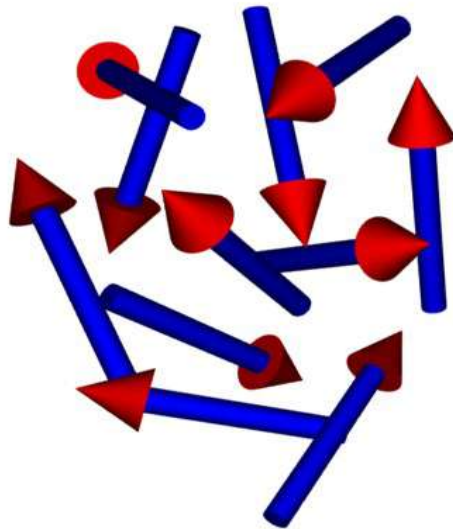
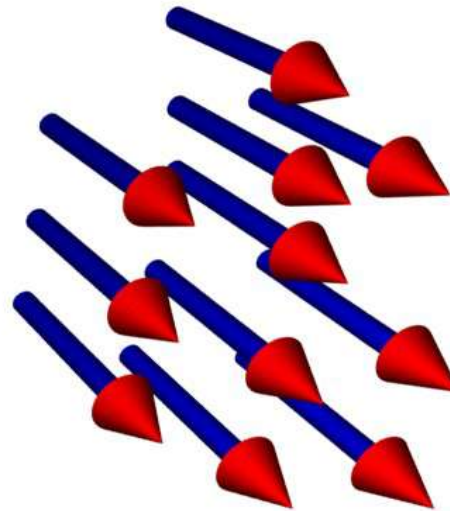


A repulsive atomic gas on the border of itinerant ferromagnetism

Weak interactions



Strong interactions



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1. Weizmann Institute, 2. Ben Gurion University, 3. University of Cambridge

G.J. Conduit & B.D. Simons, Phys. Rev. A **79**, 053606 (2009)

G.J. Conduit, A.G. Green & B.D. Simons, Phys. Rev. Lett. **103**, 207201 (2009)

G.J. Conduit & B.D. Simons, Phys. Rev. Lett. **103**, 200403 (2009)

G.J Conduit & E. Altman, arXiv: 0911.2839

Itinerant ferromagnetism in cold atom gases

- Use two ${}^6\text{Li}$ states to represent pseudo up and down-spin electrons

- Effective Hamiltonian

$$H = \sum_{\mathbf{k}\sigma} \varepsilon_{\mathbf{k}} n_{\sigma}(\varepsilon_{\mathbf{k}}) + g N_{\uparrow} N_{\downarrow}$$

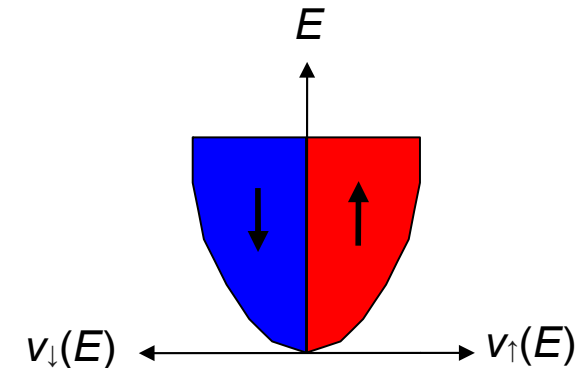
- A ΔE shift in the Fermi surface causes:

(1) Kinetic energy increase of $\frac{1}{2}v\Delta E^2$

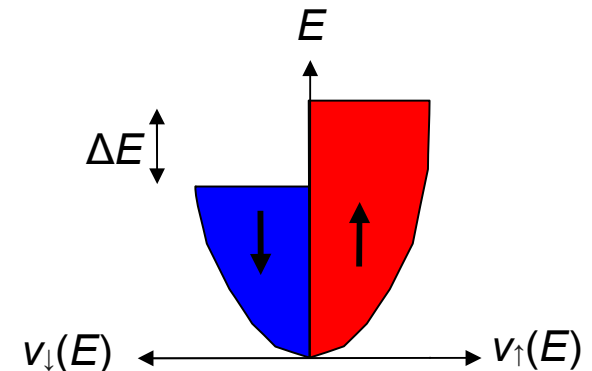
(2) Reduction of repulsion of $-\frac{1}{2}gv^2\Delta E^2$

