

Few-atom approach to many-body physics

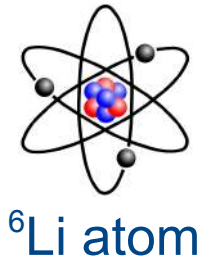
G.J. Conduit and P.O. Bugnion

POB, J. Lofthouse & GJC, Phys. Rev. Lett. **111**, 045301 (2013)

POB & GJC, Phys. Rev. A **87**, 060502(R) (2013)

POB & GJC, Phys. Rev. A **88**, 013601 (2013)

Experimental setup

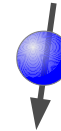


$$|F = 1/2, m_F = 1/2\rangle$$



Up spin electron

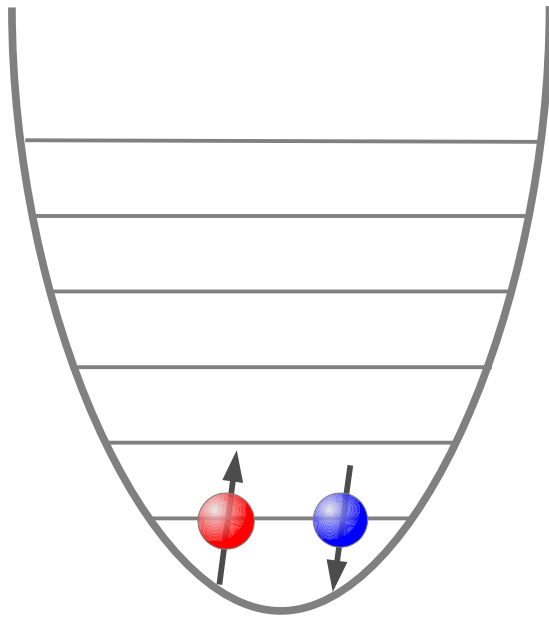
$$|F = 1/2, m_F = -1/2\rangle$$



Down spin electron

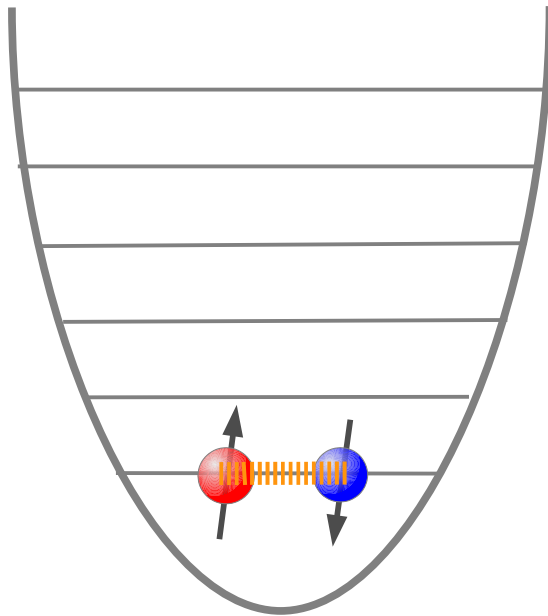
$$\hat{H} = -\frac{\nabla^2}{2} + gn_{\uparrow}(\vec{r})n_{\downarrow}(\vec{r})$$

