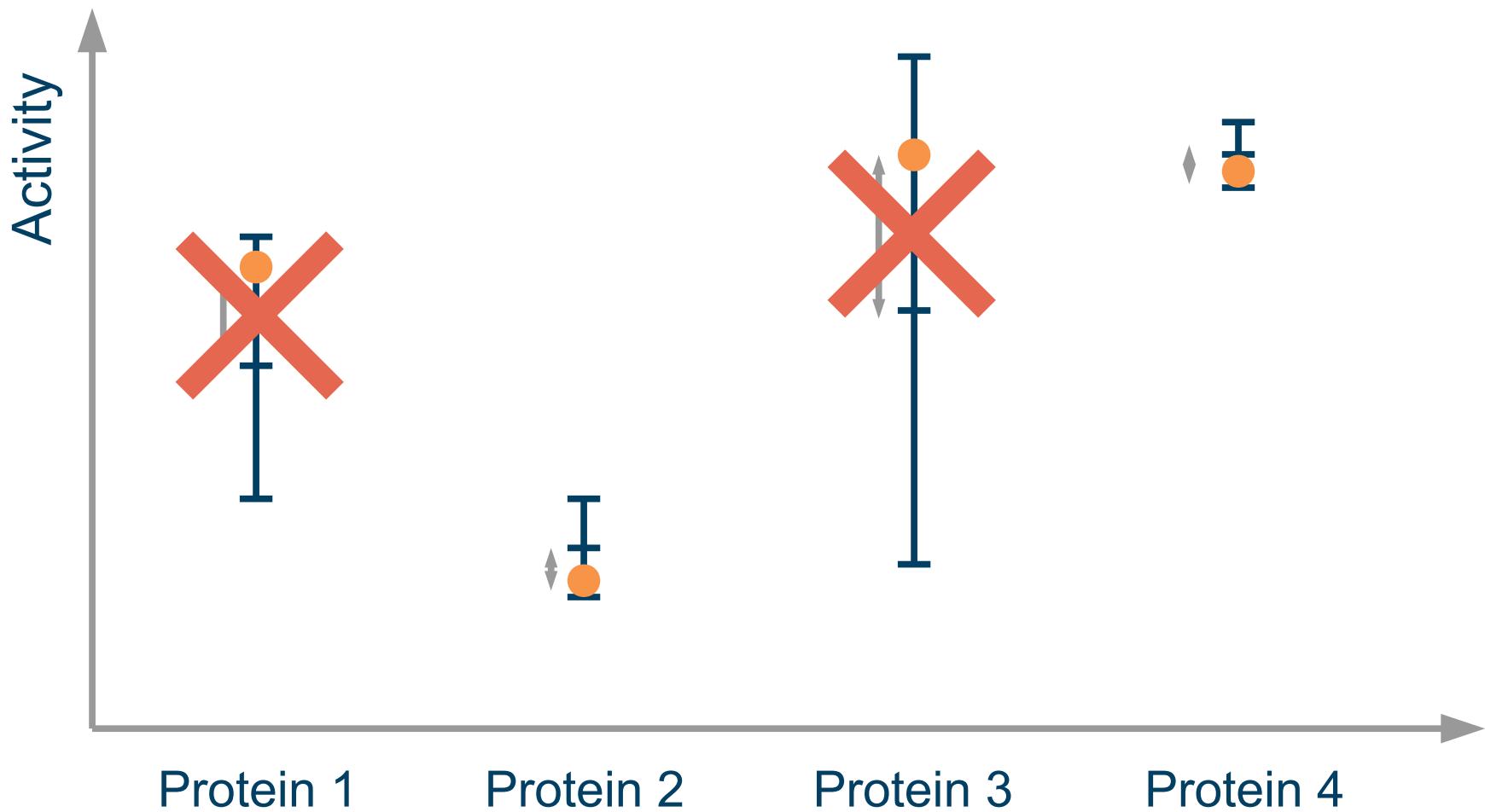
# $R^2$ metric calculated with difference from mean