- Total energy shift is $\frac{1}{2}v\Delta E^2(1-gv)$ so a ferromagnetic transition occurs if $gv > 1$

Not magnetised



Partially magnetised

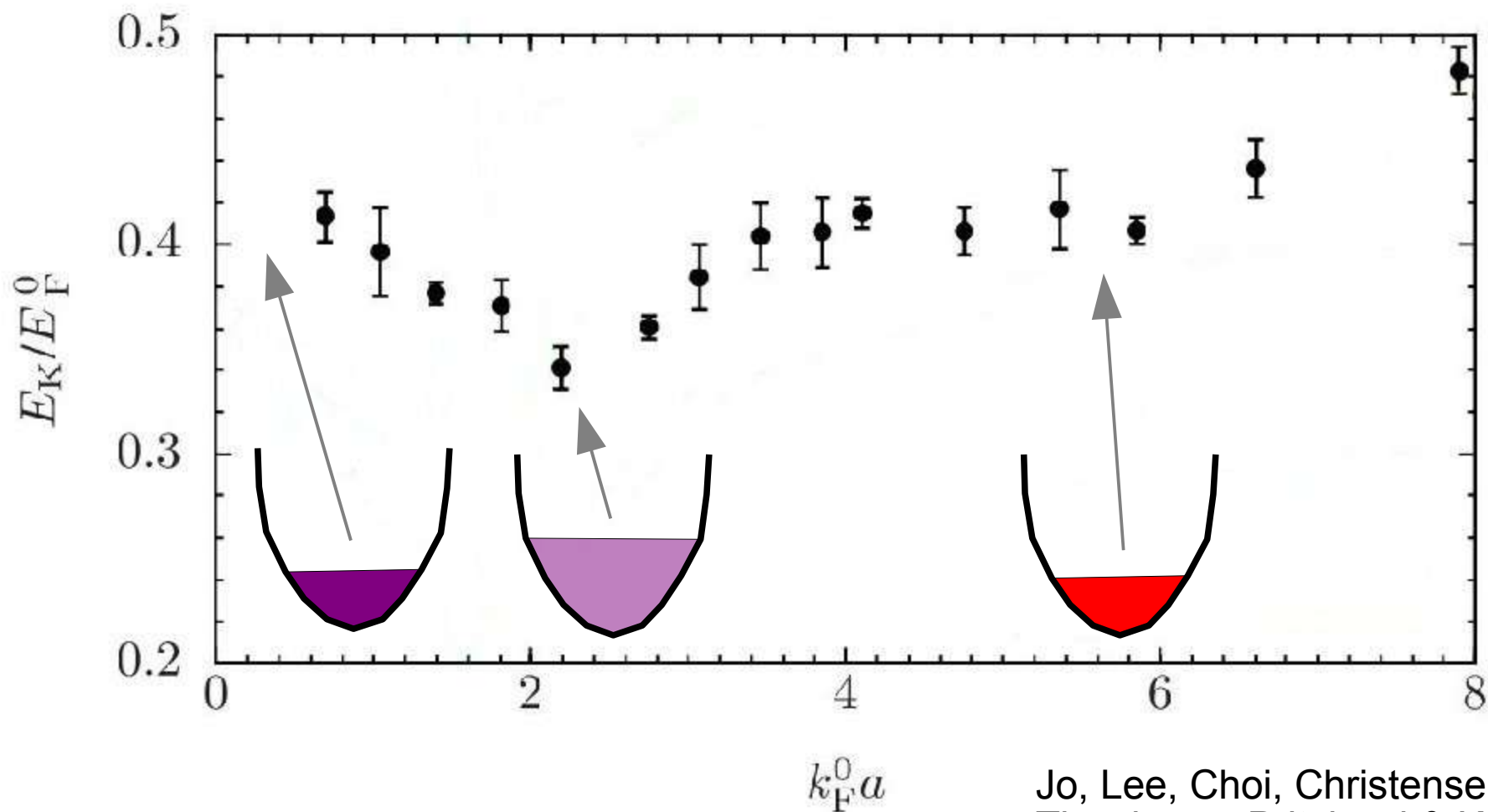


G.J. Conduit & B.D. Simons, Phys. Rev. A **79**, 053606 (2009)