Two distinguishable fermions

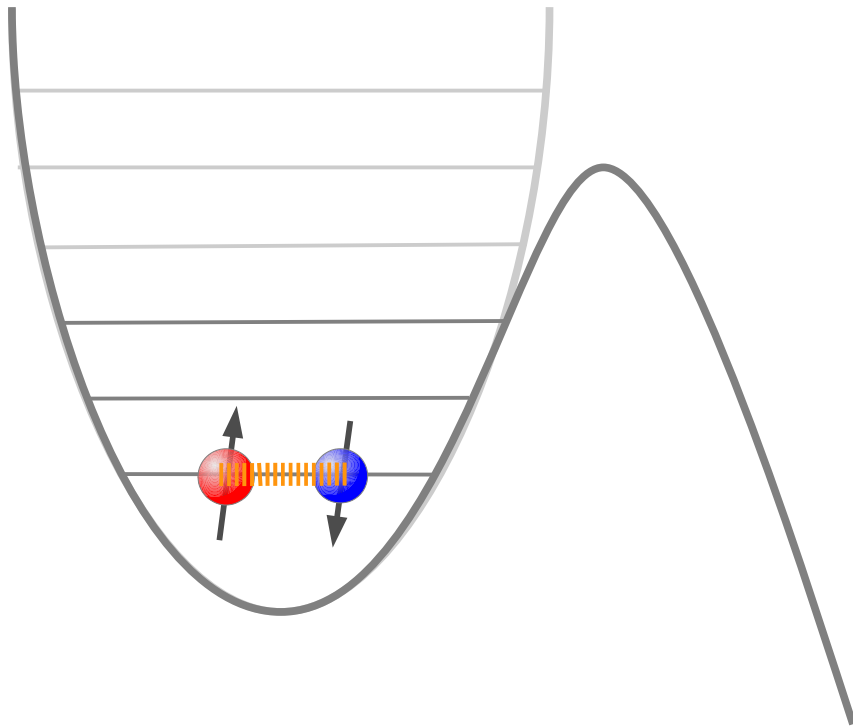


G. Zürn *et al.* PRL 108 075303 (2012)

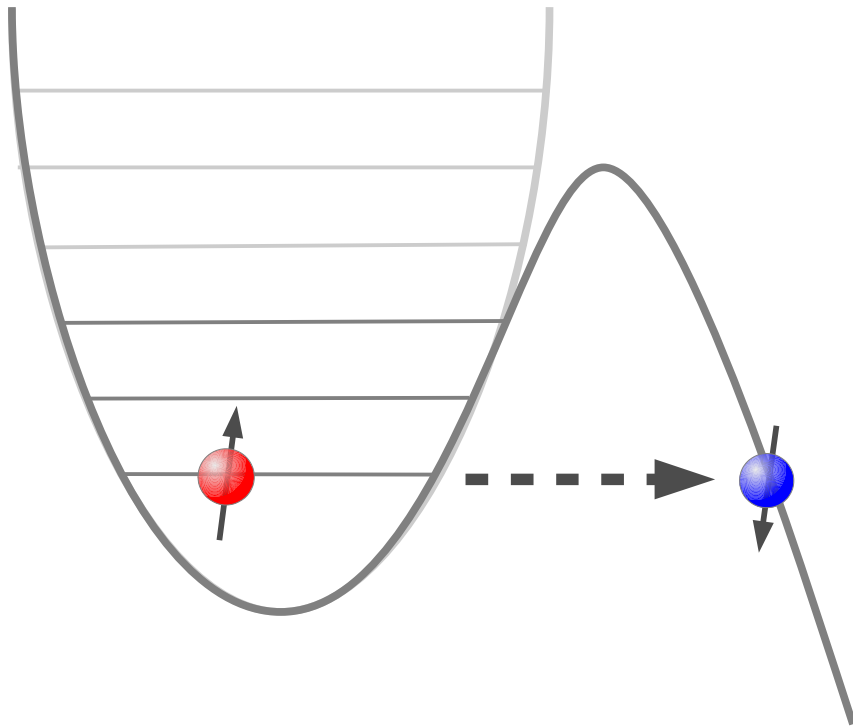
Two distinguishable fermions



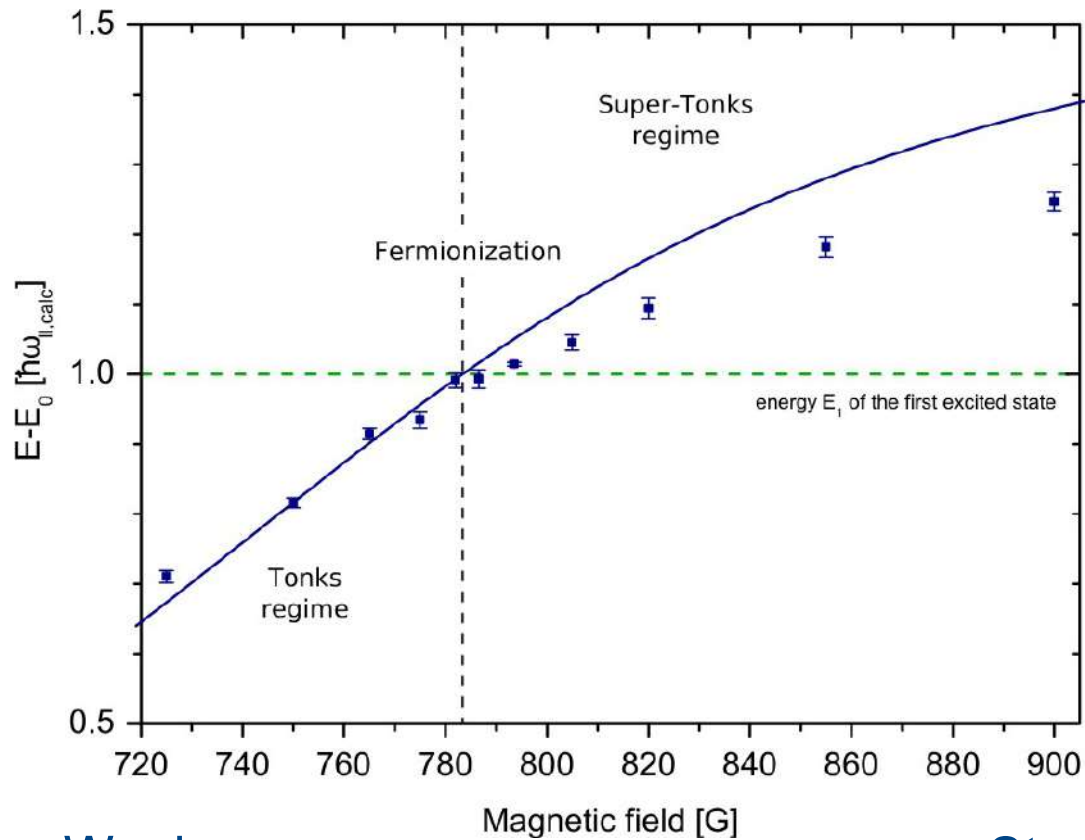
Two distinguishable fermions



Two distinguishable fermions

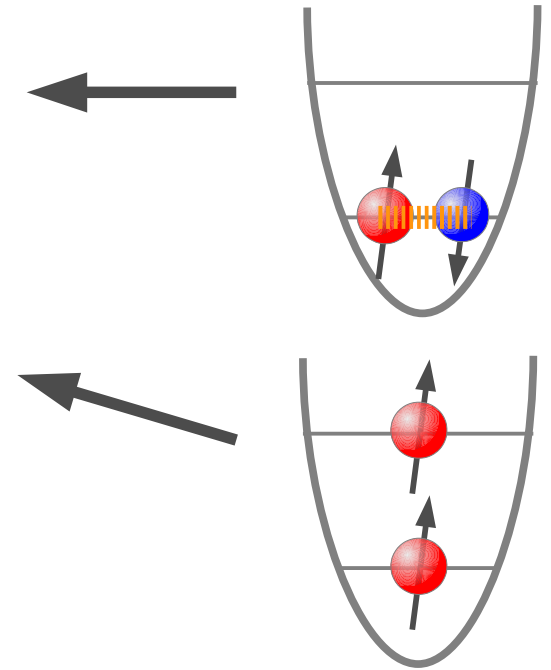


Energy of states

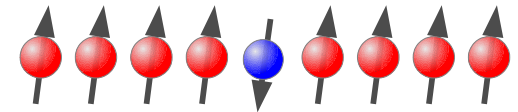
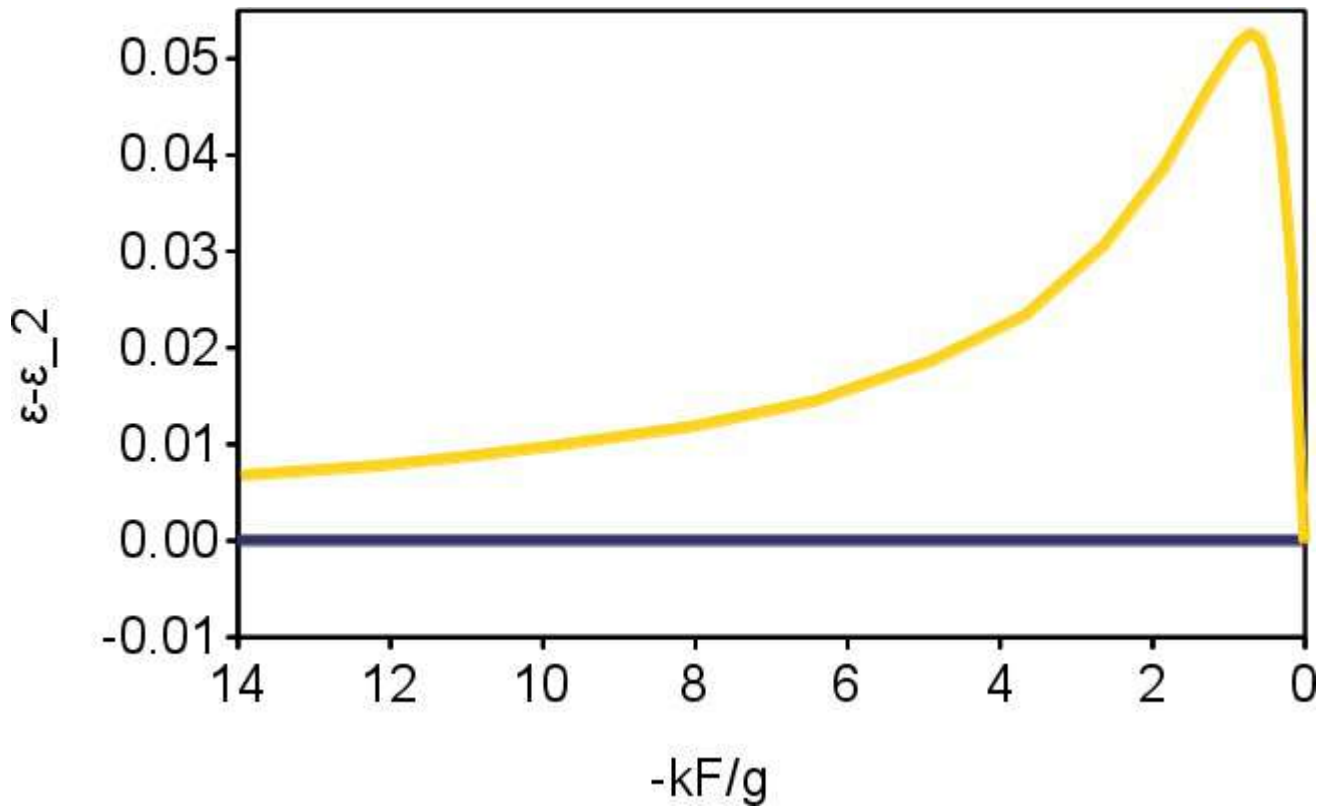


Weak
repulsion

Strong
repulsion

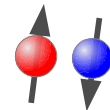


Polaron state



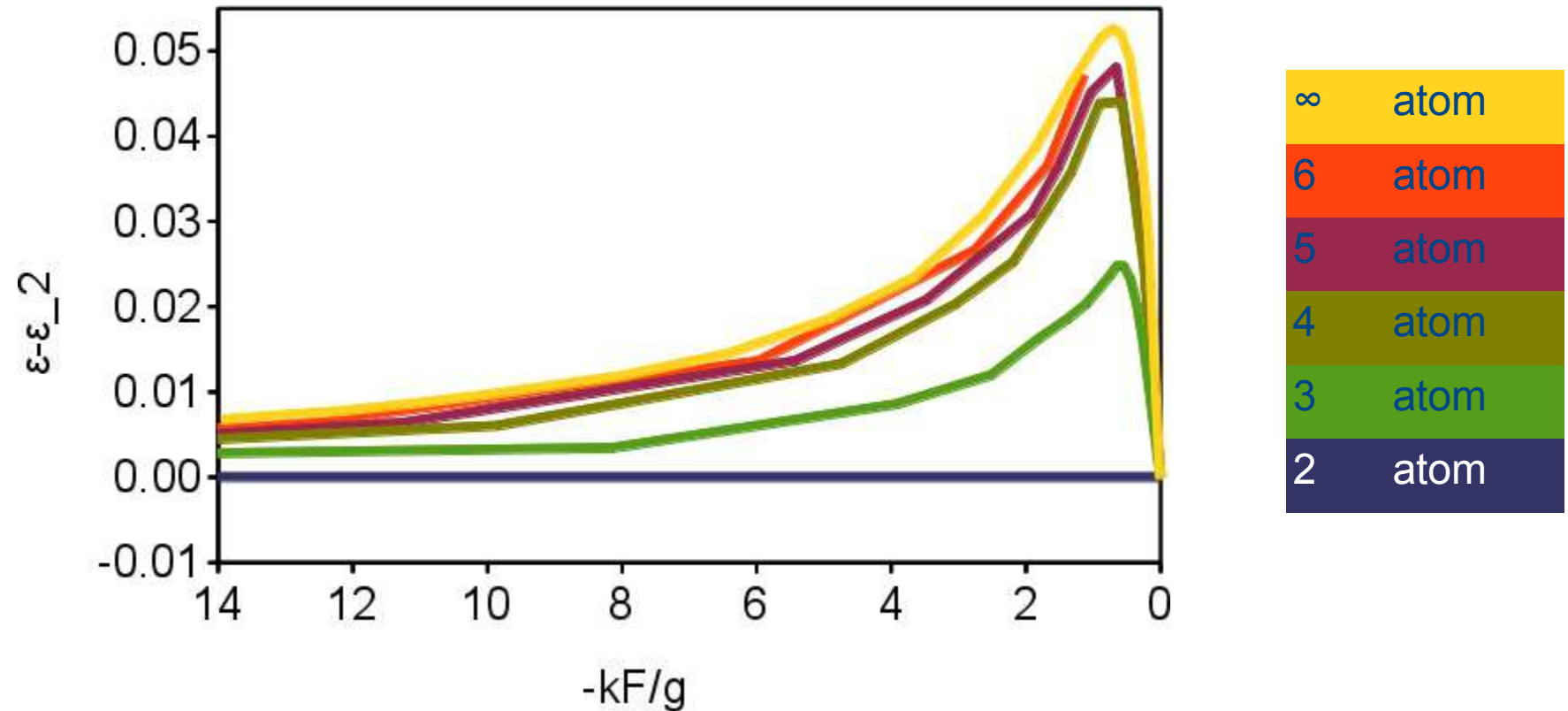
∞ atom

2 atom



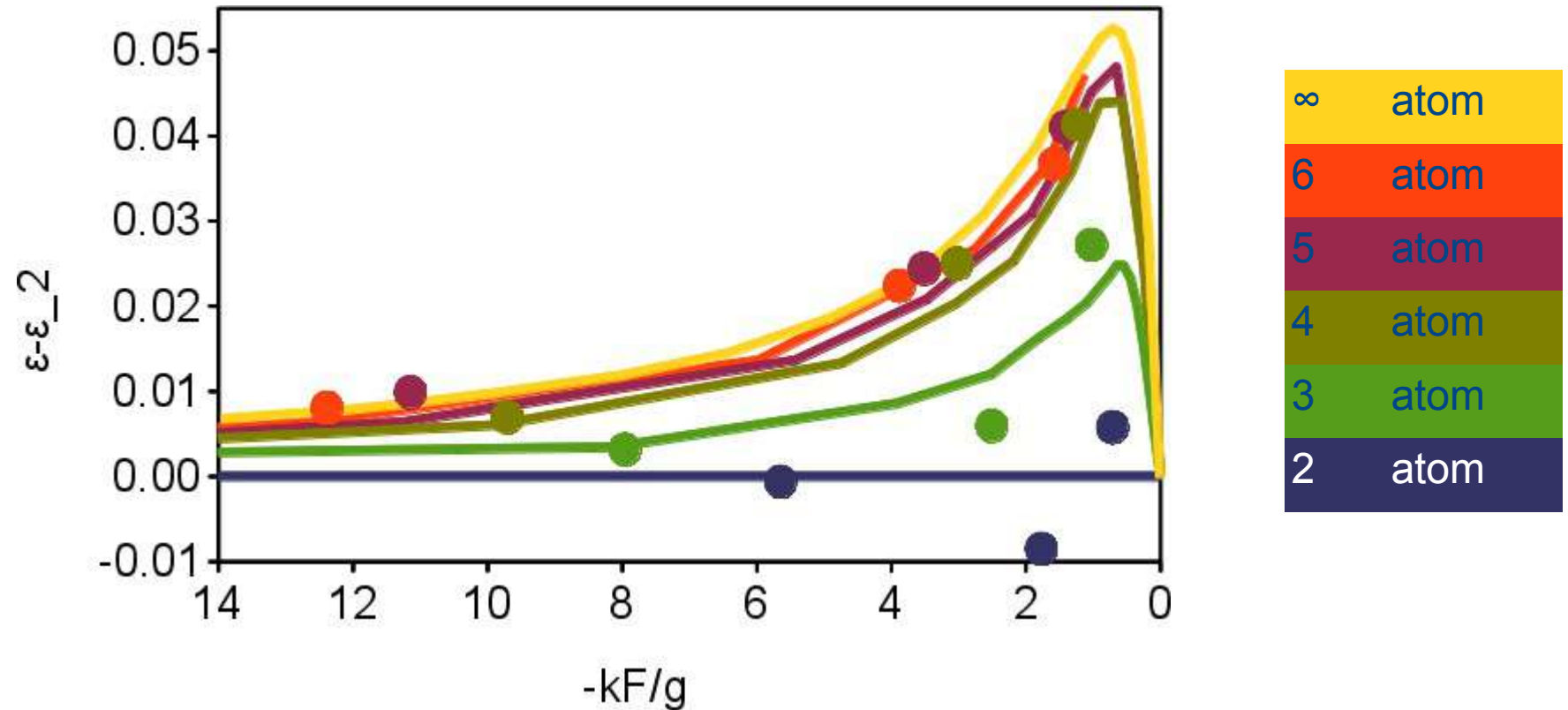
J.B. McGuire, J. Math. Phys. **6**, 432 (1965)

Polaron state



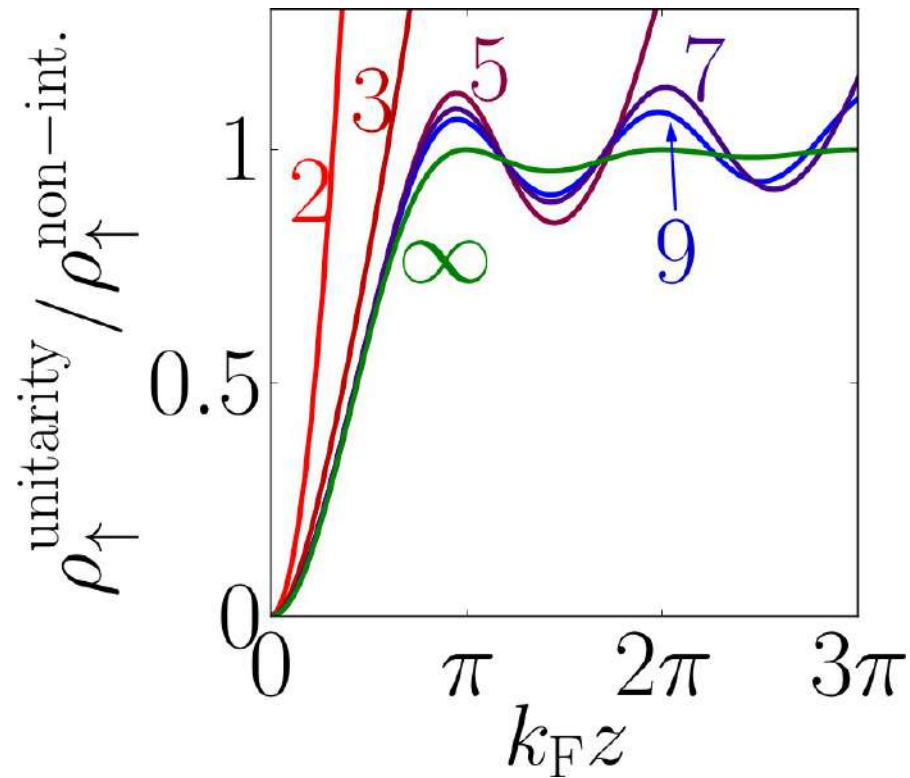
P.O. Bugnion & G.J. Conduit Phys. Rev. A **87**, 060502(R) (2013)