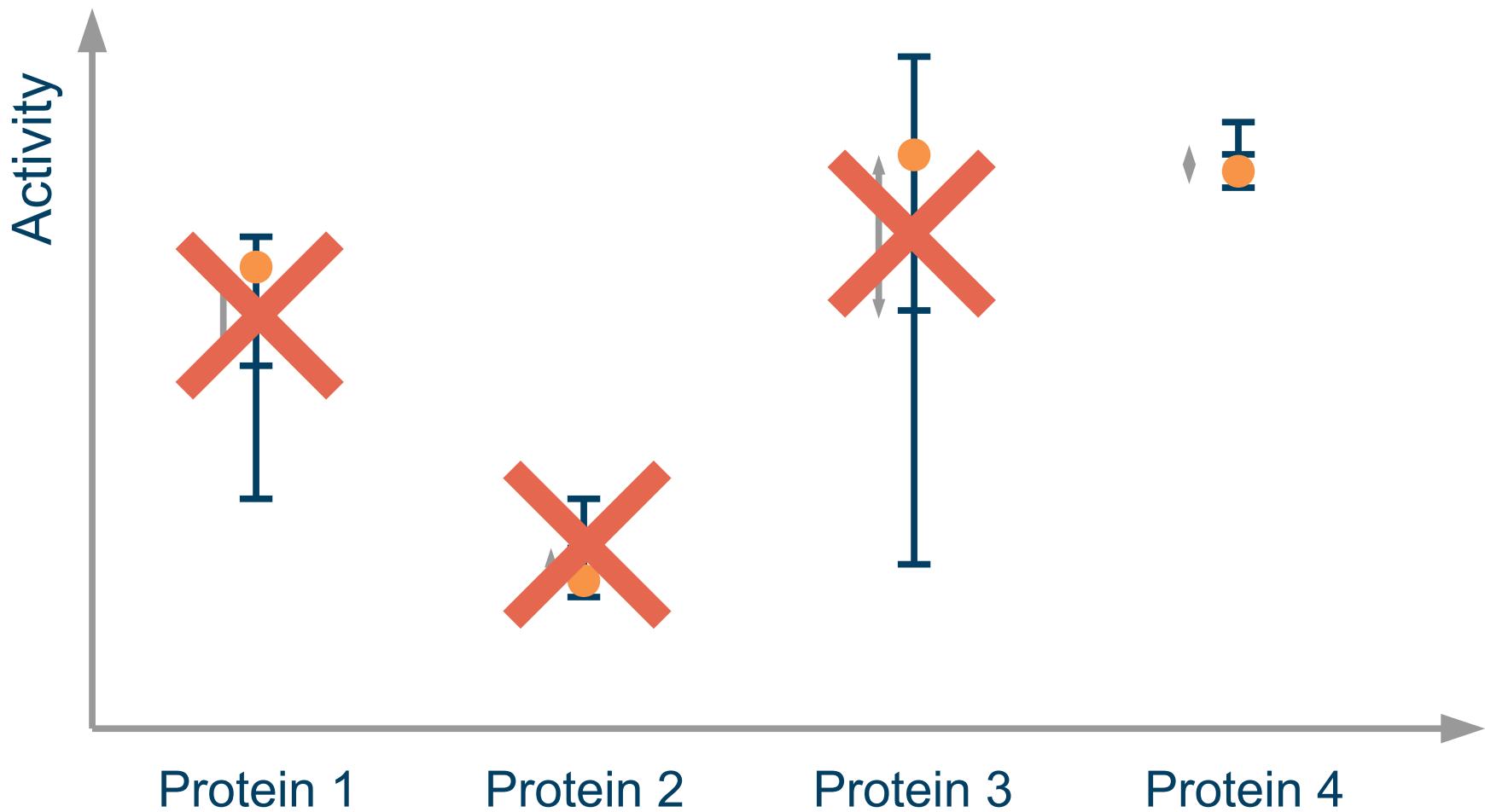
# Impute 75% of data with smallest uncertainty