Jo, Lee, Choi, Christensen, Kim, Thywissen, Pritchard & Ketterle, Science **325**, 1521 (2009)

Experimental evidence for ferromagnetism

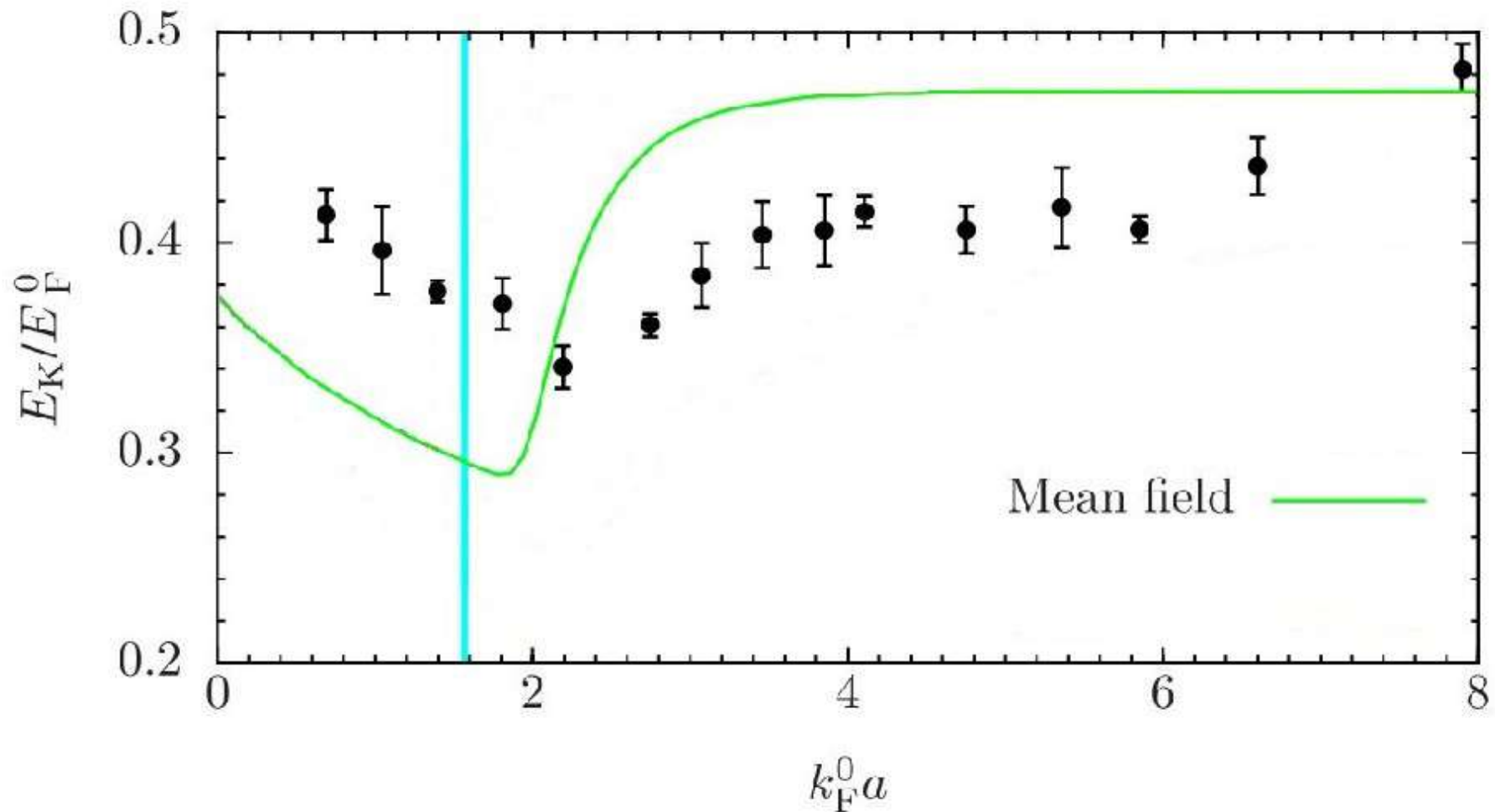
- Experimental points display same qualitative behavior but transition at $k_F a = 2.2$