Polaron state



A. Wenz *et al.*, arXiv:1307.3443

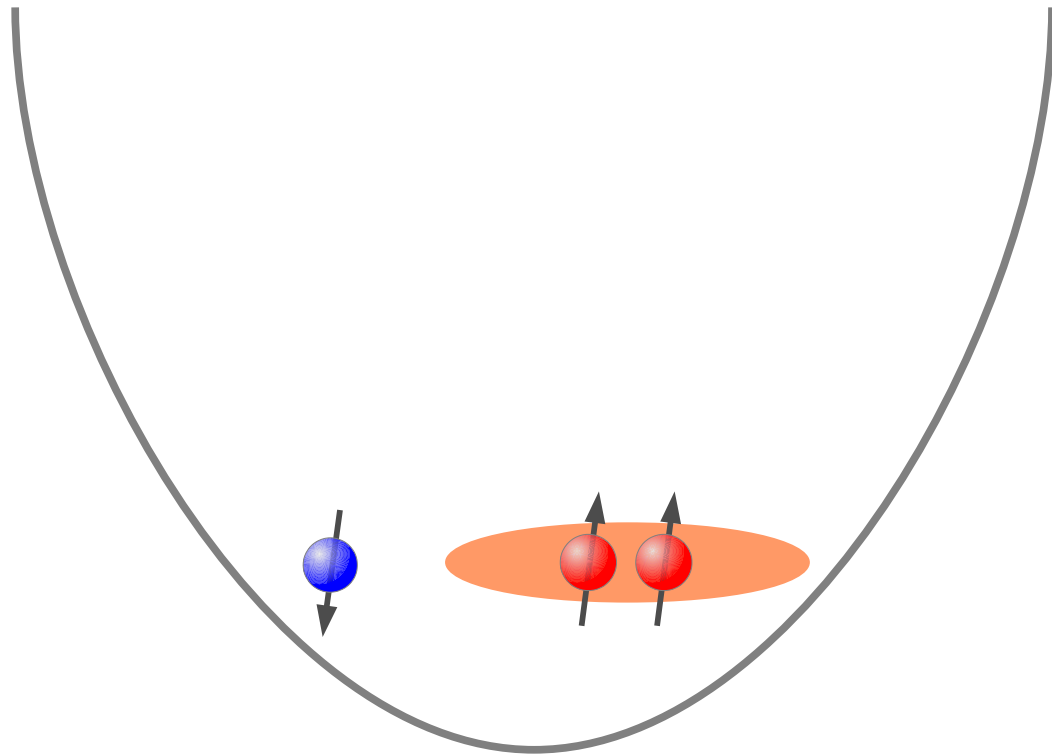
Polaron state



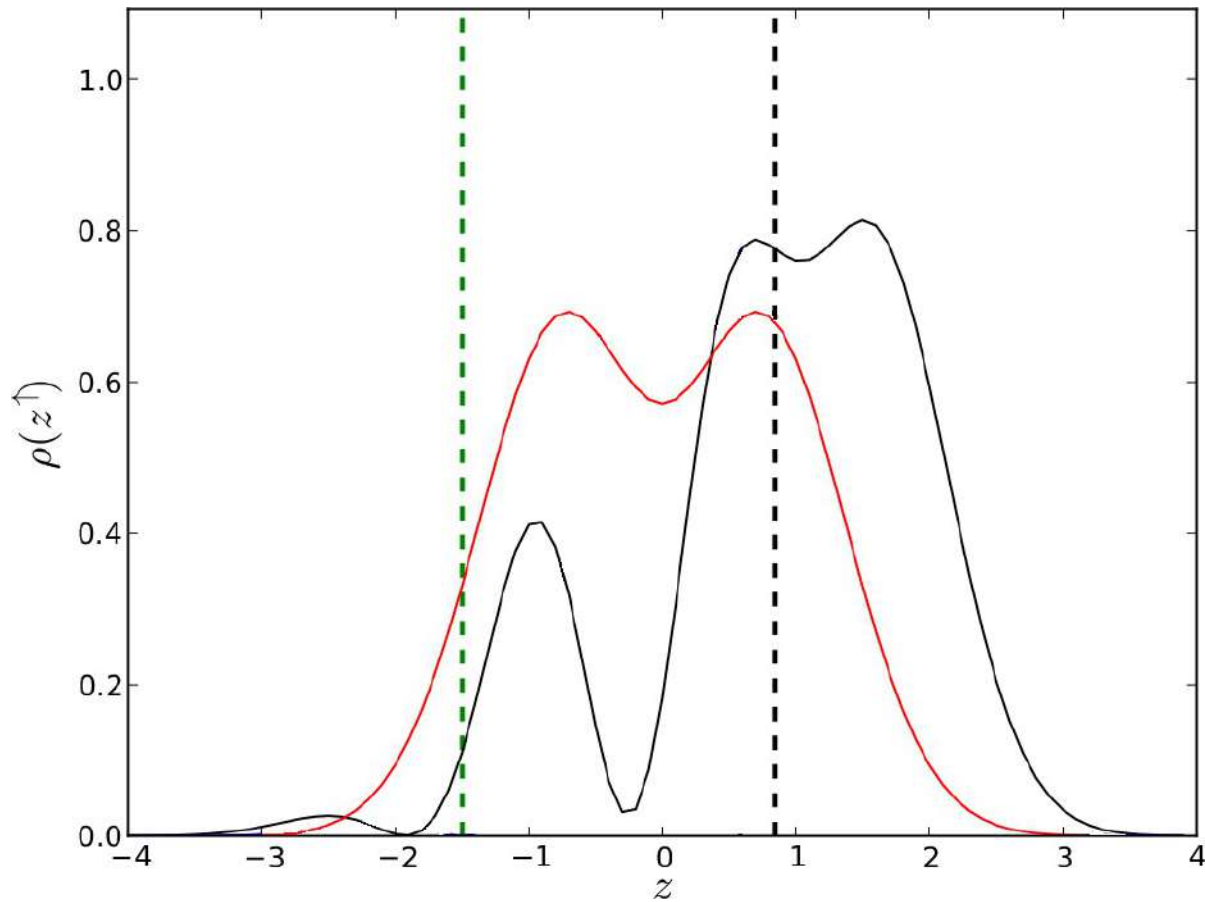
Stoner Hamiltonian

$$\hat{H} = -\frac{\nabla^2}{2} + gn_{\uparrow}(\vec{r})n_{\downarrow}(\vec{r}) + V(\vec{r})$$