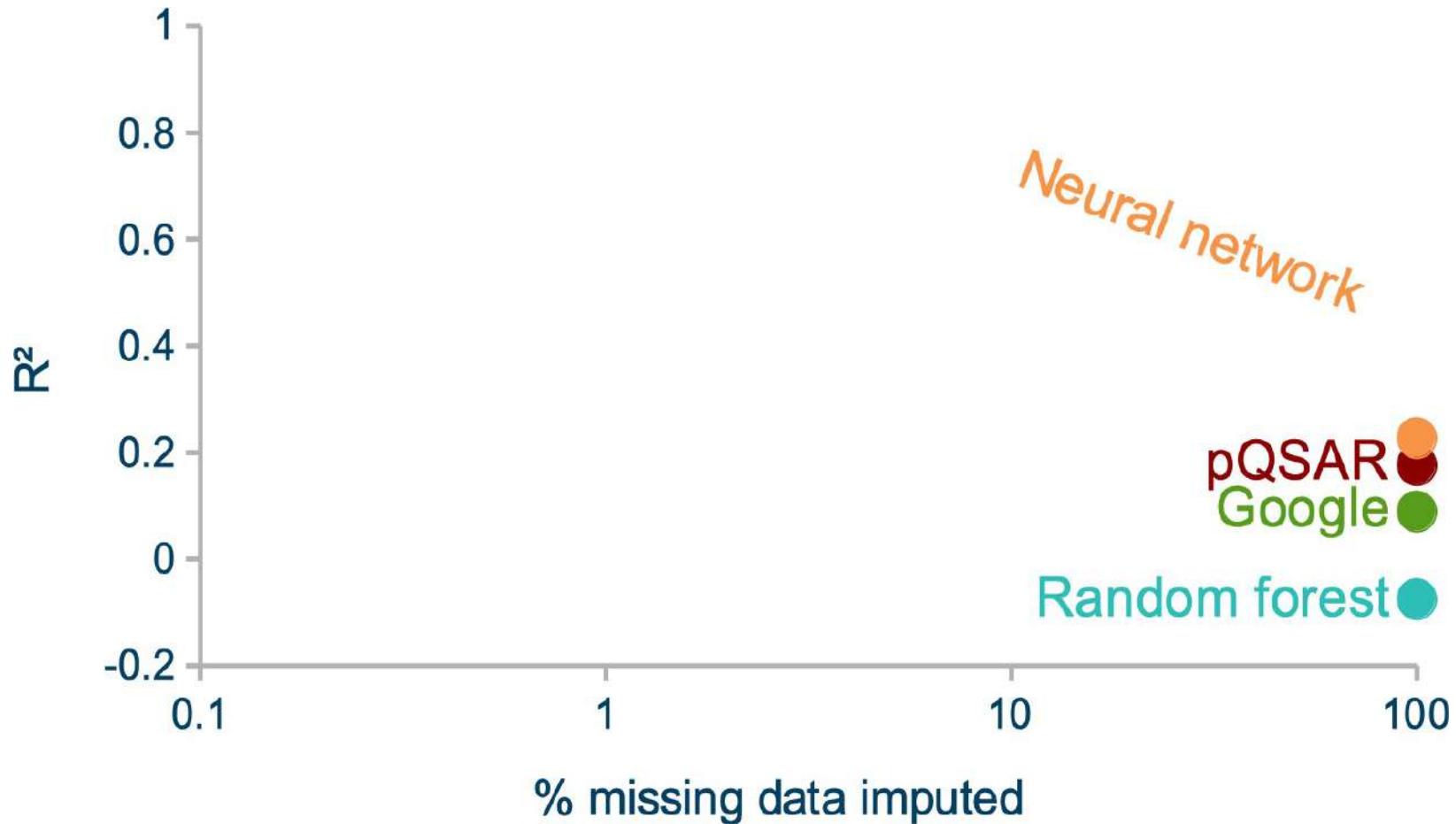
# Impute 50% of data with smallest uncertainty



