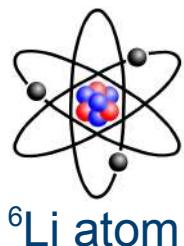


Cold atoms in a spin

Gareth Conduit¹ & Curt von Keyserlingk²

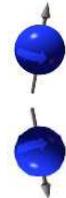
1. TCM Group, Cambridge; 2. Theoretical Physics, Oxford

Ketterle's experiment



${}^6\text{Li}$ atom

$|F = 1/2, m_F = 1/2\rangle$

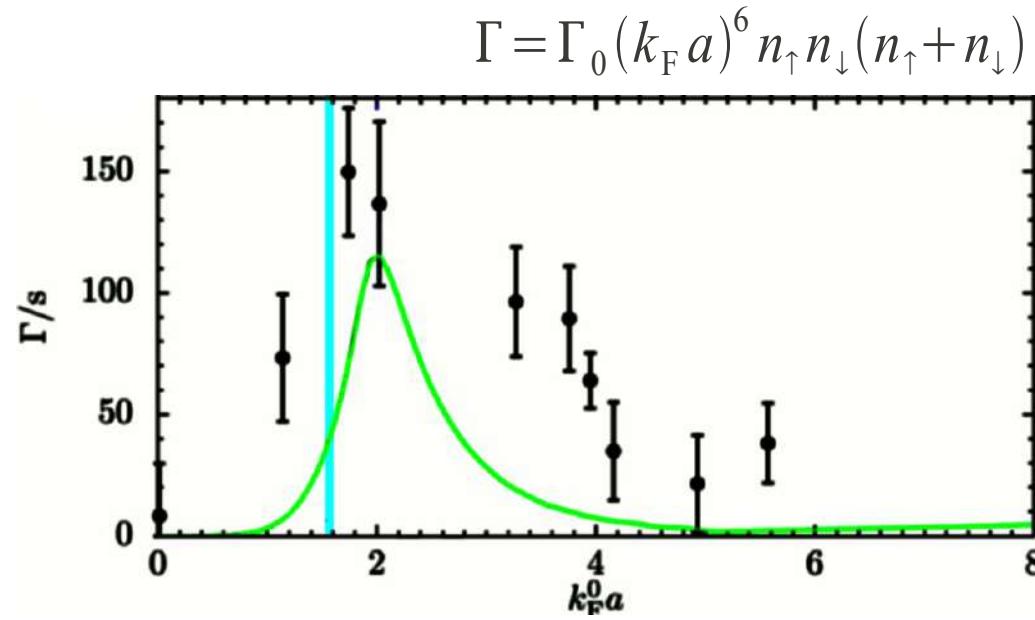
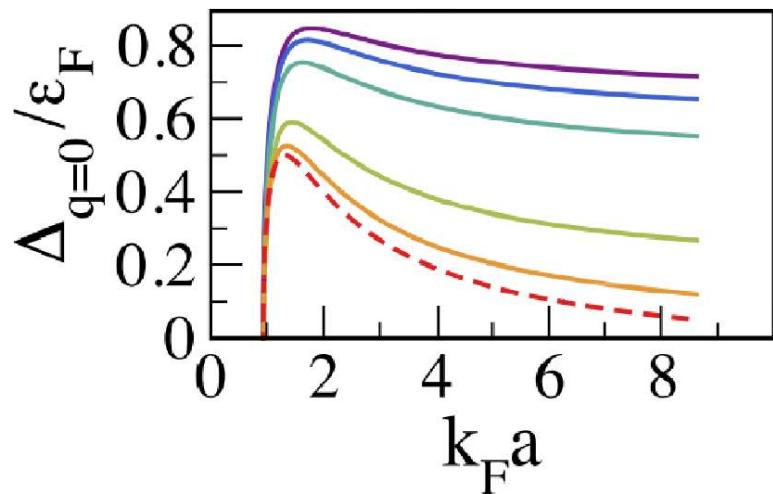


Up spin electron

$|F = 1/2, m_F = -1/2\rangle$



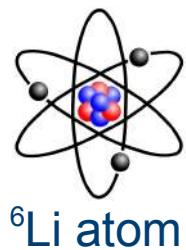
Down spin electron



Jo et al, Science **325**, 1521 (2009); GJC & Simons PRL **103**, 200403 (2009)

Pekker et al, PRL **106**, 050402 (2011); Petrov, PRA **67**, 010703(R) (2003)

Ketterle's experiment



$|F = 1/2, m_F = 1/2\rangle$

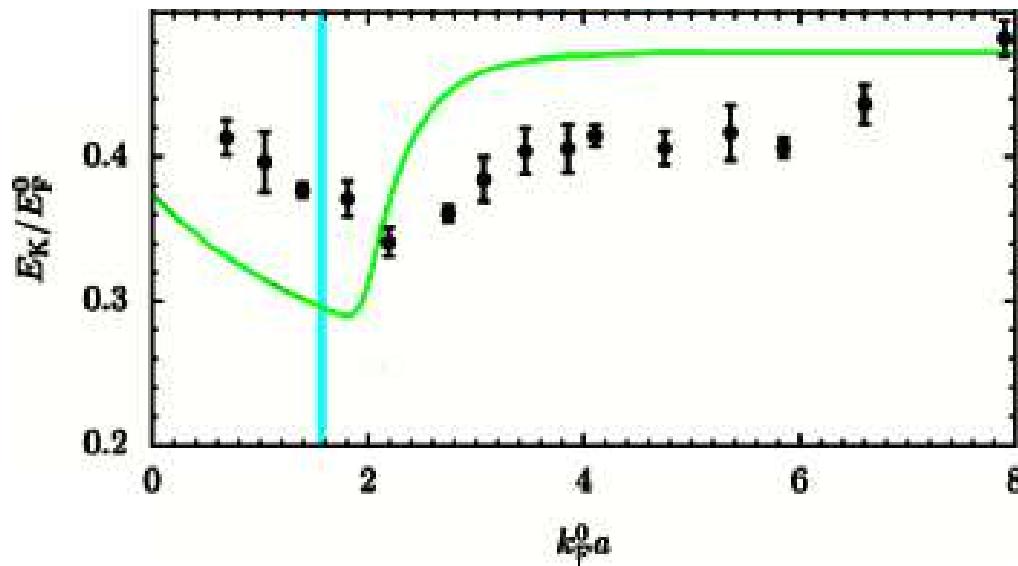
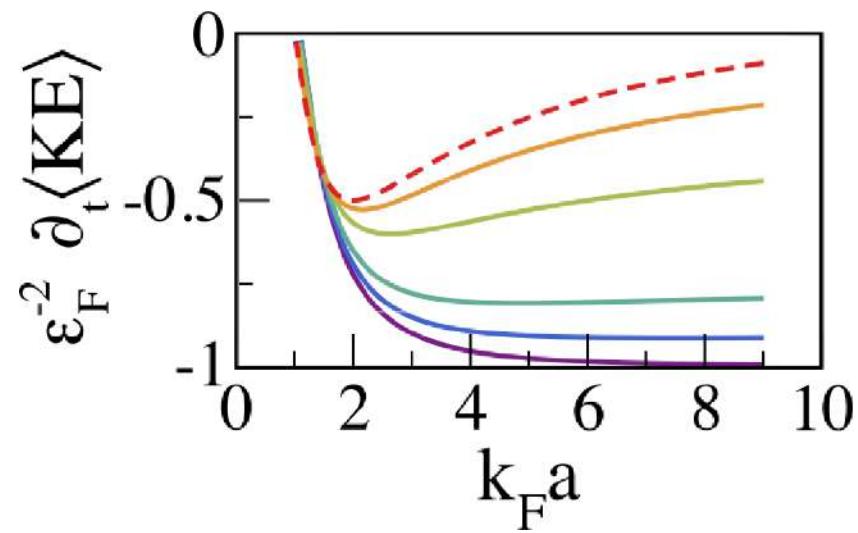