Jo, Lee, Choi, Christensen, Kim, Thywissen, Pritchard & Ketterle, Science **325**, 1521 (2009)

Mean-field theory for ferromagnetism

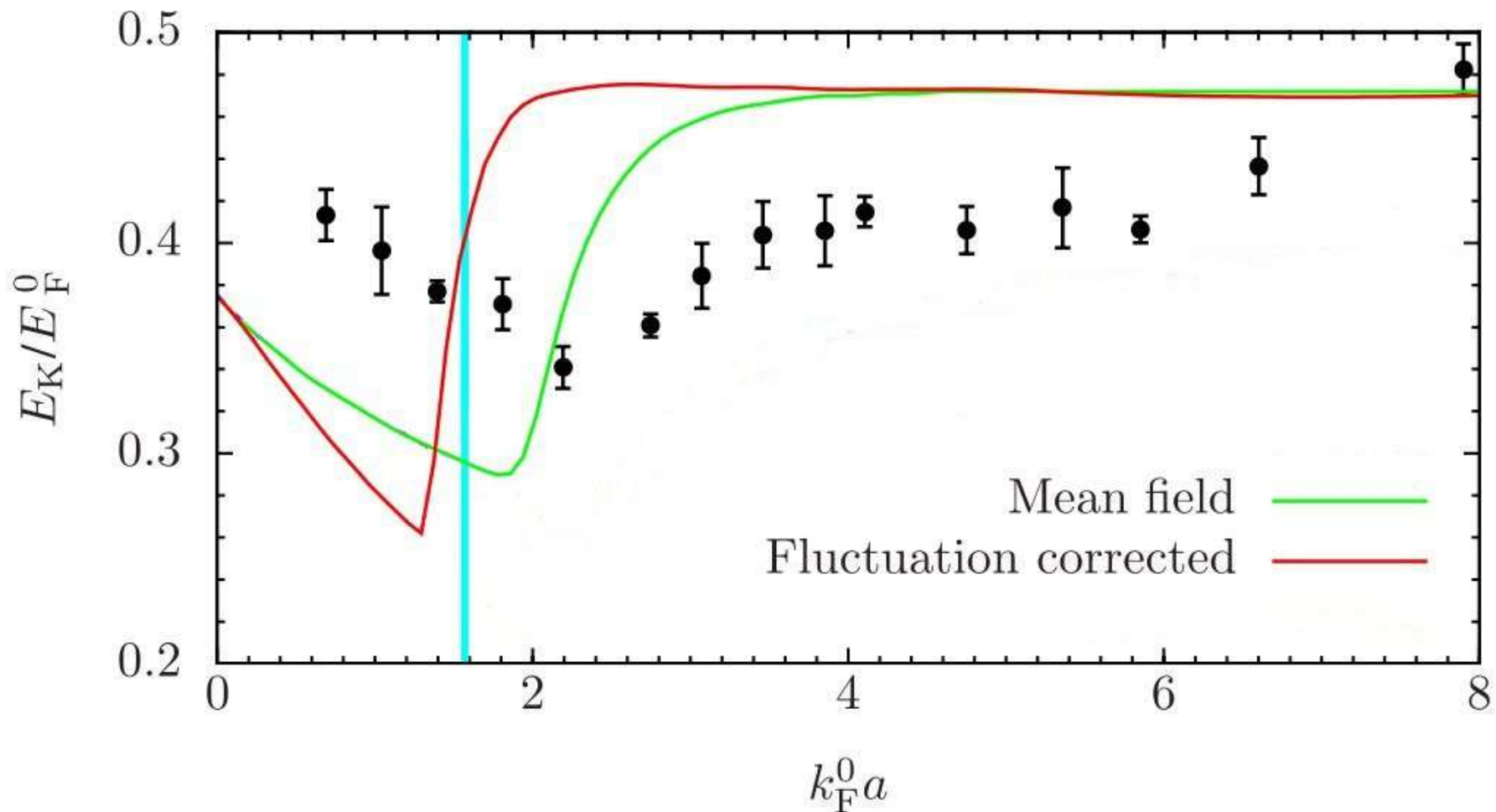
- The Stoner model predicts¹ a minimum in the kinetic energy at $k_F a = 1.8$