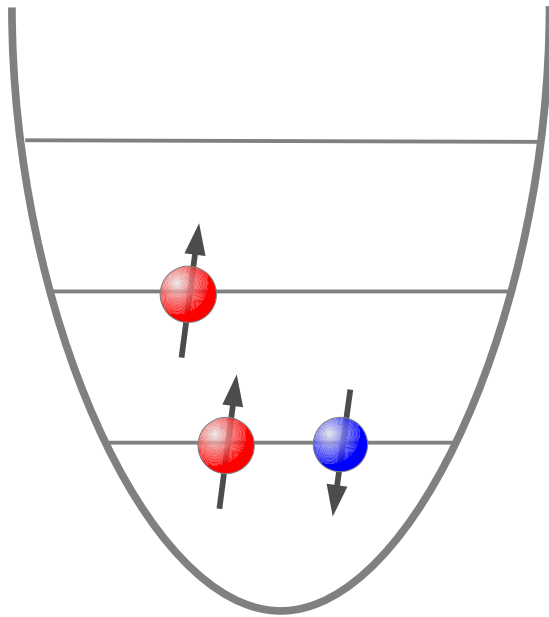
Density profiles



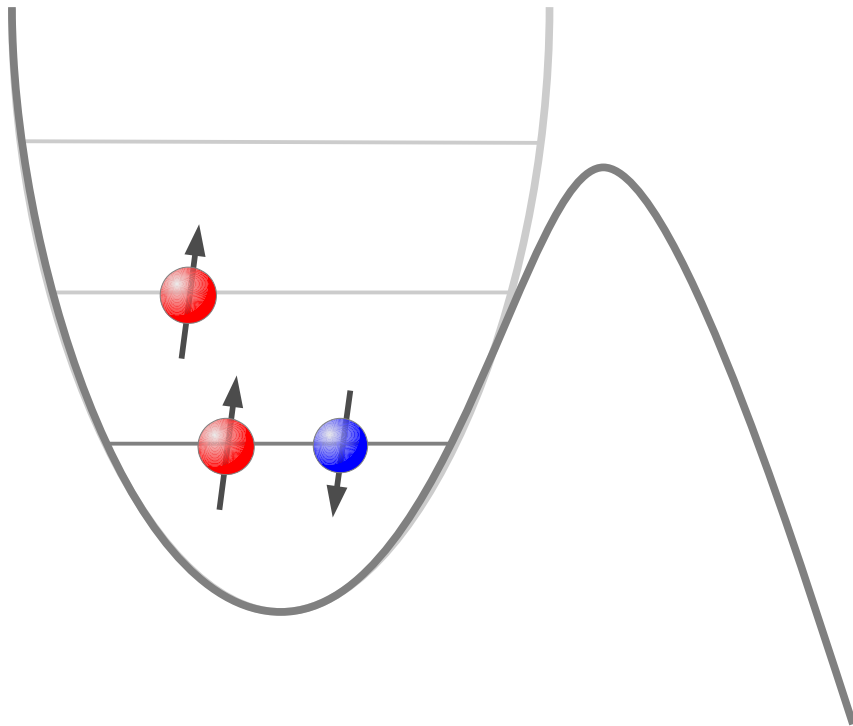
Density profiles



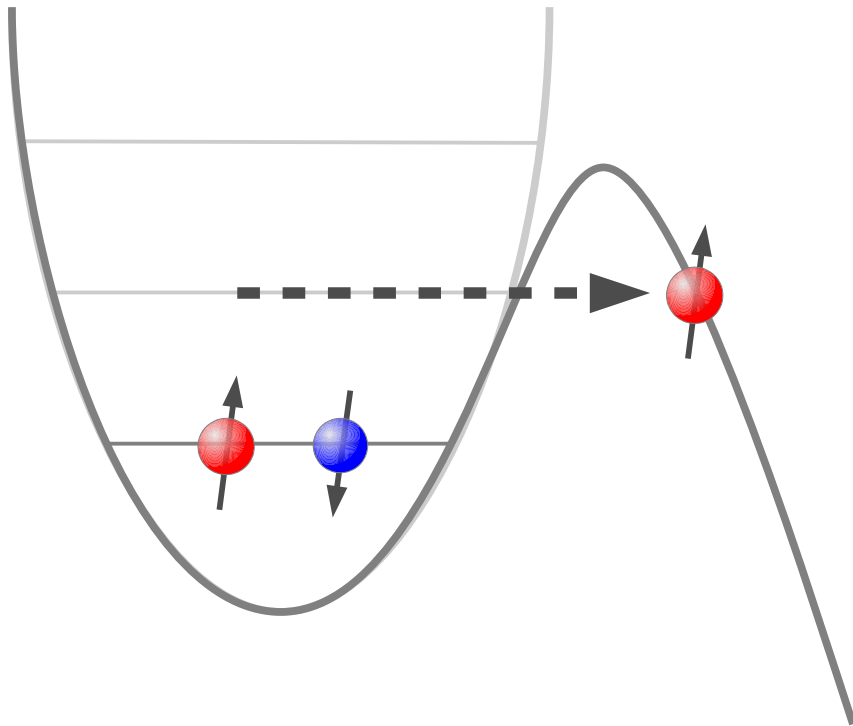
Polaron state



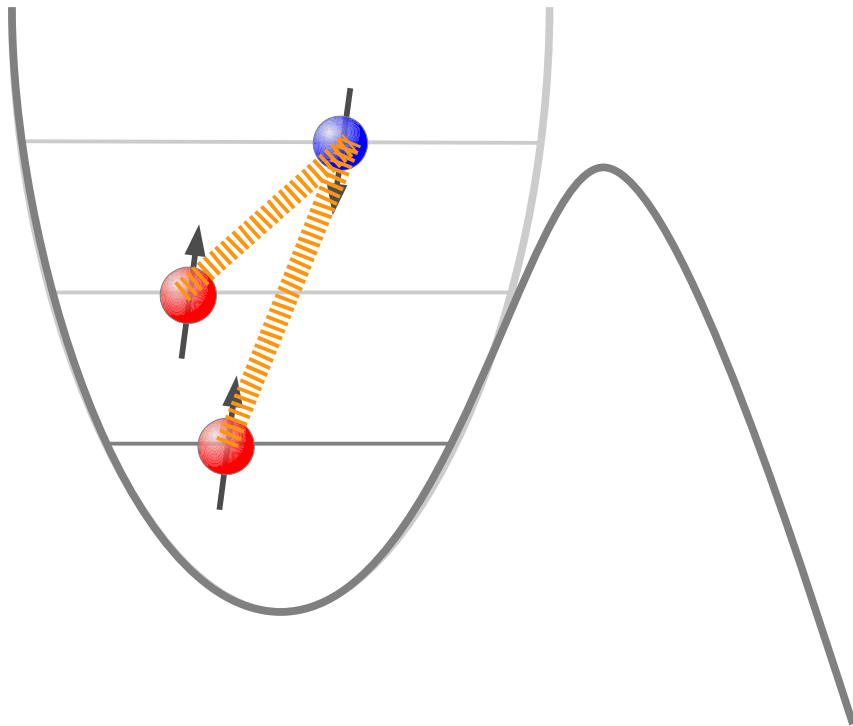
Polaron state



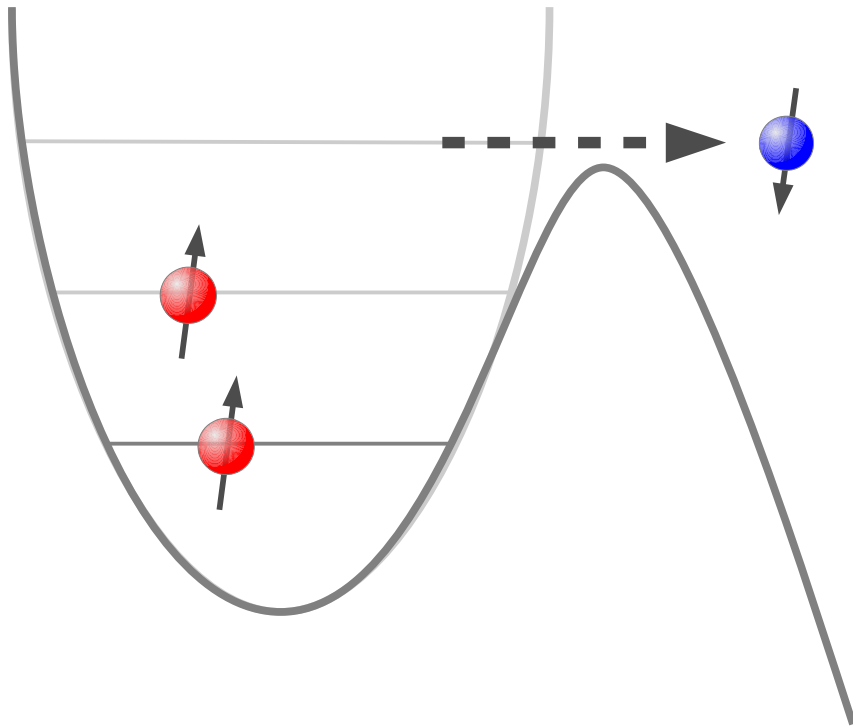
Polaron state



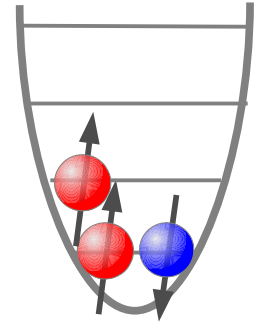
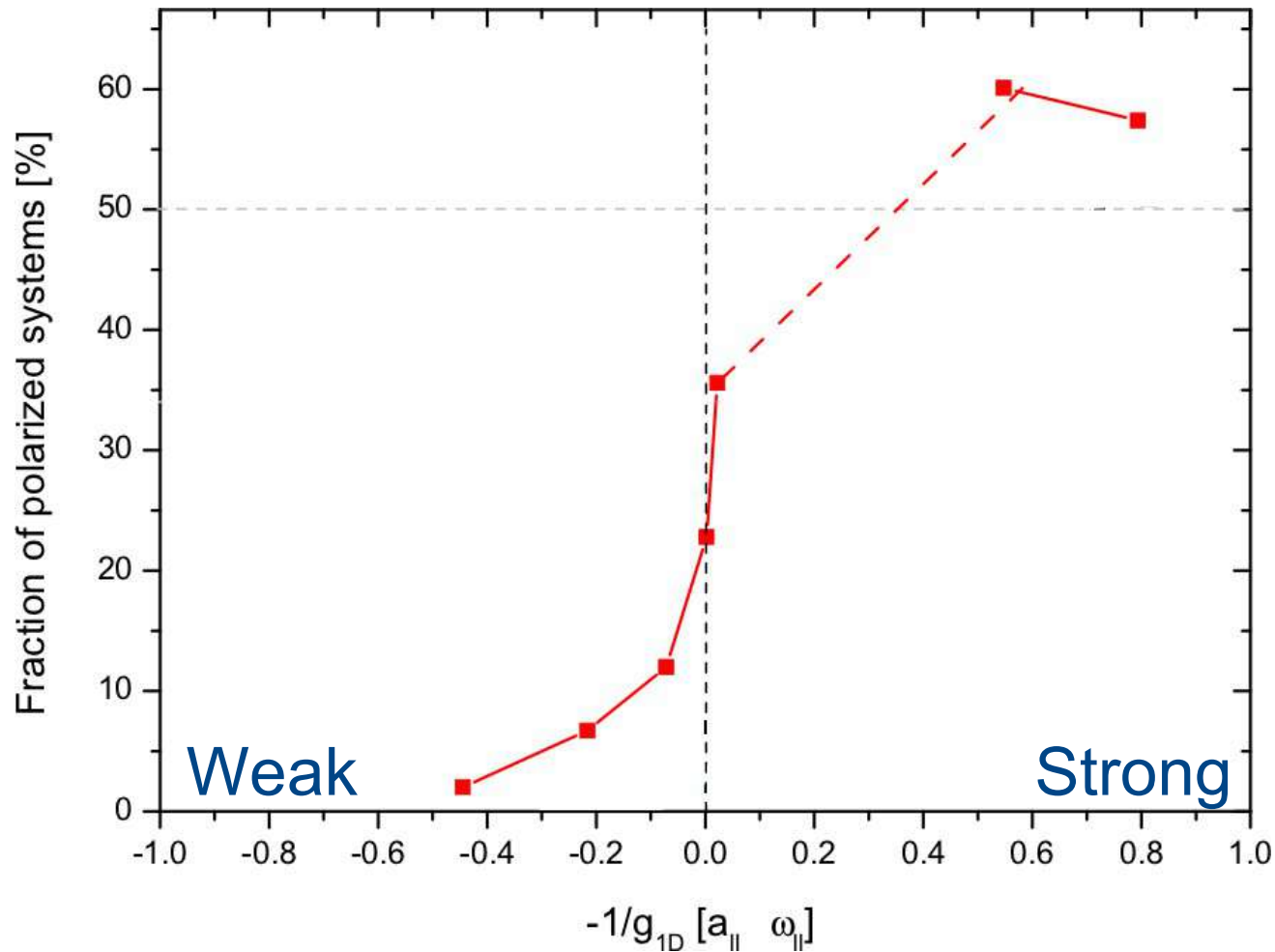
Polaron state



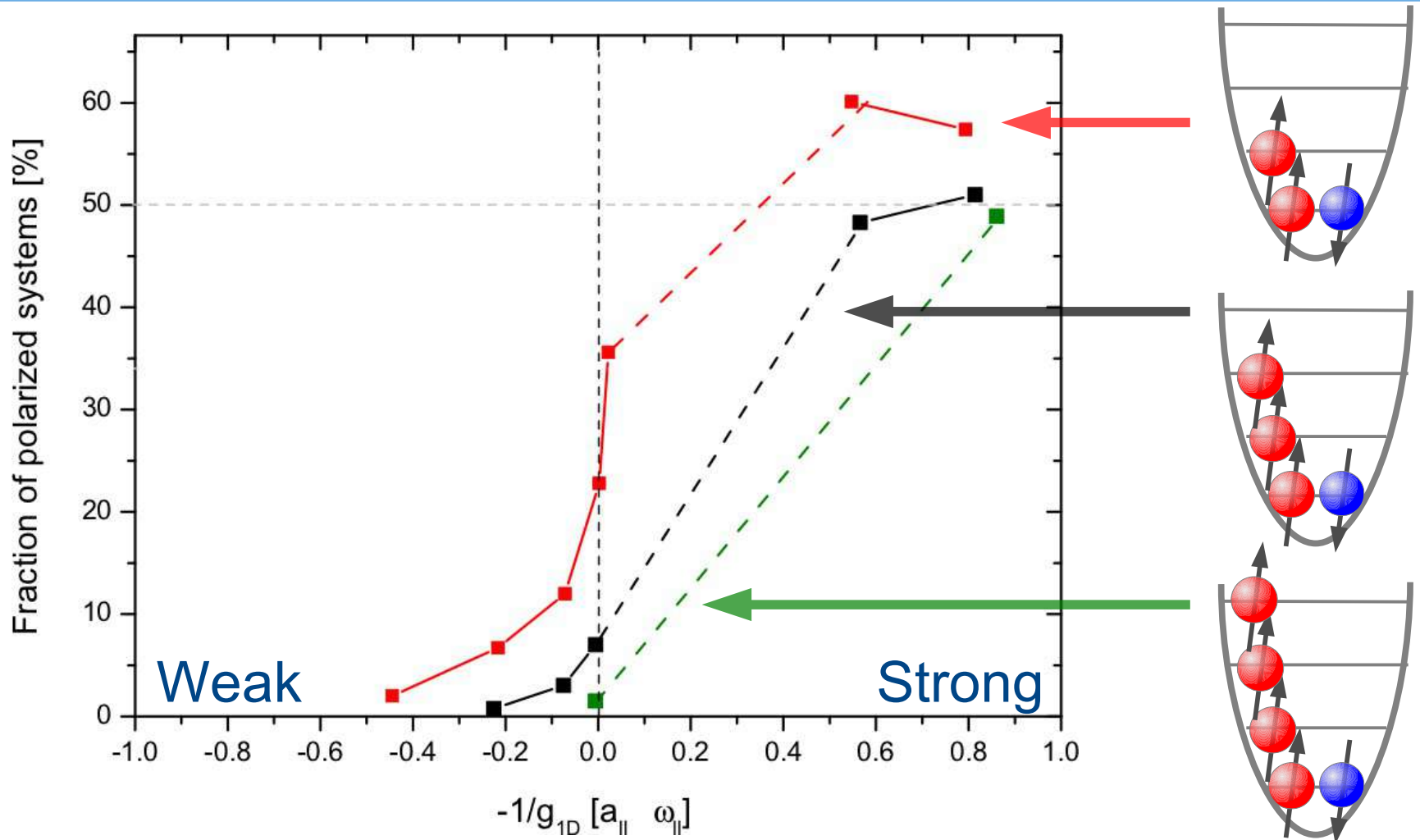
Polaron state



Loss region

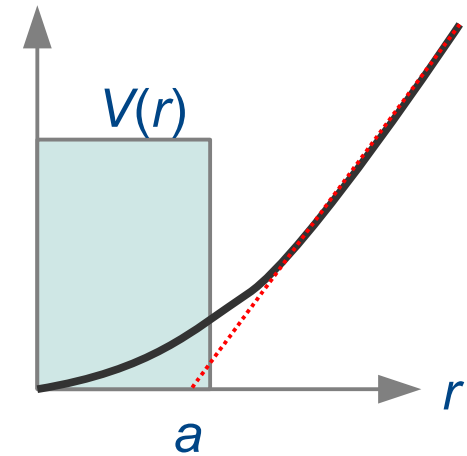


Tunneling probability



Two-atom scattering

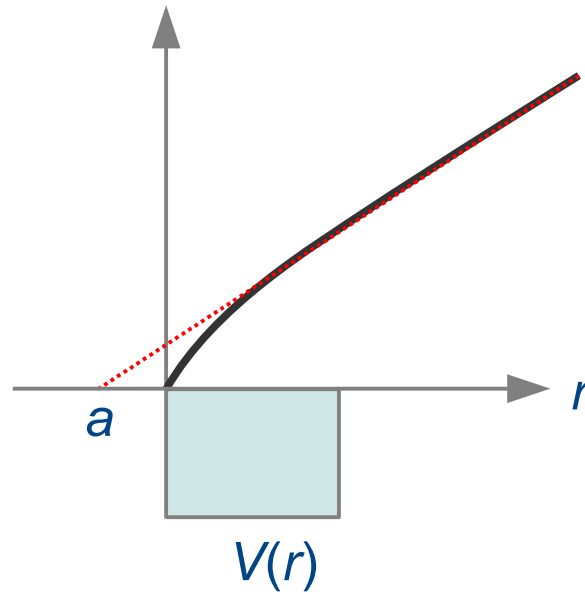
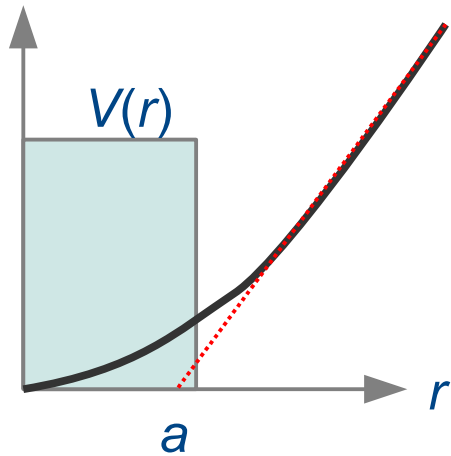
Repulsive