Up spin electron

$|F = 1/2, m_F = -1/2\rangle$



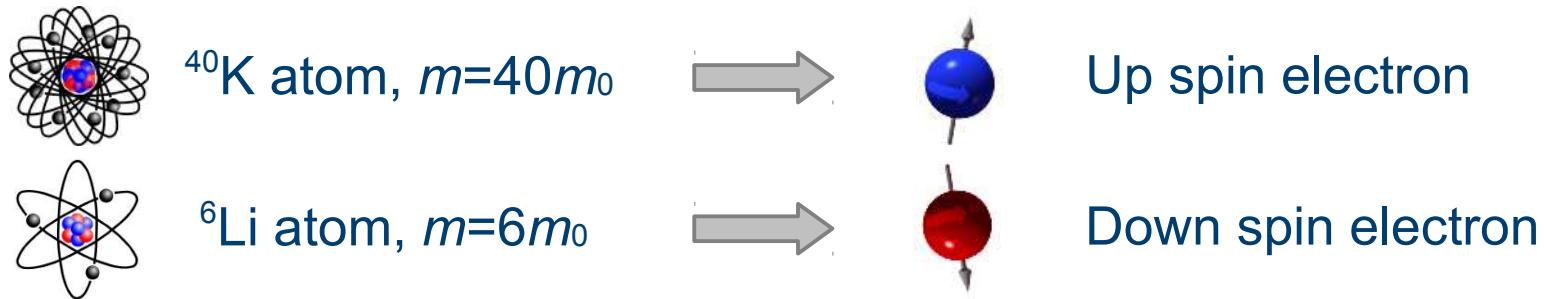
Down spin electron



Mysteries about magnetism

- Competing many-body instabilities
Pekker *et al*, PRL **106**, 050402 (2011)
- Absence of domains
Ho in “Magnetized Gas Points to New Physics”, Science (2009)
- Tan relations
Barth & Zwerger, Annals of Physics **326**, 2544 (2011)
- Instability of fully polarized state
Zhai, PRA **80**, 051605 (2009)
- Textured phases
Uhlárz, Pfleiderer & Hayden, PRL **93**, 256404 (2004)
GJC, Green & Simons, PRL **103**, 207201 (2009)

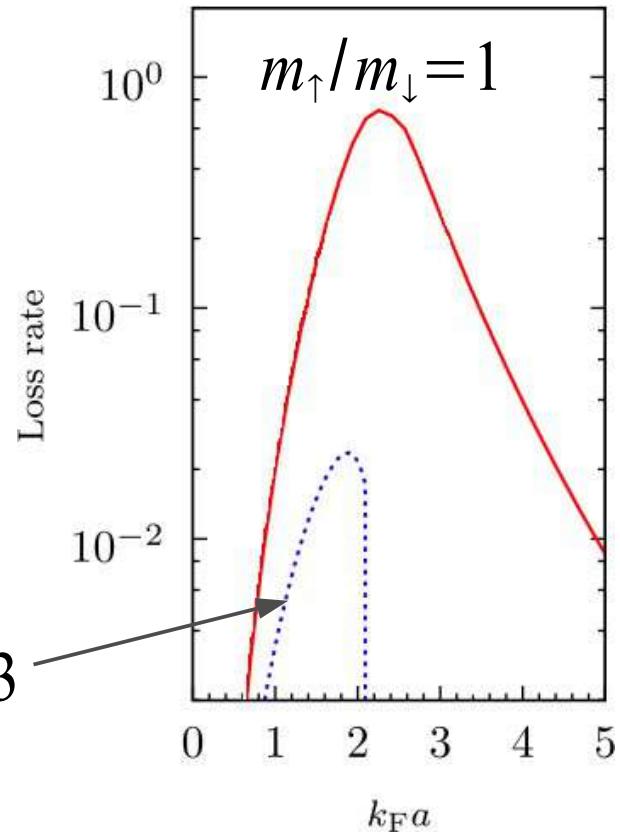
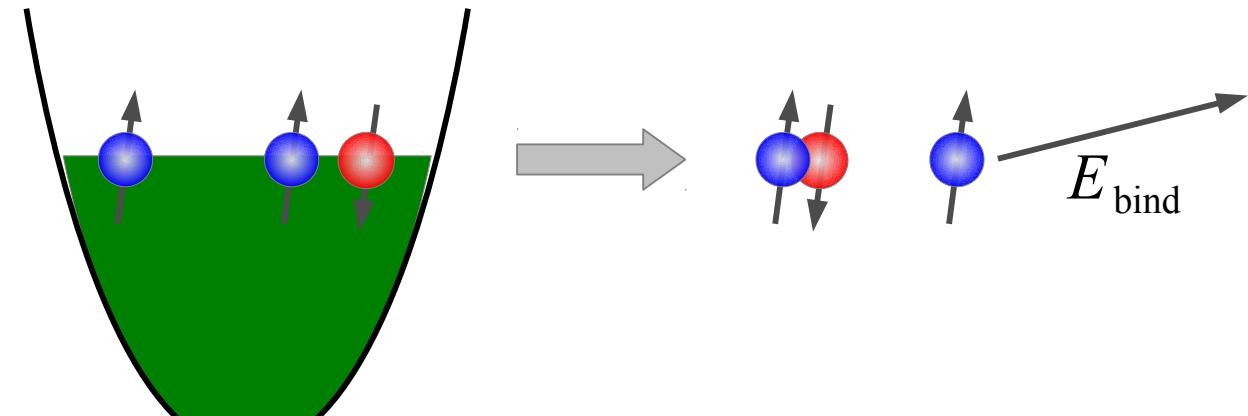
Mass imbalance ferromagnetism



$$\hat{H} = \sum_k \frac{k^2}{2m_\uparrow} c_{k\uparrow}^\dagger c_{k\uparrow} + \sum_k \frac{k^2}{2m_\downarrow} c_{k\downarrow}^\dagger c_{k\downarrow} + g \sum_{kk'q} c_{k\uparrow}^\dagger c_{k'+q\downarrow}^\dagger c_{k'+q\downarrow} c_{k'\uparrow}$$

- Two and three-body losses suppressed
Keyserlingk & GJC, PRA **83**, 053625 (2011)
- Phase separates into just two domains
Keyserlingk & GJC, PRA **83**, 053625 (2011)
- Experimental procedure used to study polarons
Kohstall et al, arXiv:1112.0020; Massignan & Brunn, Eur. Phys. J D 65, 83 (2011);
Massignan arXiv:1112.1029