¹LeBlanc *et al.*, PRA **80**, 013607 (2009) & Conduit & Simons, PRL **103**, 200403 (2009)

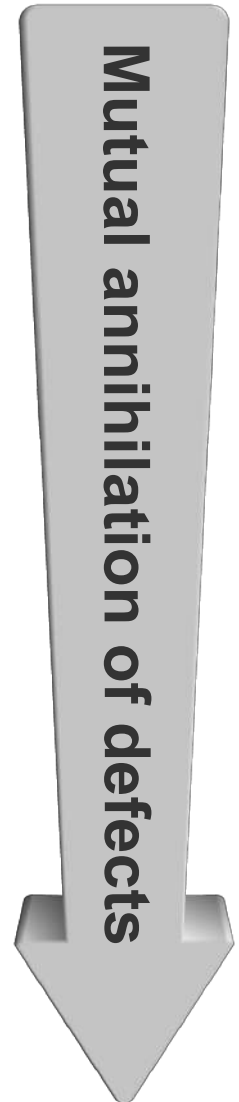
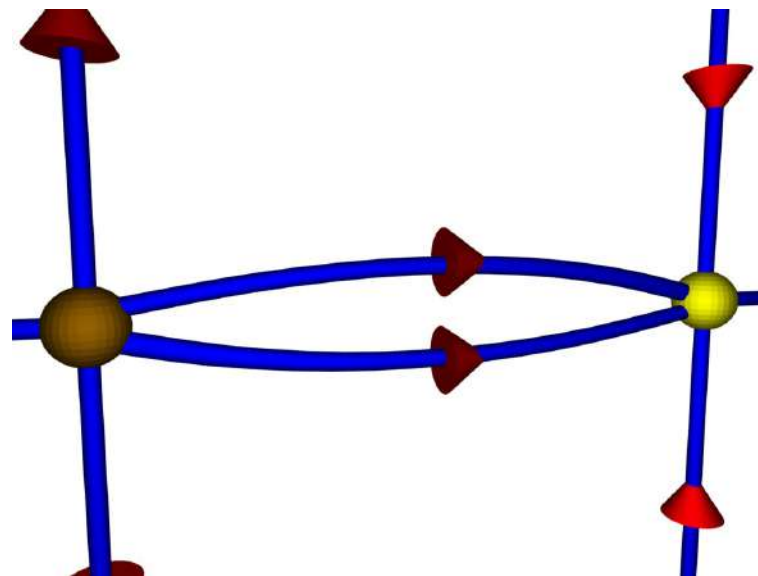
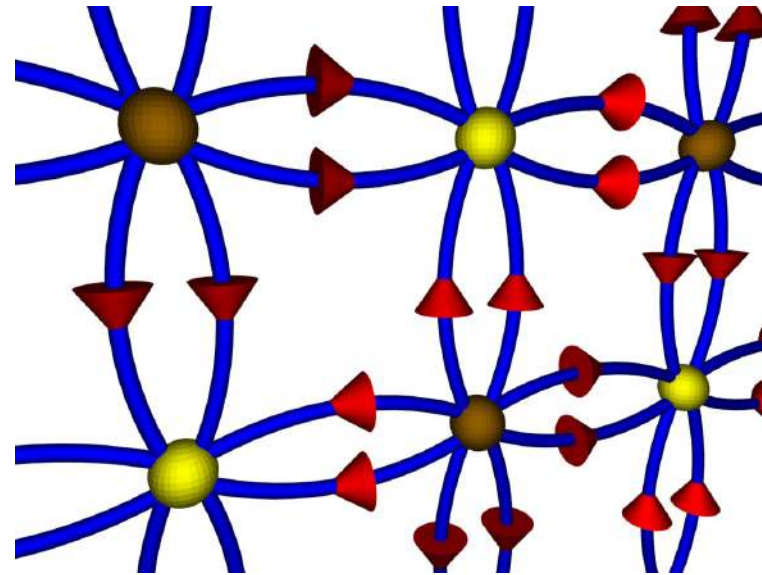
Fluctuation corrections