Two-atom scattering

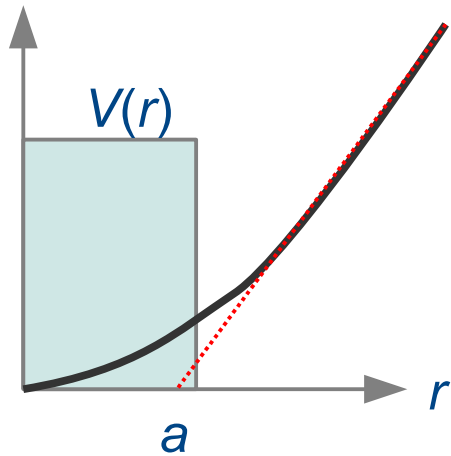
Repulsive

Attractive

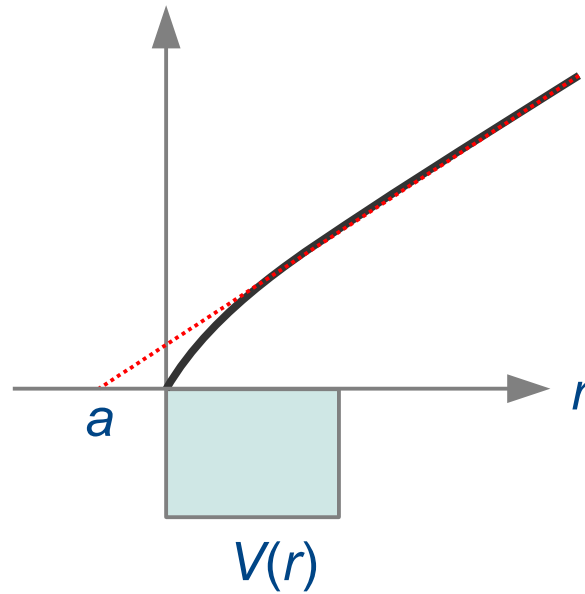


Two-atom scattering

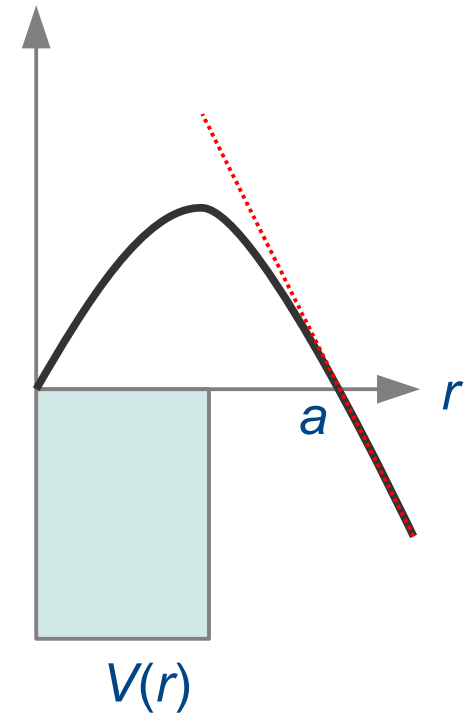
Repulsive



Attractive

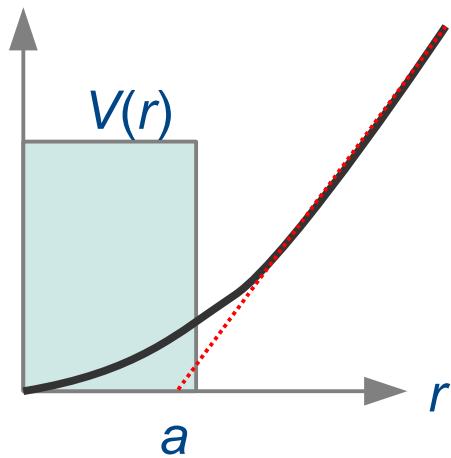


Repulsive

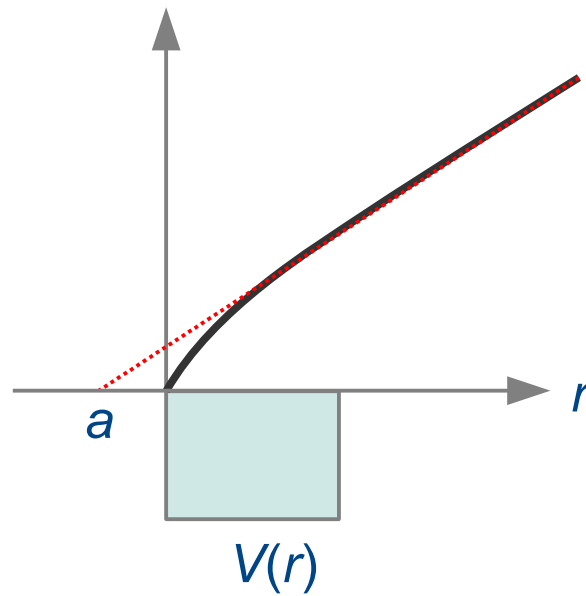