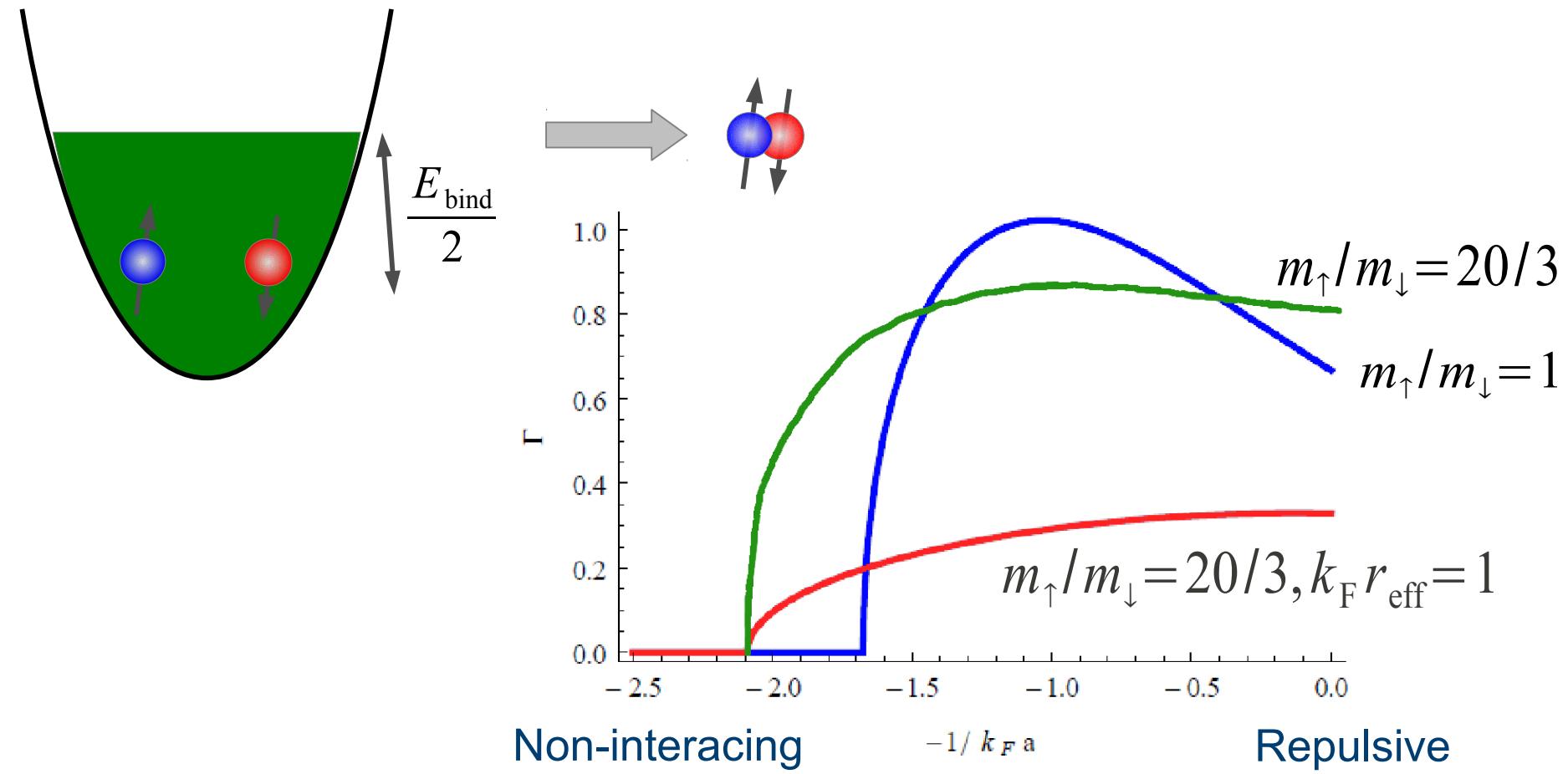
Three-body loss



Petrov, PRA **67**, 010703(R) (2003)

Keyserlingk & GJC, PRA **83**, 053625 (2011)

Two-body loss



Pekker et al, PRL 106, 050402 (2011)

Magnetization instabilities

- Energy change due to magnetization $\delta m_z^{\omega, \vec{q}}$ and $\delta m_{\perp}^{\omega, \vec{q}}$

$$\delta E = g \sum_{\omega, \vec{q}} |\delta m_z^{\omega, \vec{q}}|^2 \left[1 - \frac{g}{2} (\Pi_{\uparrow\downarrow}^{\omega, \vec{q}} + \Pi_{\downarrow\uparrow}^{\omega, \vec{q}}) \right] + g \sum_{\omega, \vec{q}} |\delta m_{\perp}^{\omega, \vec{q}}|^2 \left[\frac{1 - g^2 \Pi_{\uparrow\uparrow}^{\omega, \vec{q}} \Pi_{\downarrow\downarrow}^{\omega, \vec{q}}}{1 - g (\Pi_{\uparrow\uparrow}^{\omega, \vec{q}} + \Pi_{\downarrow\downarrow}^{\omega, \vec{q}})/2} \right]$$

Stoner instability

- Energy change due to magnetization $\delta m_z^{\omega, \vec{q}}$ and $\delta m_{\perp}^{\omega, \vec{q}}$

$$\delta E = g \sum_{\omega, \vec{q}} |\delta m_z^{\omega, \vec{q}}|^2 \left[1 - \frac{g}{2} (\Pi_{\uparrow\downarrow}^{\omega, \vec{q}} + \Pi_{\downarrow\uparrow}^{\omega, \vec{q}}) \right] + g \sum_{\omega, \vec{q}} |\delta m_{\perp}^{\omega, \vec{q}}|^2 \left[\frac{1 - g^2 \Pi_{\uparrow\uparrow}^{\omega, \vec{q}} \Pi_{\downarrow\downarrow}^{\omega, \vec{q}}}{1 - g (\Pi_{\uparrow\uparrow}^{\omega, \vec{q}} + \Pi_{\downarrow\downarrow}^{\omega, \vec{q}})/2} \right]$$

- Instability to phase separation

$$g(v_{\uparrow}v_{\downarrow})^{1/2} = 1$$

Magnetization texture

- Energy change due to magnetization $\delta m_z^{\omega, \vec{q}}$ and $\delta m_{\perp}^{\omega, \vec{q}}$

$$\delta E = g \sum_{\omega, \vec{q}} |\delta m_z^{\omega, \vec{q}}|^2 \left[1 - \frac{g}{2} (\Pi_{\uparrow\downarrow}^{\omega, \vec{q}} + \Pi_{\downarrow\uparrow}^{\omega, \vec{q}}) \right] + g \sum_{\omega, \vec{q}} |\delta m_{\perp}^{\omega, \vec{q}}|^2 \left[\frac{1 - g^2 \Pi_{\uparrow\uparrow}^{\omega, \vec{q}} \Pi_{\downarrow\downarrow}^{\omega, \vec{q}}}{1 - g (\Pi_{\uparrow\uparrow}^{\omega, \vec{q}} + \Pi_{\downarrow\downarrow}^{\omega, \vec{q}})/2} \right]$$

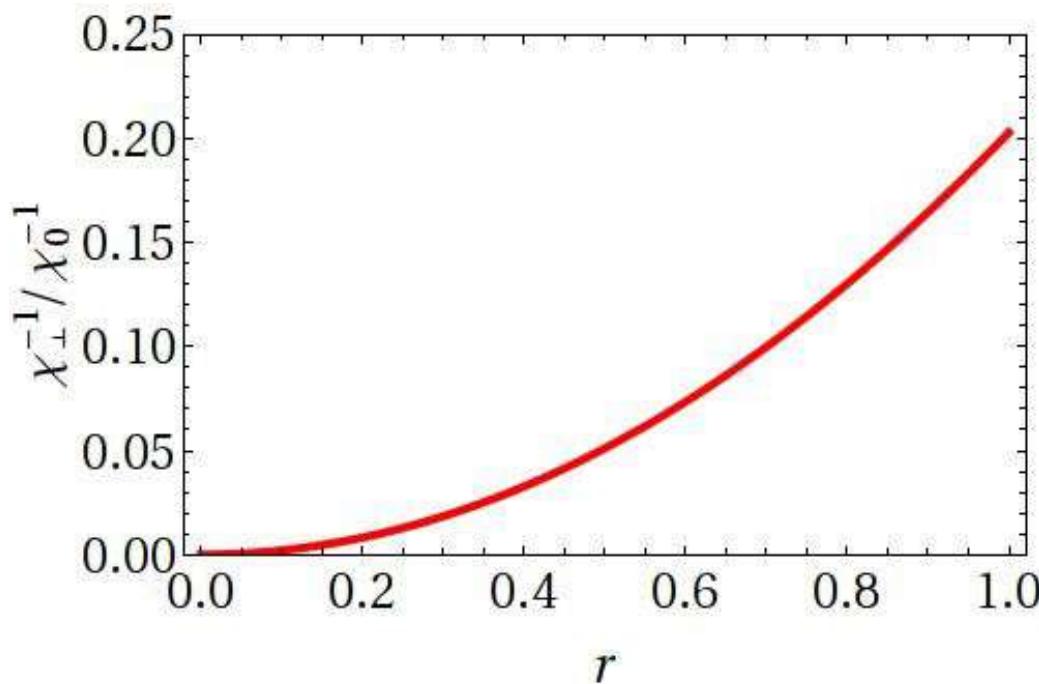
- Instability to textured phase

$$g(v_{\uparrow}v_{\downarrow})^{1/2} = 1 + \frac{q^2}{24 p_{F\uparrow}^2} + \frac{q^2}{24 p_{F\downarrow}^2}$$