- Extend theory through fluctuation corrections



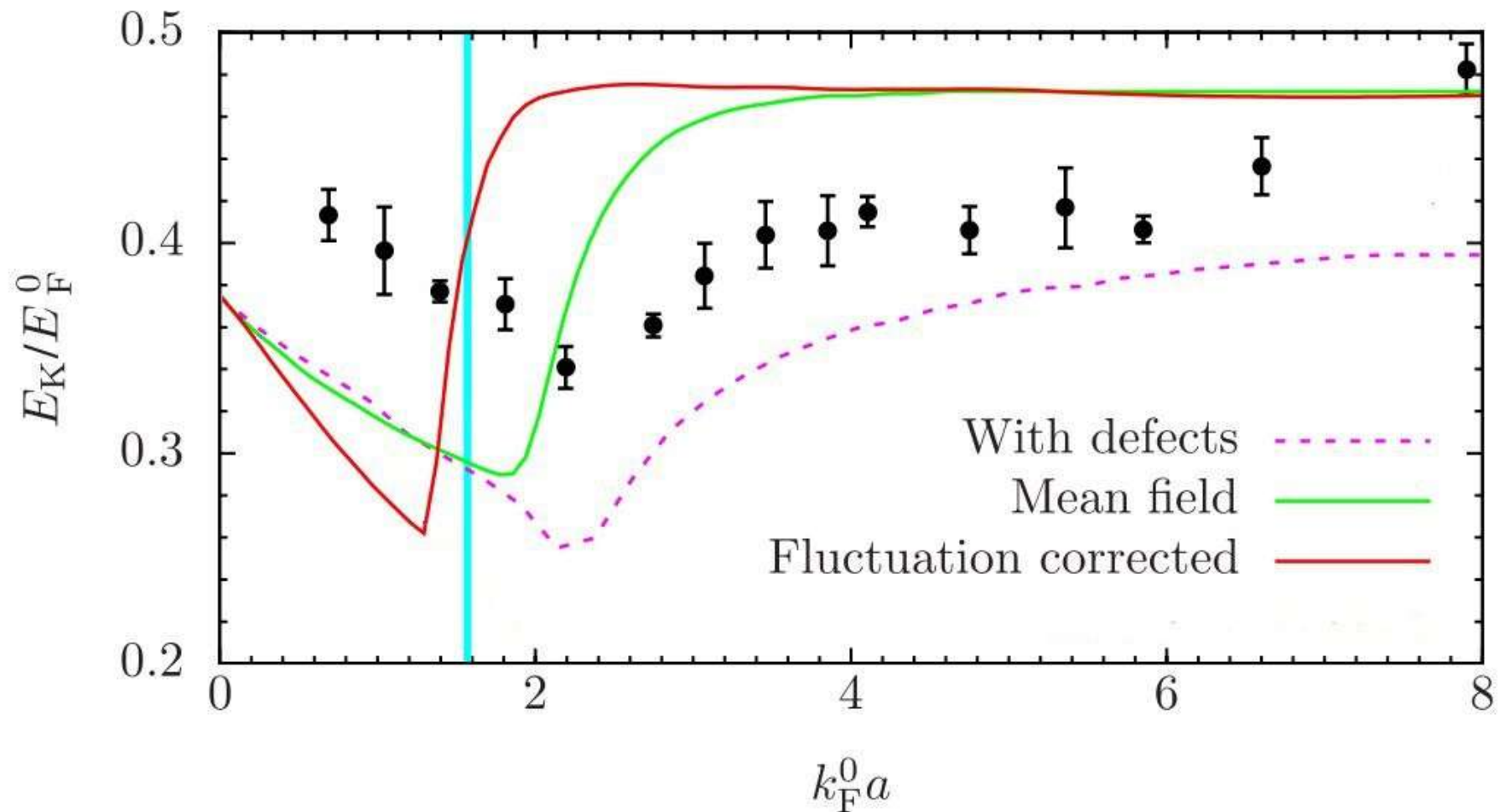
Condensation of topological defects

- Defects freeze out from disordered state
- Defect annihilation hinders the formation of the ferromagnetic phase thus raising the required interaction strength