Two-atom scattering

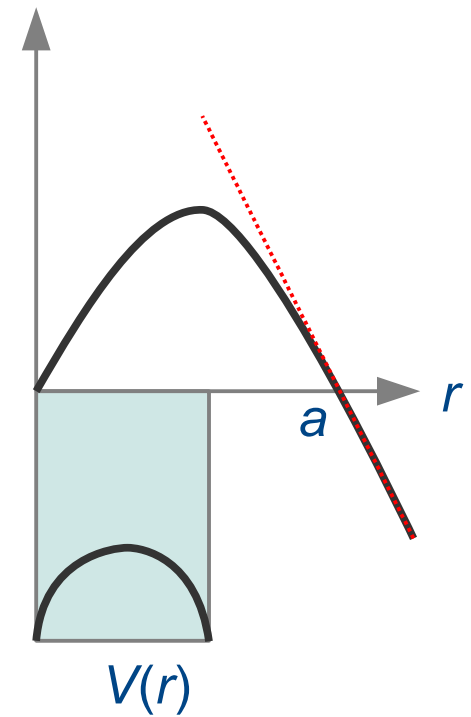
Repulsive



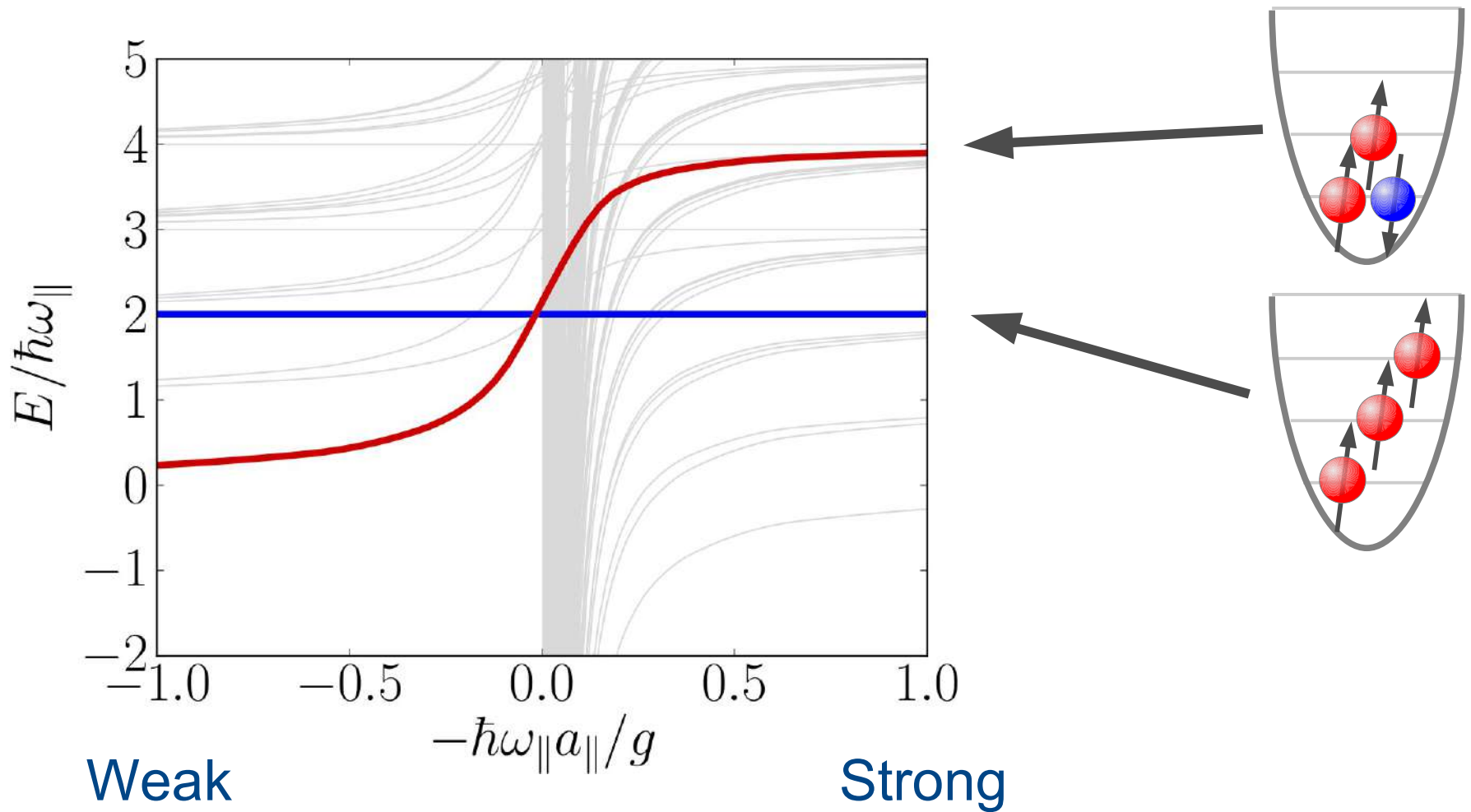
Attractive



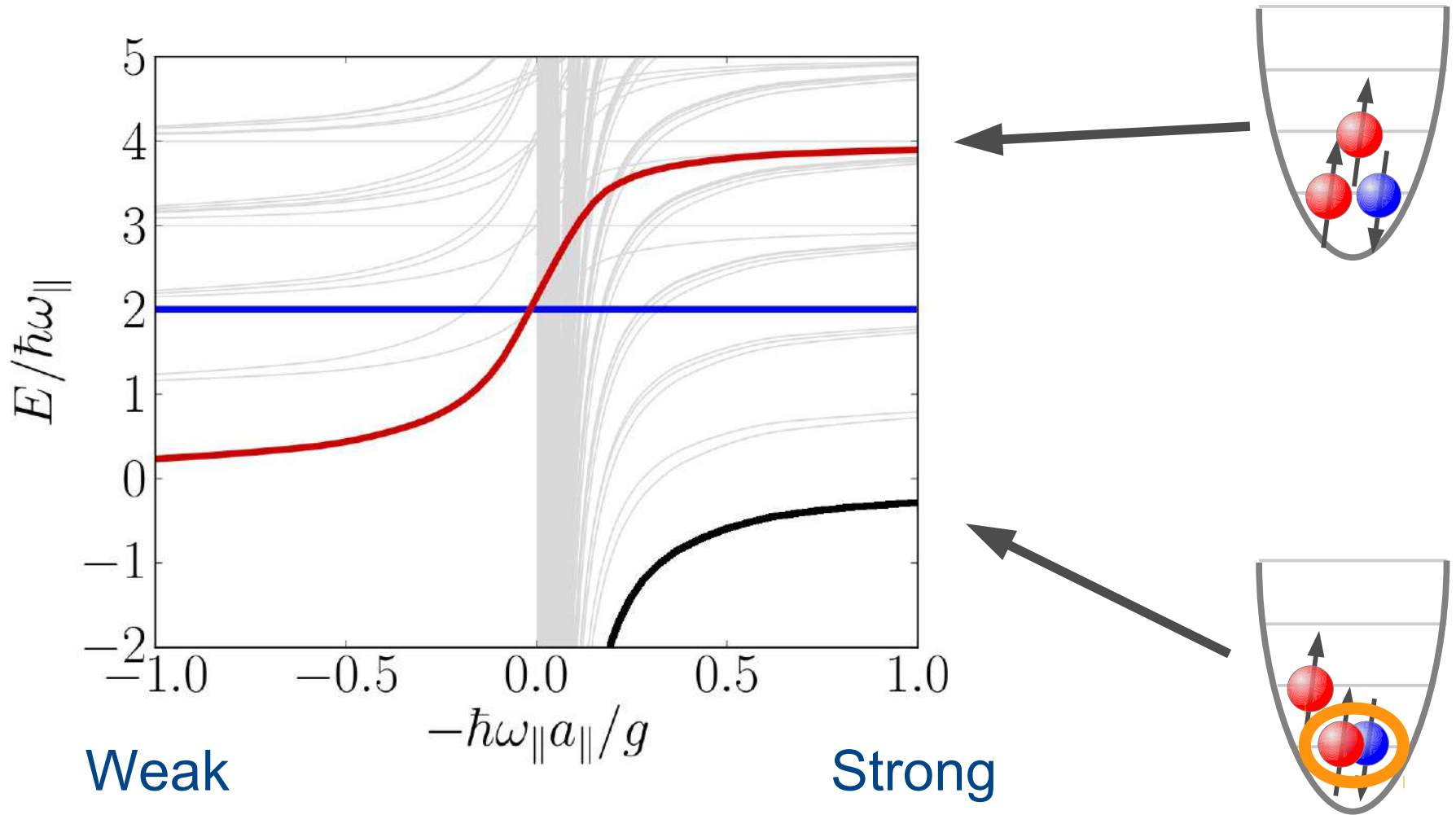
Repulsive



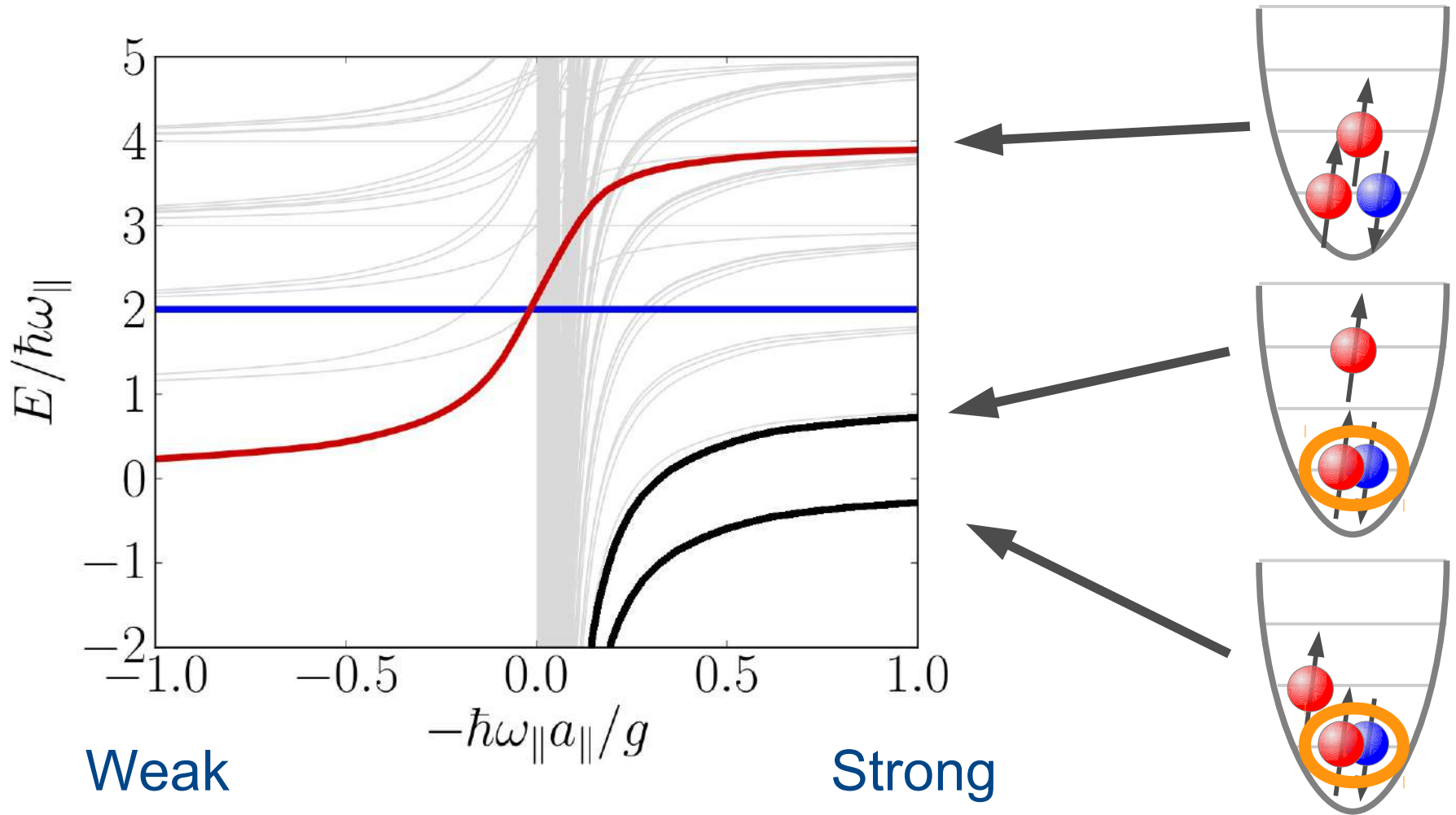
Three-atom bound state



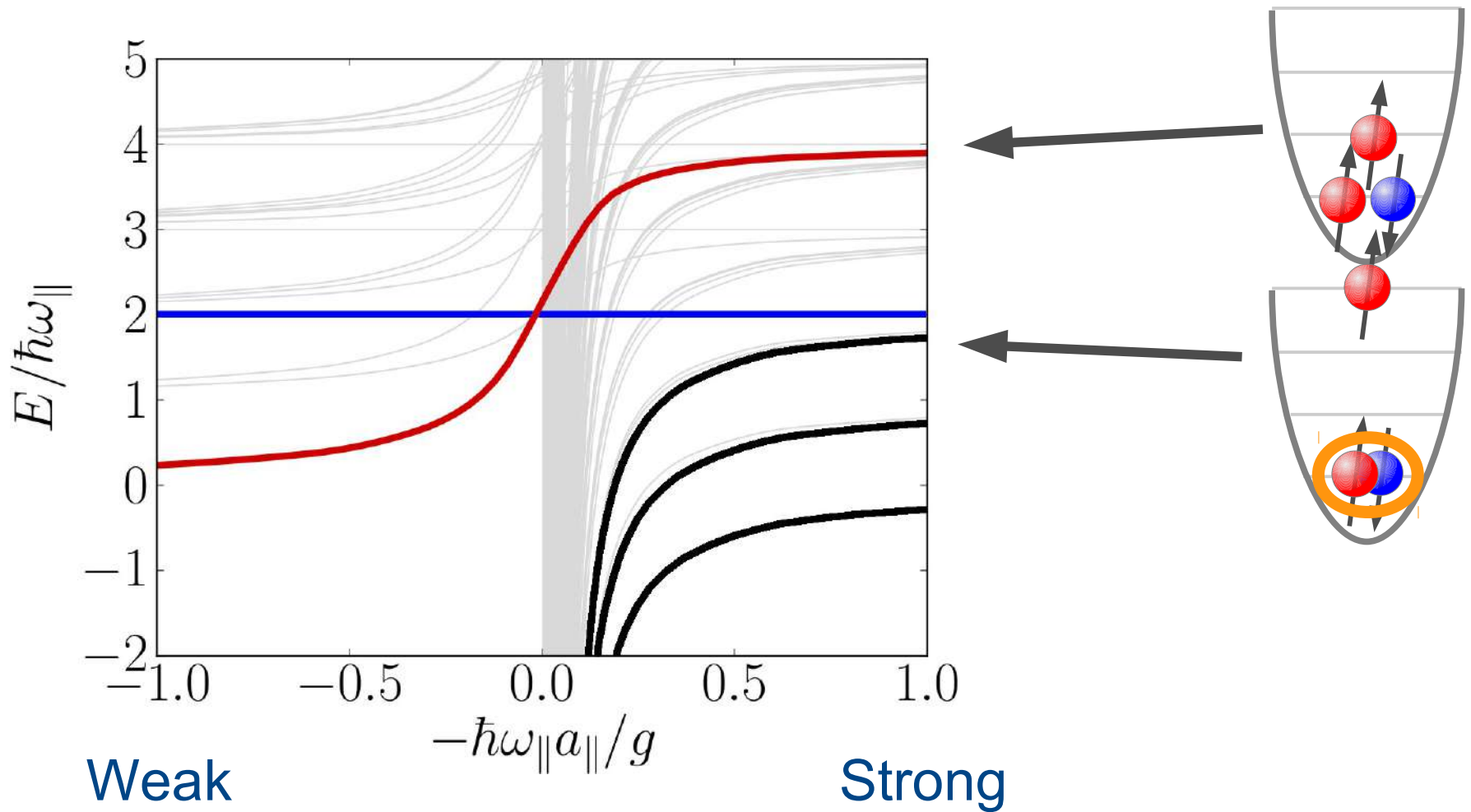