Orientation of magnetization

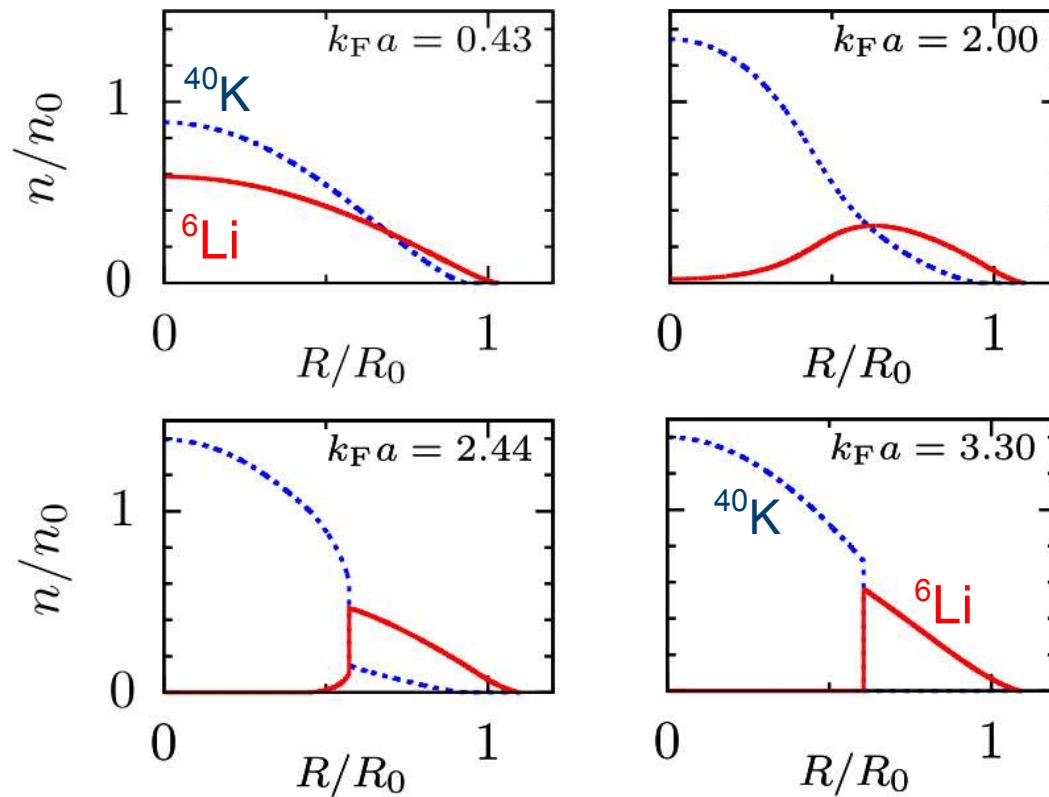
- Instability to magnetization in x-y plane

$$\chi_{\perp}^{-1} > \chi_0^{-1} \left(\frac{36r^2}{175} - \frac{8|r^3|}{2625} \right) > 0 \quad r = \frac{m_1 - m_2}{m_1 + m_2} \quad 0 \leq |r| \leq 1$$

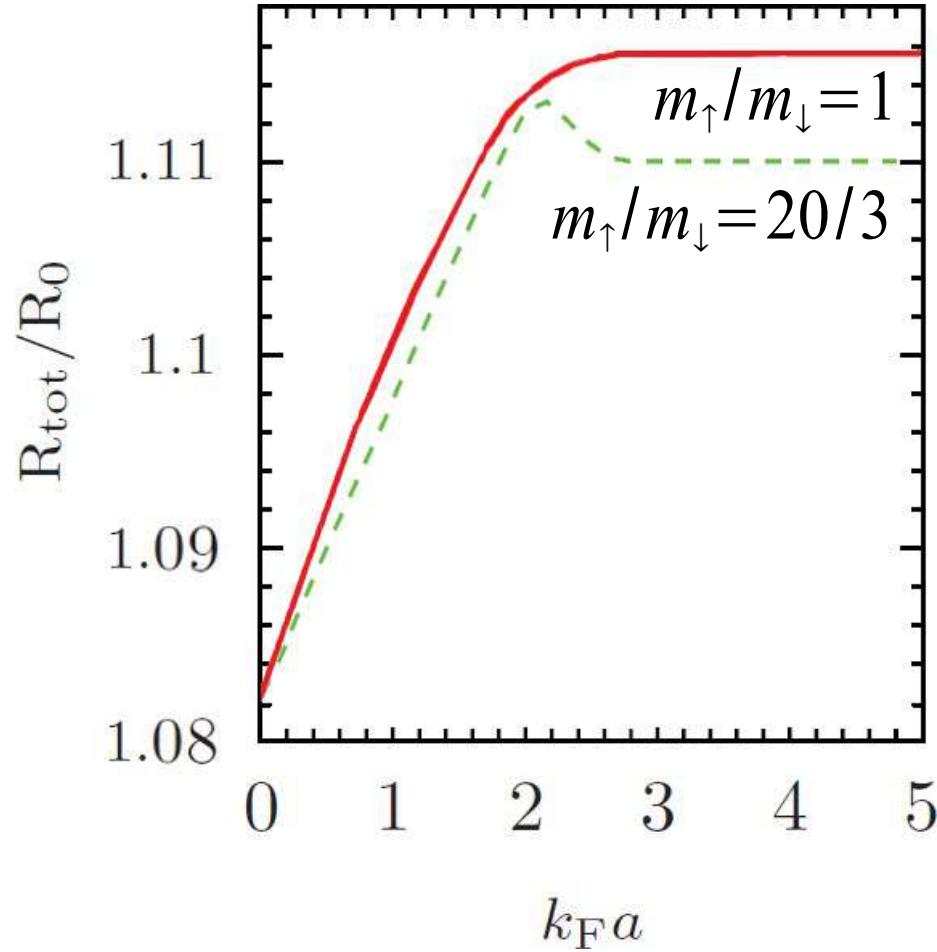


Trapped behavior

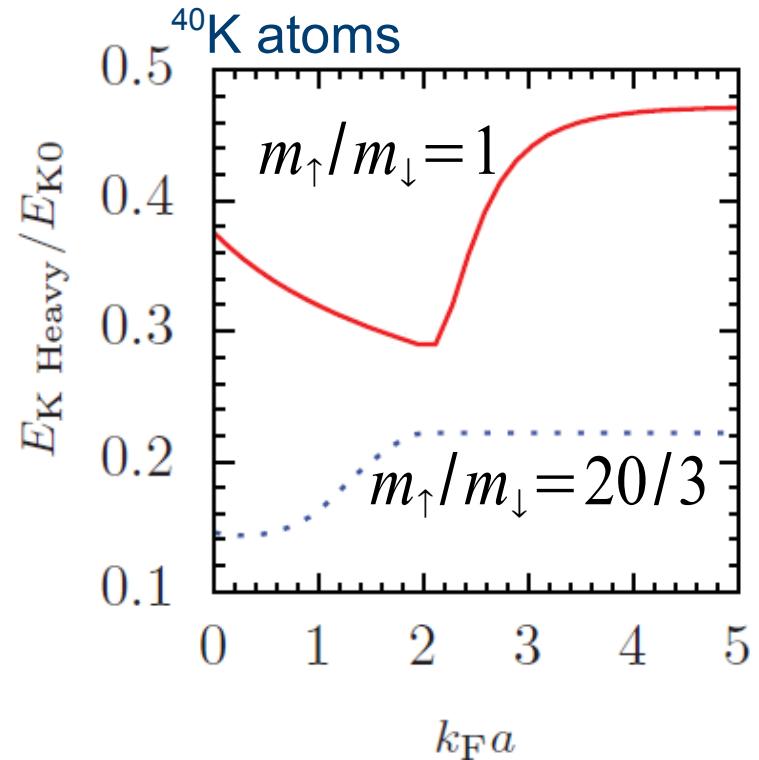
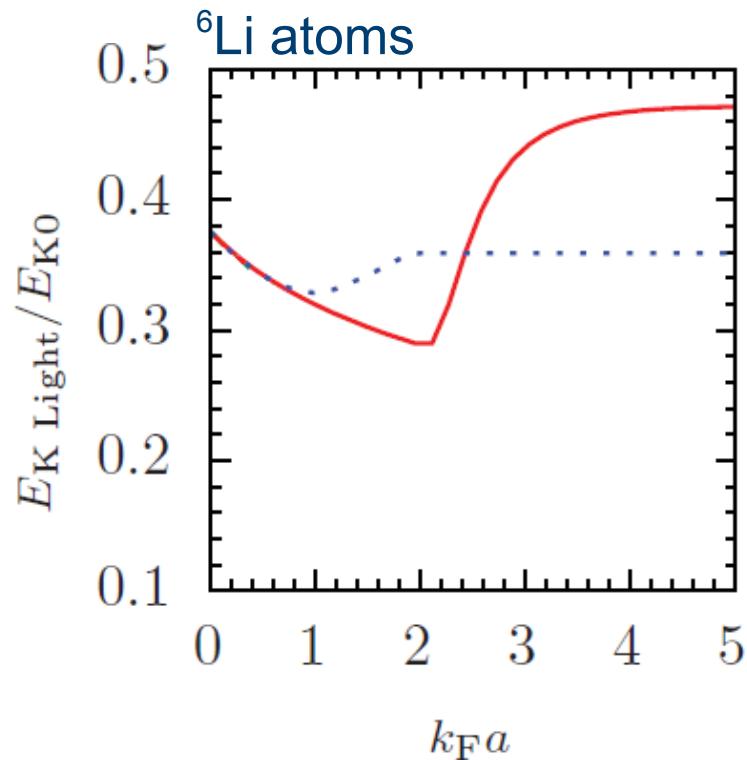
- At zero interaction strength atoms spread all over trap, at high interaction strength light atoms forced to outside