- Defect radius $L \sim t^{1/2}$ [Bray, Adv. Phys. **43**, 357 (1994)]



Condensation of topological defects

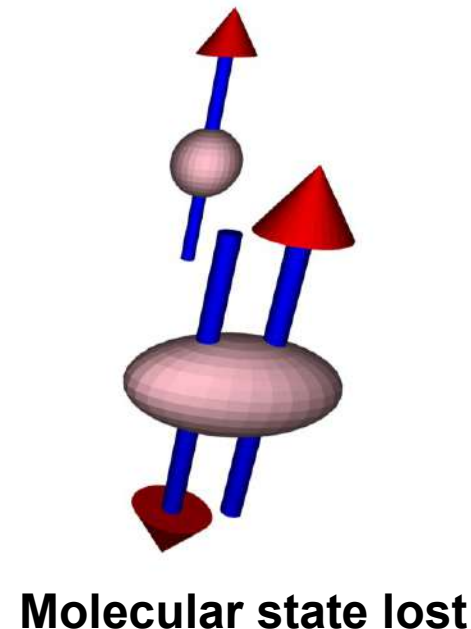
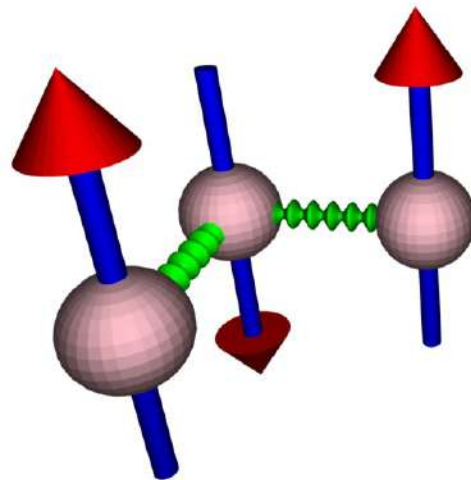
- Condensation of defects inhibits the transition