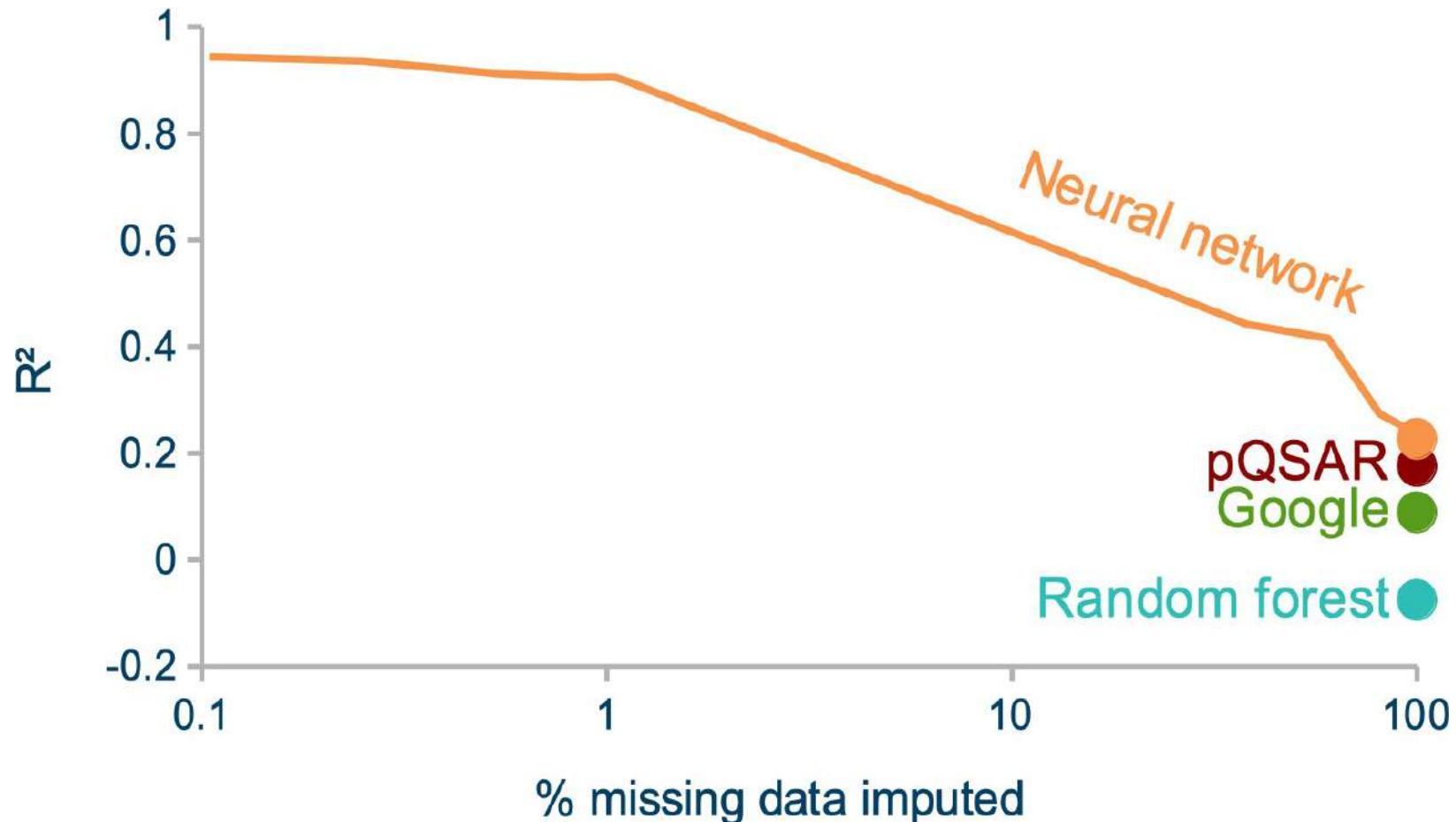
# Impute 25% of data with smallest uncertainty



# Improved performance by exploiting uncertainty



# Improved performance by exploiting uncertainty



# Different drugs can treat the same ailment



# Roadmap to productization

Reseller agreement with drug discovery software company  
**Optibrium**

Machine learning tool embedded into next generation of  
Optibrium software for release in **October 2020**



# Summary

Merge different experimental quantities and computer simulations into a **holistic** design tool

Exploit **mathematical knowledge** about physical relationships

Designed and experimentally verified alloy for **direct laser deposition**

Improved predictability of drug design from  $R^2=0.18$  to  **$R^2=0.93$**