Cloud size maximum

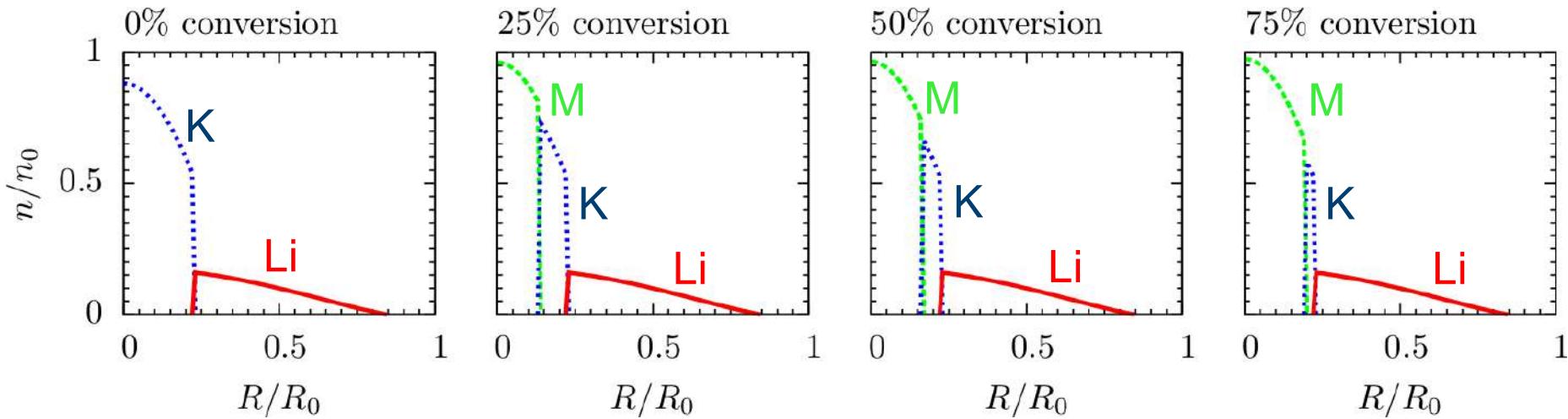


Kinetic energy plots

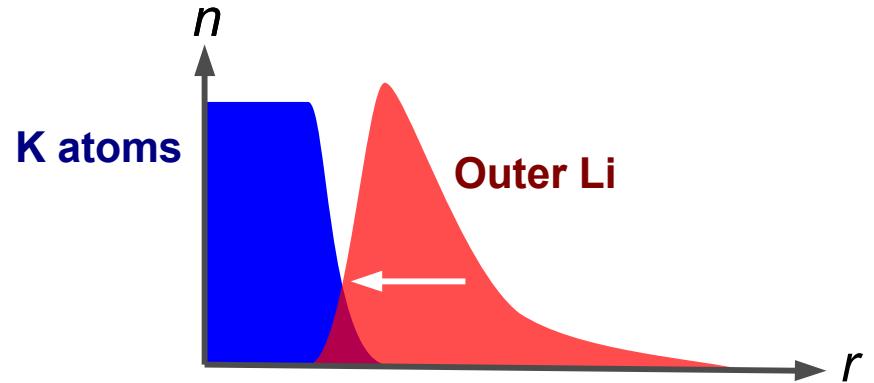


Trapped behavior

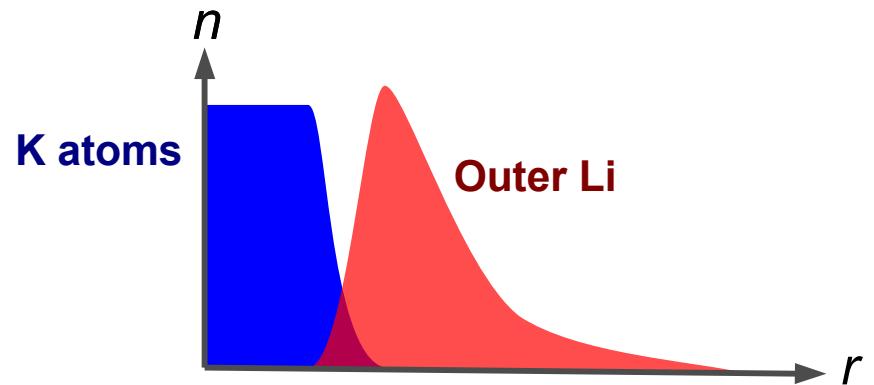
- Heavier molecules reside at trap center



Are losses responsible for phase separation?



Is Li-K repulsion responsible for phase separation?



$$P_K = n_K T_K \quad P_{Li} = \frac{2}{5} n_{Li} T_{F,Li}$$

- Temperature is $T_K \approx 0.3 T_{F, Li}$
- Density of atoms is $n_K \approx 0.5 n_{Li}$.

$$\frac{P_K}{P_{Li}} = \frac{5}{2} \frac{n_K}{n_{Li}} \frac{T_K}{T_{F,Li}} \approx 0.4$$

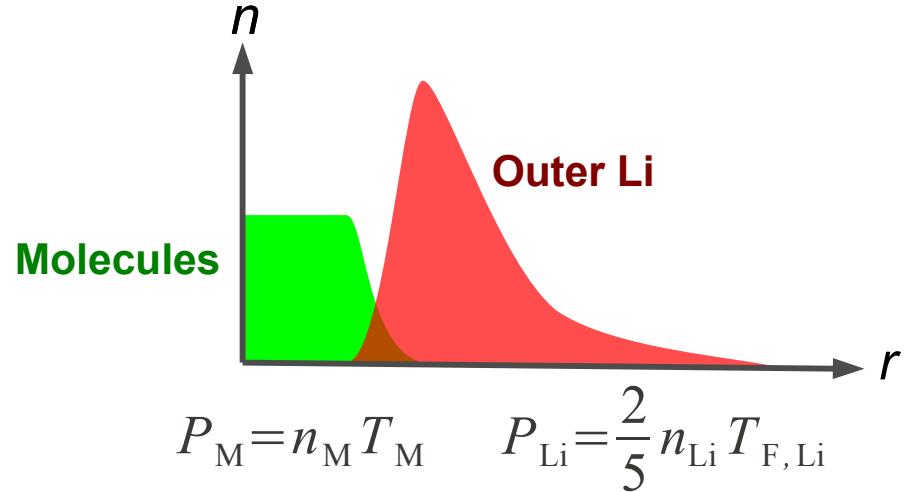
Are the molecules responsible for phase separation?

- From the scattering lengths
[Levinsen arXiv:1101.5979]

$$g_{\text{Li}-\text{M}} \approx 0.98 g_{\text{Li}-\text{K}}$$

$$g_{\text{K}-\text{M}} \approx 0.49 g_{\text{Li}-\text{K}}$$

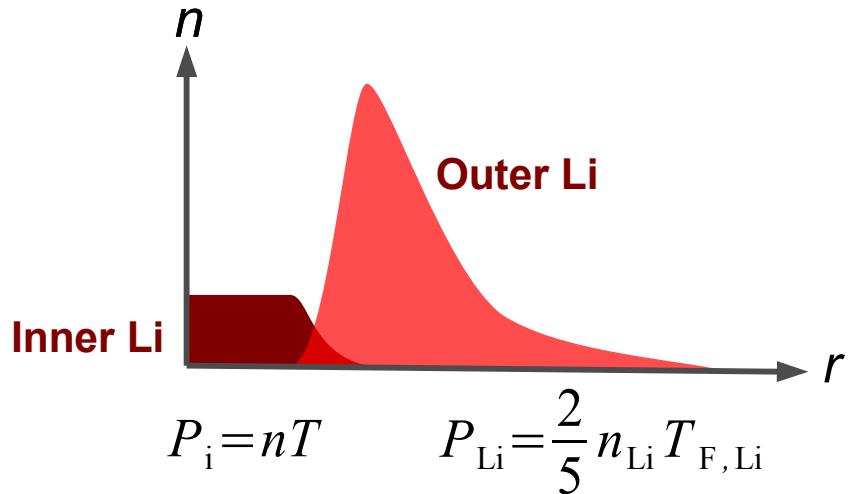
$$g_{\text{M}-\text{M}} \approx 0.057 g_{\text{Li}-\text{K}}$$



- The Li-molecule T -matrix is similar to the Li-K T -matrix so the molecules also drive phase separation

$$\frac{P_M}{P_{\text{Li}}} \approx 0.4$$

Is heating responsible for phase separation?