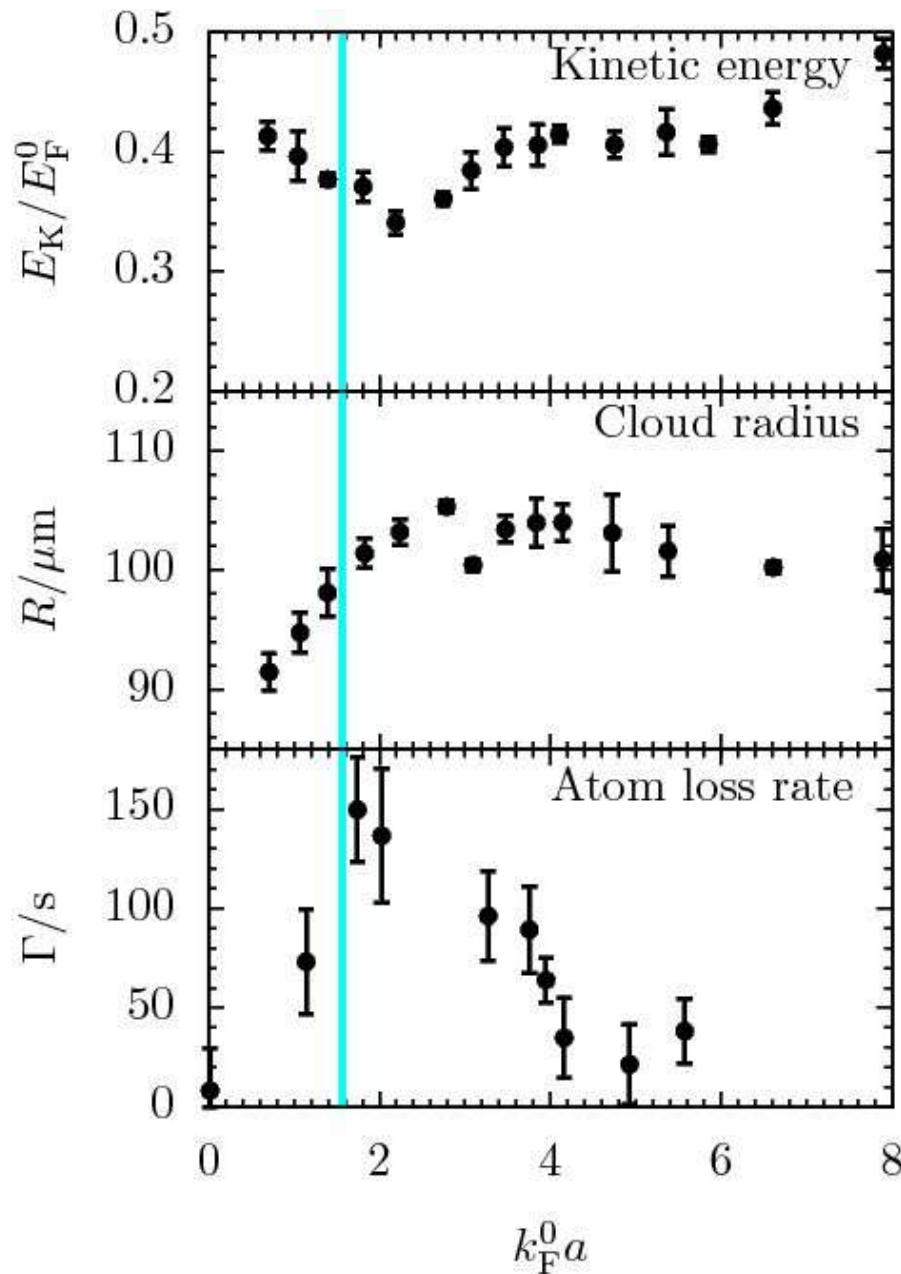
Conclusions

- Mean-field theory provides a reasonable qualitative description of the transition
- Discrepancy in the interaction strength could be accounted for by the mutual annihilation of defects inhibiting the formation of the ferromagnetic phase
- Work ongoing on the renormalization of interaction strength due to three-body atom loss [Conduit & Altman, arXiv: 0911.2839]

Three-body interaction



Key experimental signatures



Jo, Lee, Choi, Christensen, Kim, Thywissen, Pritchard & Ketterle, Science **325**, 1521 (2009)