Three-atom bound state



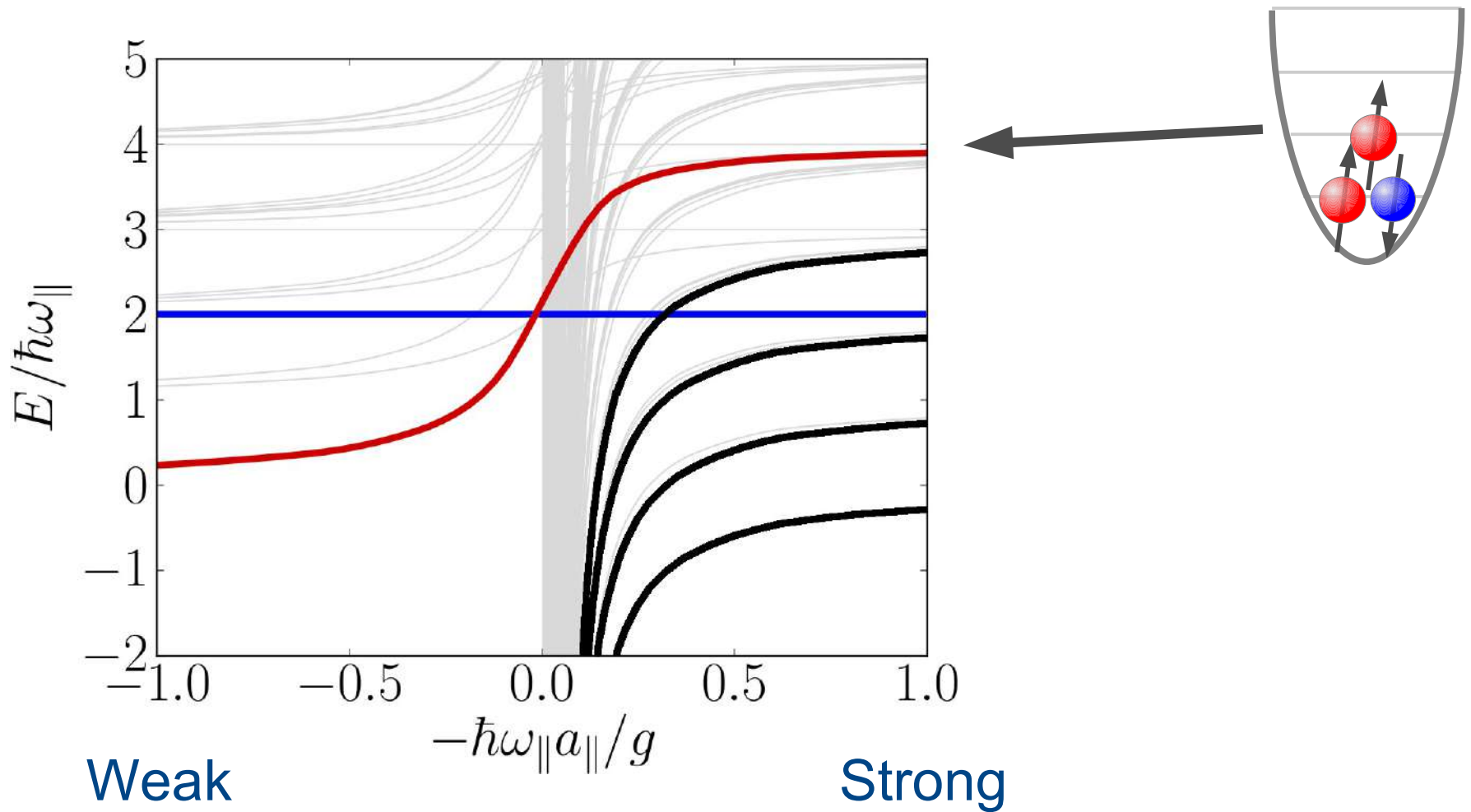
Three-atom bound state



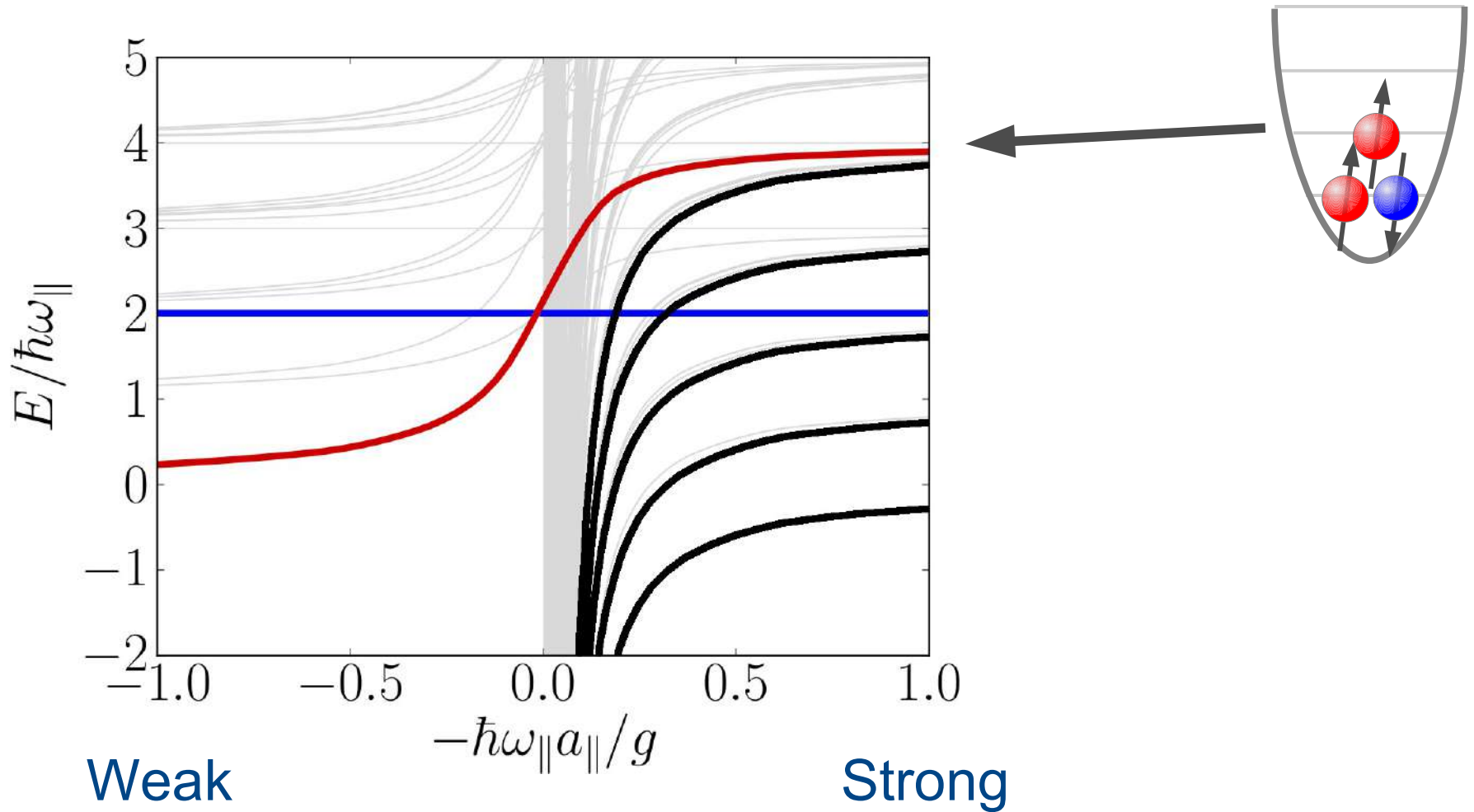
Three-atom bound state



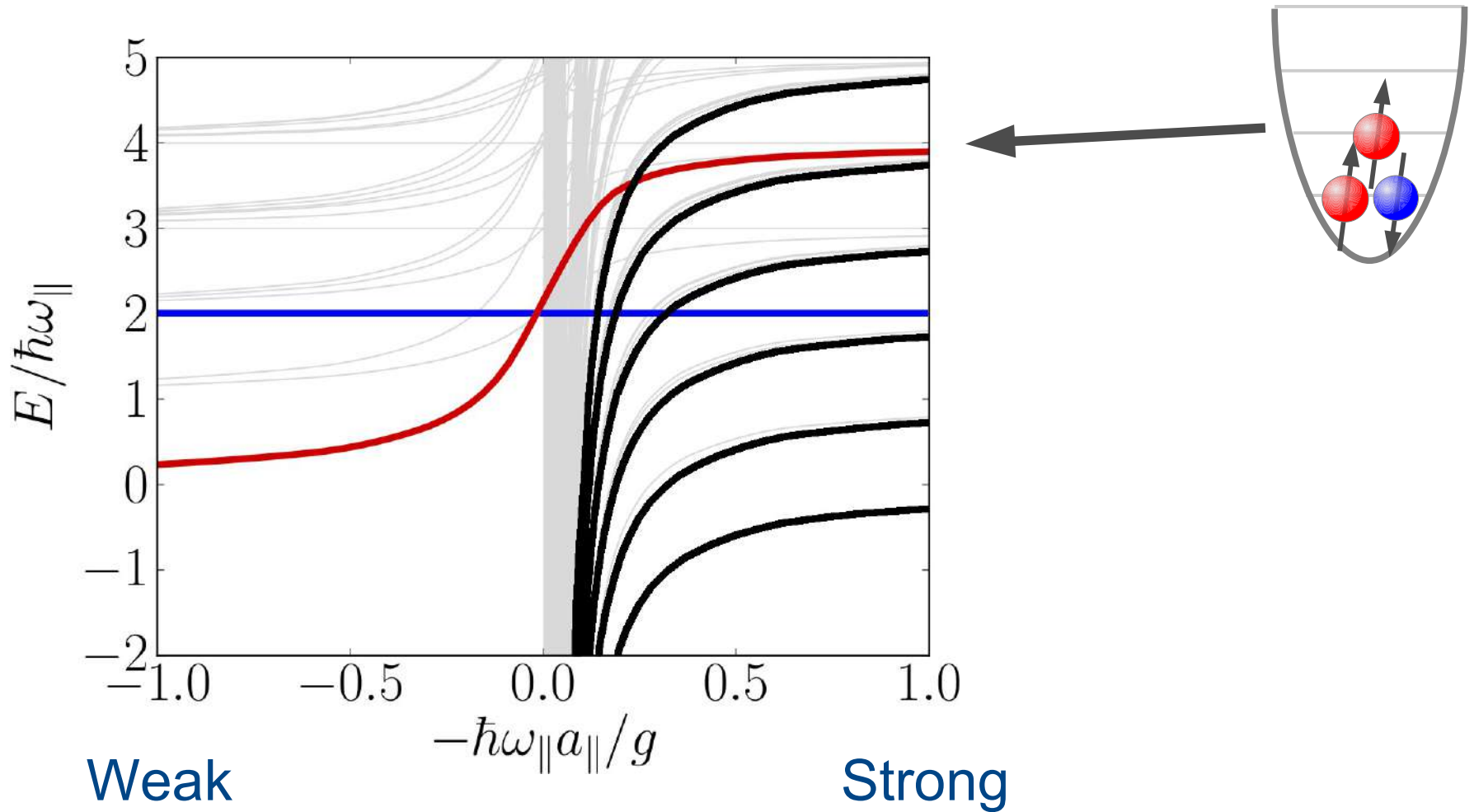
Three-atom bound state



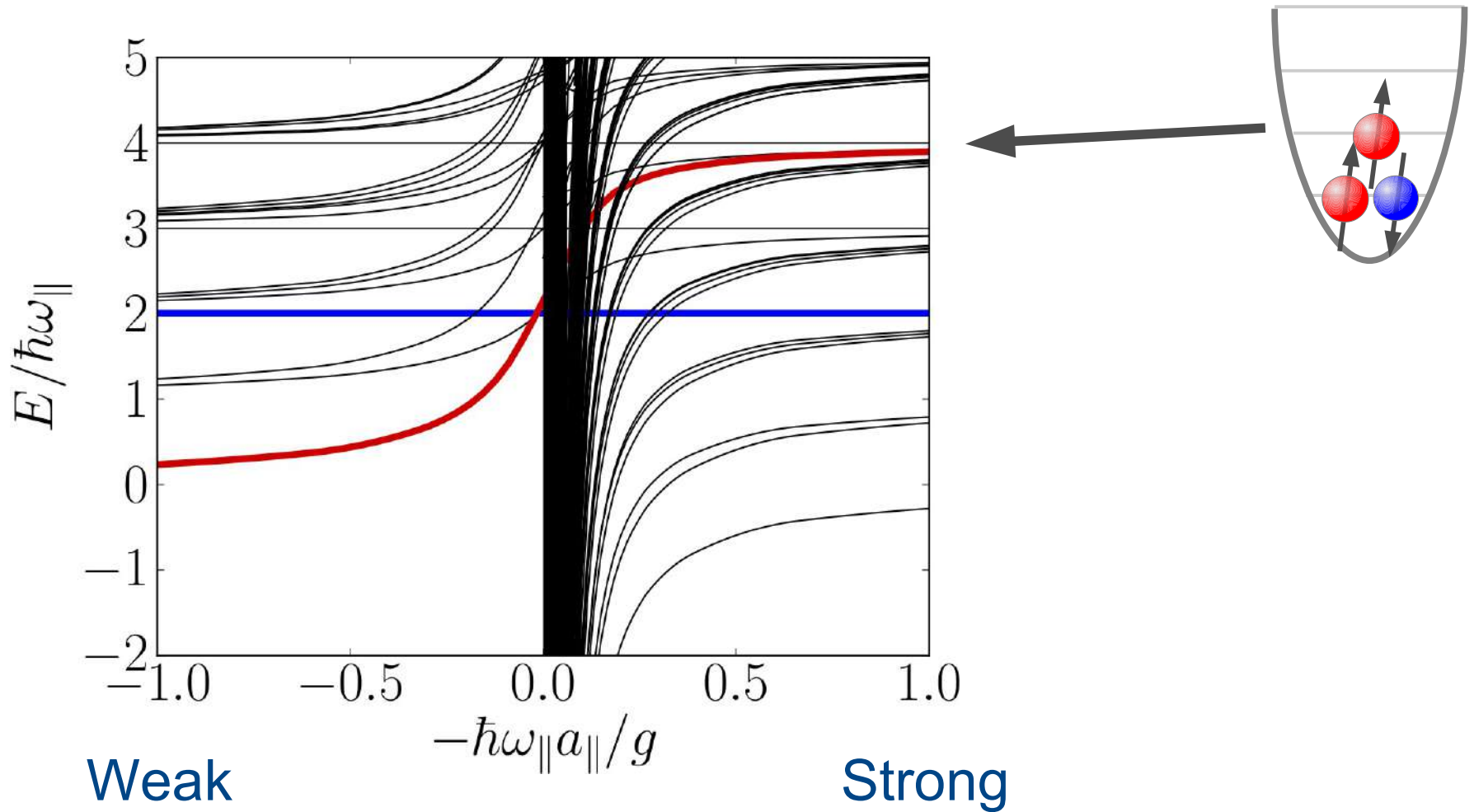
Three-atom bound state