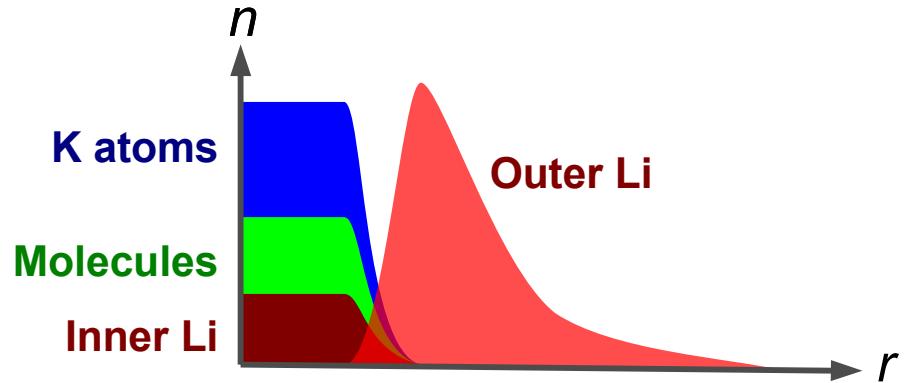


- Inner classical gas, in thermal equilibrium with central K atoms with temperature $T_K \approx 0.3 T_{F,Li}$ demands

$$n \approx 1.3 n_{Li}$$

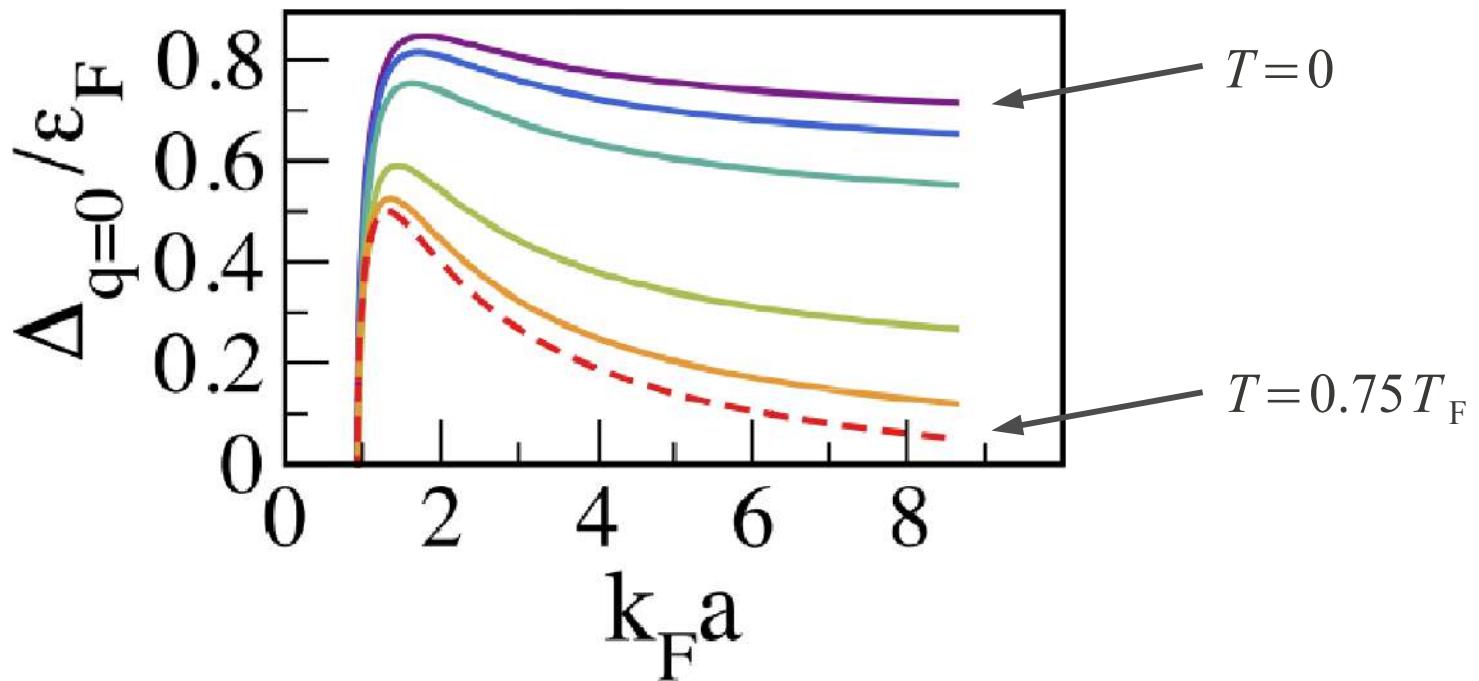
- Reactivation of losses also precludes heating mechanism

What drives phase separation?



- Repulsion from the inner K atom combined with molecules is sufficient to support phase separation
- Continual losses and heating appear negligible

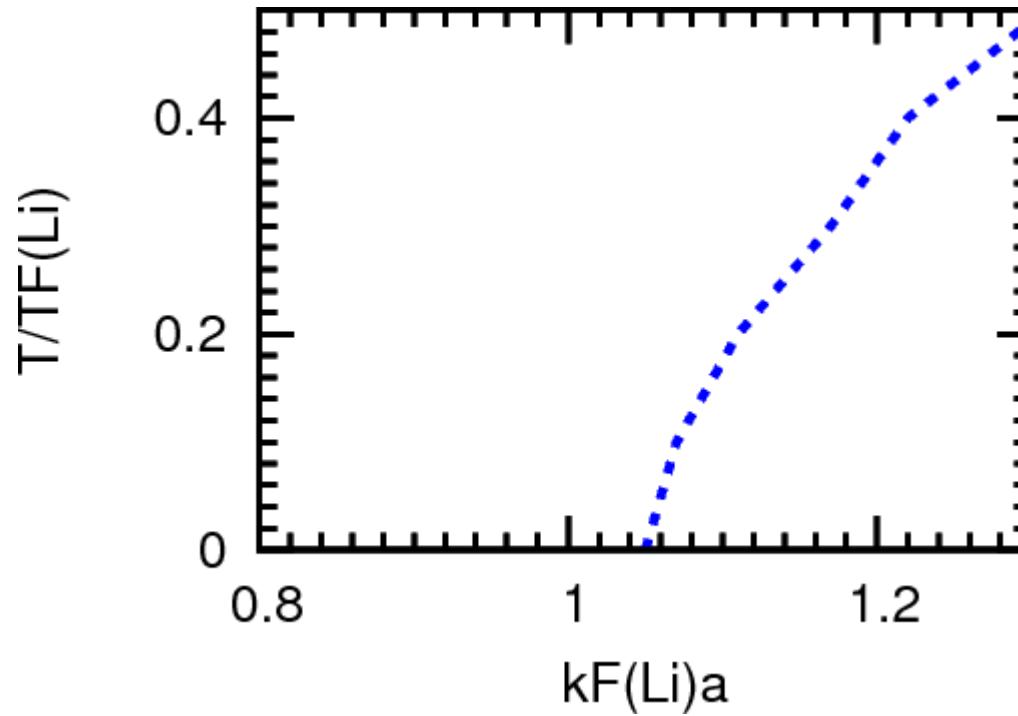
Pairing rate reduces with temperature



Pekker et al, PRL 106, 050402 (2011)

Magnetism at finite temperature

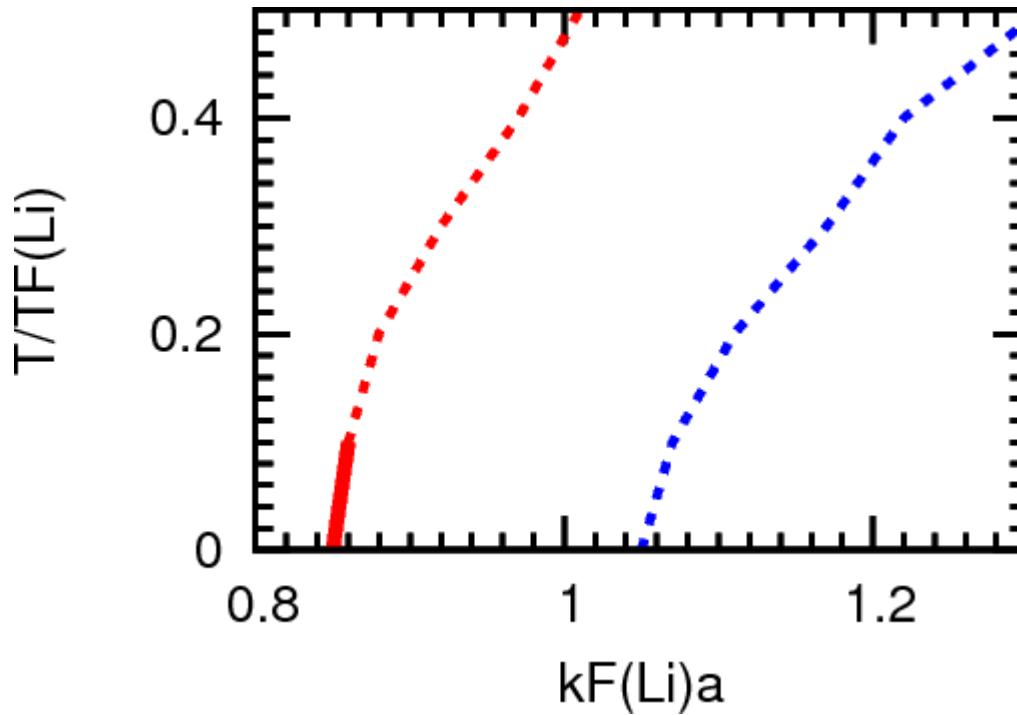
$$F = \frac{1}{V} \sum_{\vec{k}, \sigma} \epsilon_{\vec{k}, \sigma} n(\epsilon_{\vec{k}, \sigma}) + \frac{2k_F a}{\pi v V^2} N_\uparrow N_\downarrow$$



GJC & Simons, PRA 79, 053606 (2009)

Magnetism at finite temperature

$$F = \frac{1}{V} \sum_{\vec{k}, \sigma} \epsilon_{\vec{k}, \sigma} n(\epsilon_{\vec{k}, \sigma}) + \frac{2k_F a}{\pi v V^2} N_\uparrow N_\downarrow - \frac{2}{V^3} \left(\frac{2k_F a}{\pi v} \right)^2 \frac{\sum_{\vec{k}_1, \vec{k}_2, \vec{k}_3, \vec{k}_4} n(\epsilon_{\vec{k}_1, \uparrow}) n(\epsilon_{\vec{k}_2, \downarrow}) [n(\epsilon_{\vec{k}_3, \uparrow}) + n(\epsilon_{\vec{k}_4, \downarrow})]}{\epsilon_{\vec{k}_1, \uparrow} + \epsilon_{\vec{k}_2, \downarrow} - \epsilon_{\vec{k}_3, \uparrow} - \epsilon_{\vec{k}_4, \downarrow}}$$



GJC & Simons, PRA 79, 053606 (2009)

Temperature reduced scattering cross-section

- Thermally averaged scattering cross-section

Bruun & Smith, PRA **72**, 043605 (2005)

- $$\langle \sigma \rangle = \frac{\int d^3 p_1 d^3 p_2 f(p_1^2/2m_1) f(p_2^2/2m_2) \sigma(\vec{p}_r)}{\int d^3 p_1 d^3 p_2 f(p_1^2/2m_1) f(p_2^2/2m_2)}$$

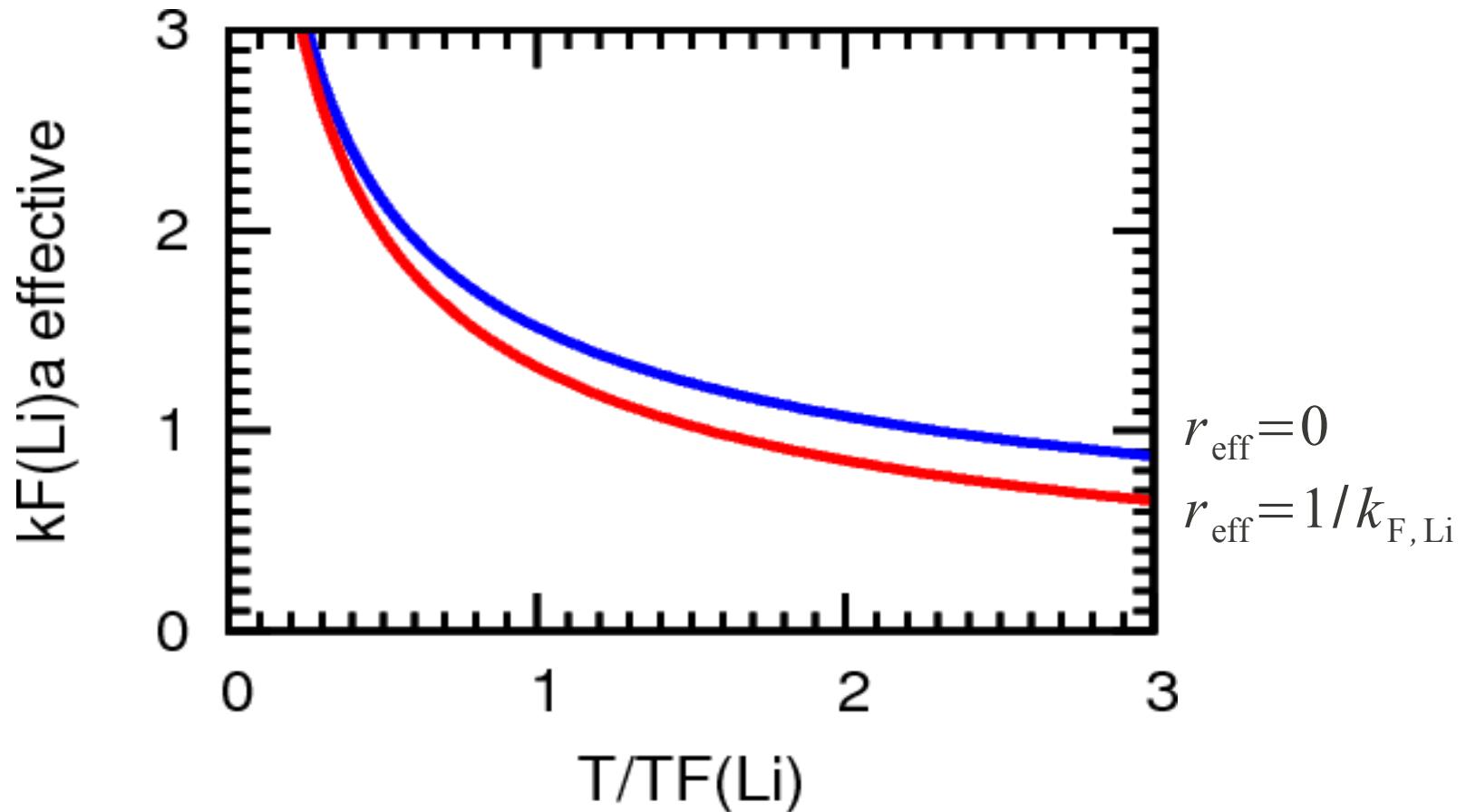
with

$$\sigma(\vec{p}_r) = \frac{4\pi a^2}{(1 - r_{\text{eff}} a p_r^2/2)^2 + a^2 p_r^2} \quad \vec{p}_r = \left(\frac{\vec{p}_1 m_2}{m_1 + m_2} - \frac{\vec{p}_2 m_1}{m_1 + m_2} \right)$$

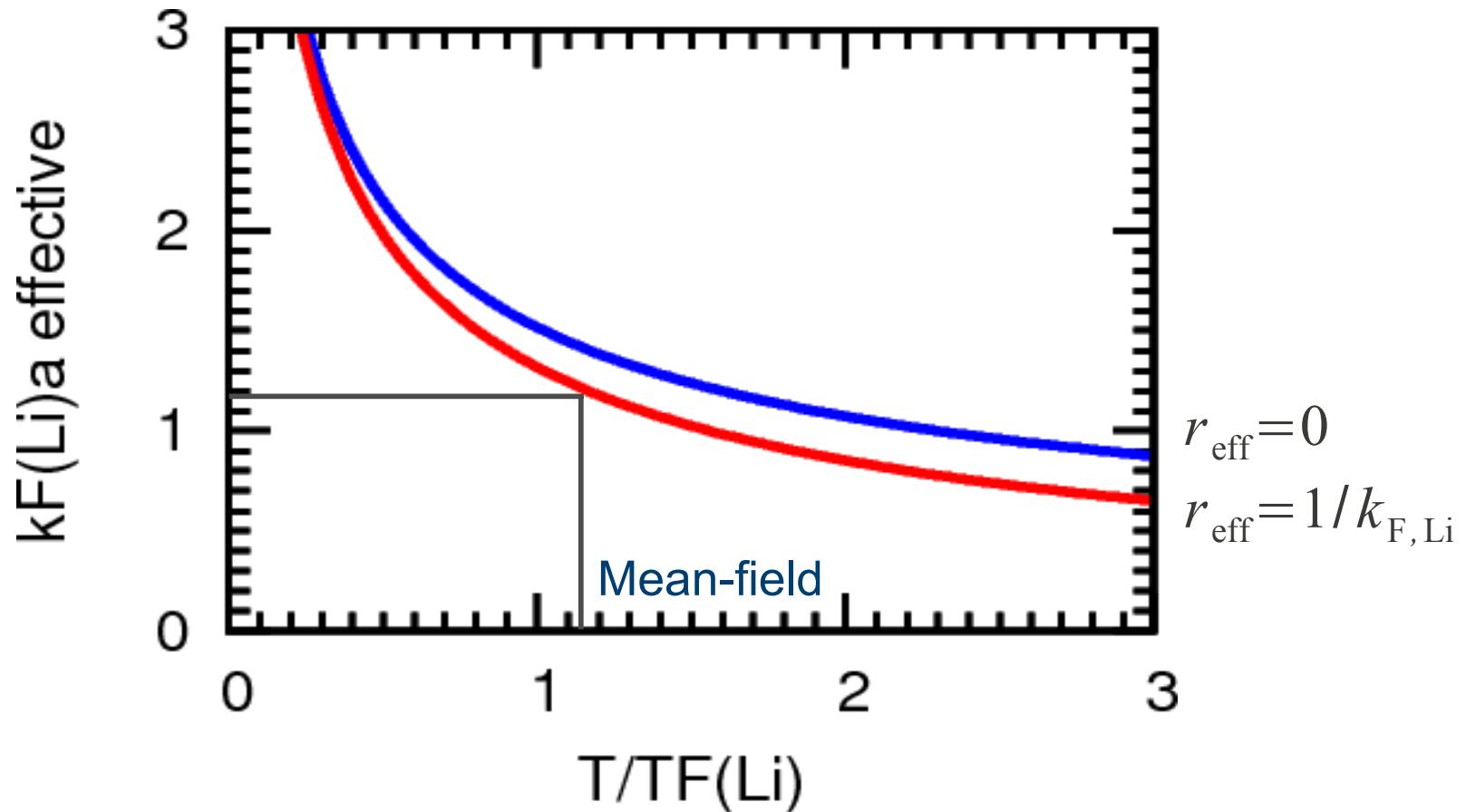
- In the high temperature unitarity limit

$$\langle \sigma \rangle = \frac{4\pi}{T} \frac{m_1 + m_2}{m_1 m_2} \frac{1}{\sqrt{1 + \frac{T r_{\text{eff}}^2}{2} \frac{m_1 m_2}{m_1 + m_2}}}$$

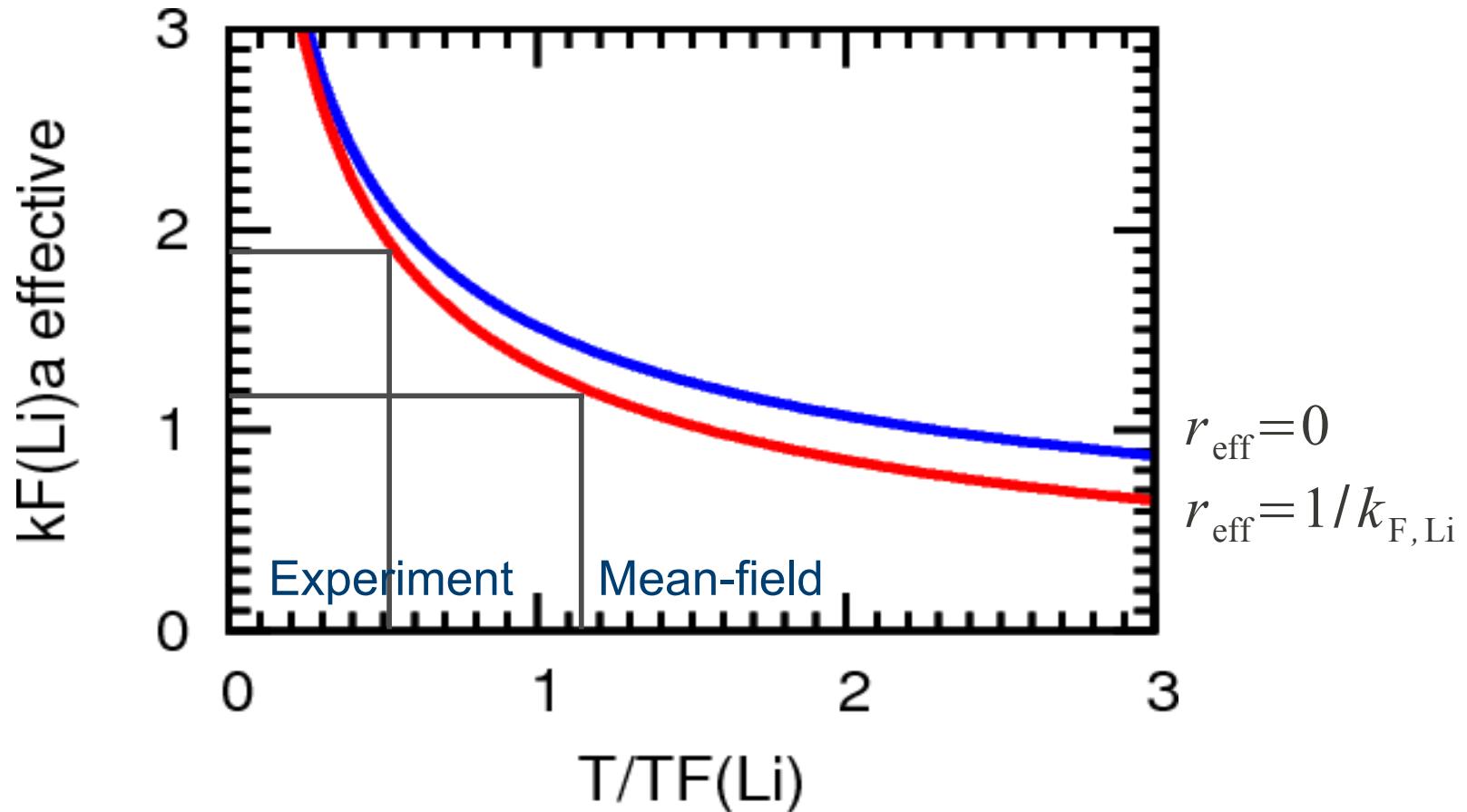
Temperature reduced scattering cross-section



Temperature reduced scattering cross-section



Temperature reduced scattering cross-section



Conclusions

- The behavior of repulsively interacting gases of Fermions remains an important unanswered question
- Mass imbalance suppresses competing many-body instabilities and gives explicit domain formation
- Feshbach molecules and K atoms together drive phase separation
- High temperature further reduces pairing losses