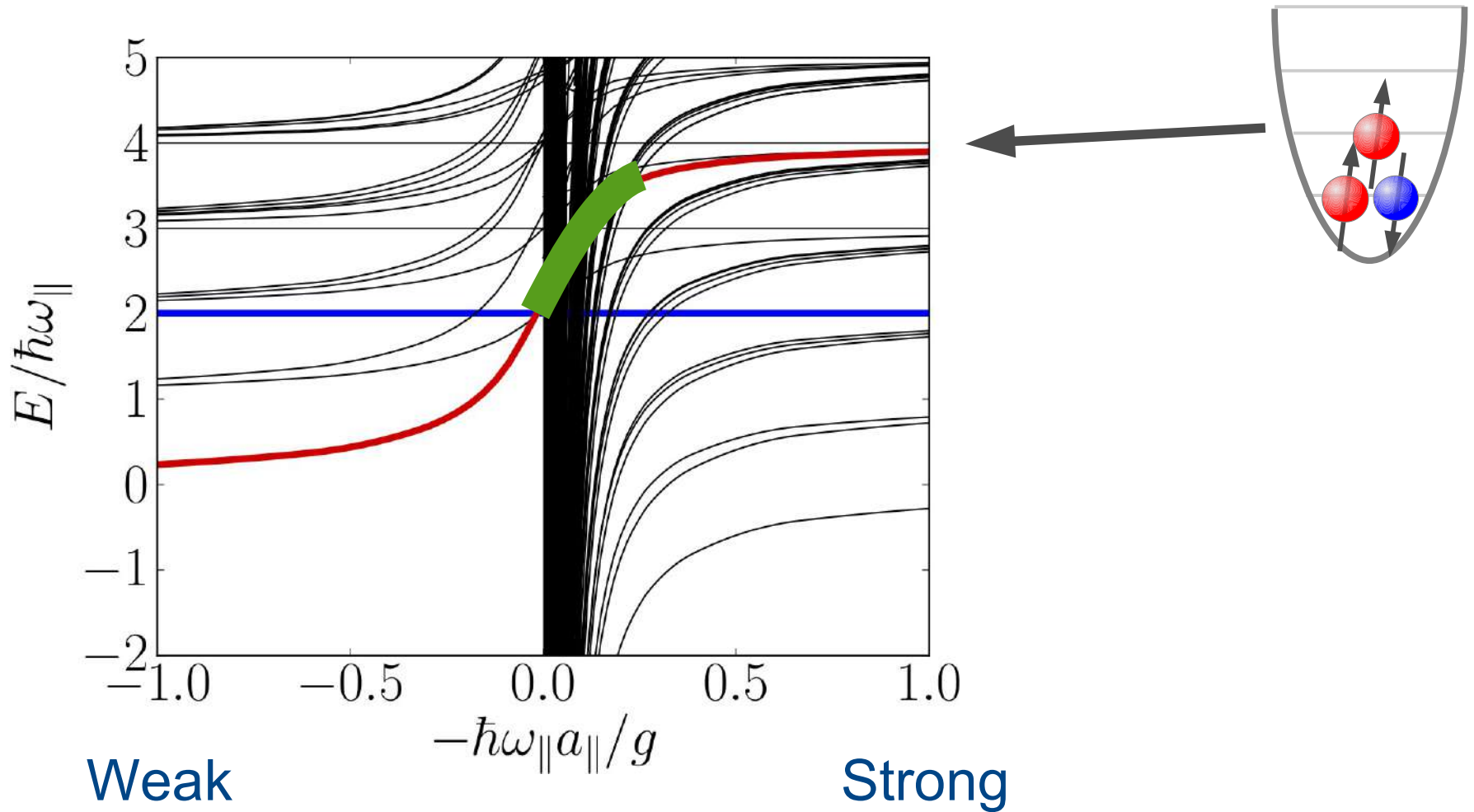
Three-atom bound state



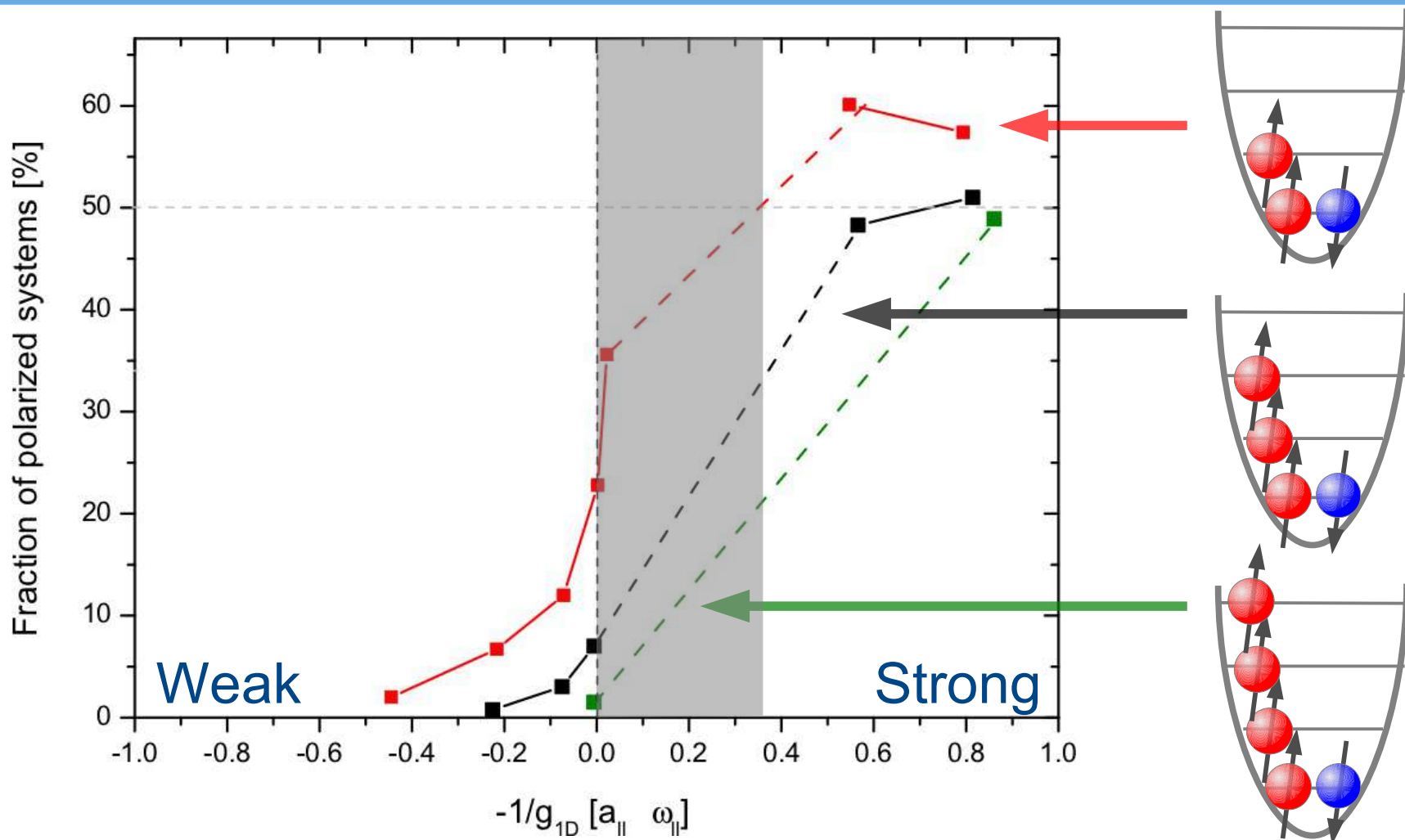
Three-atom bound state



Three-atom bound state

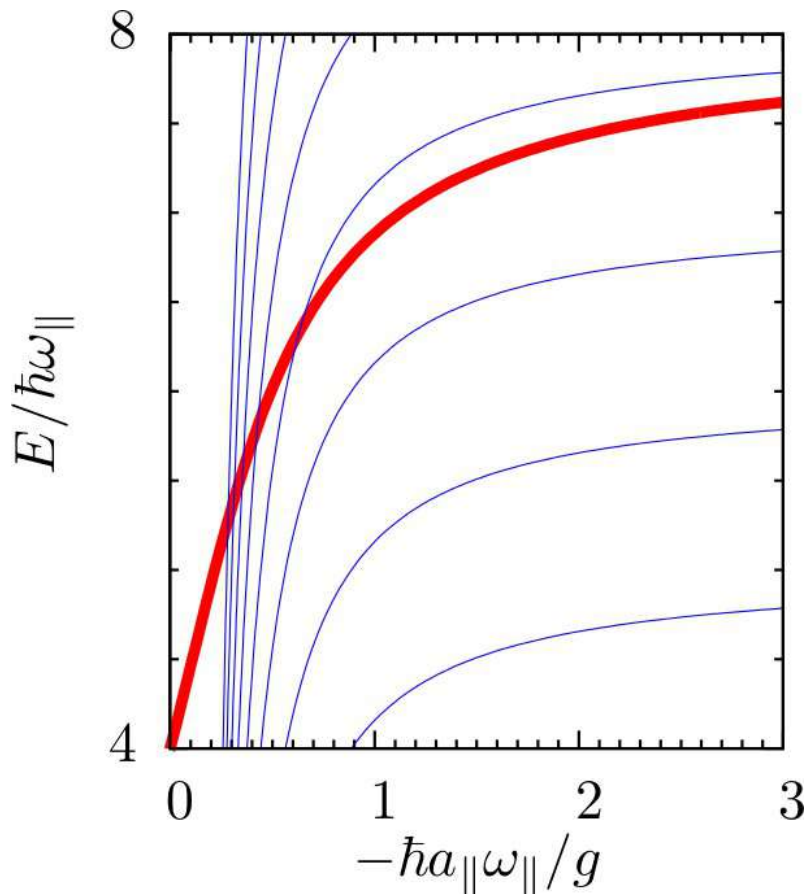


Tunneling probability

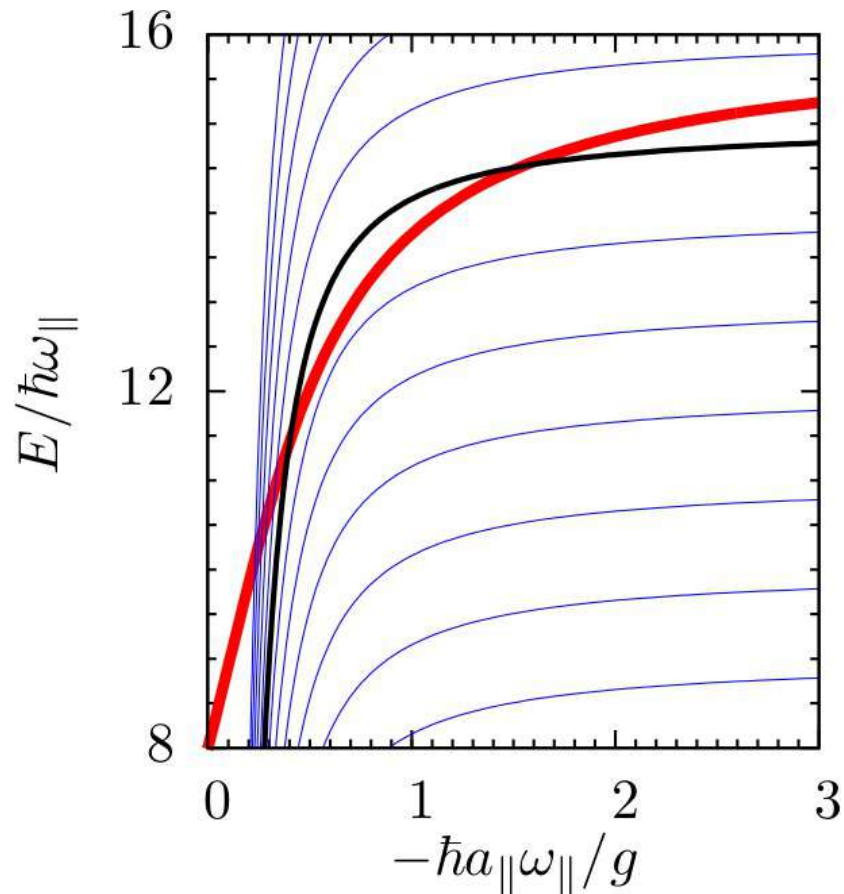


Band crossings

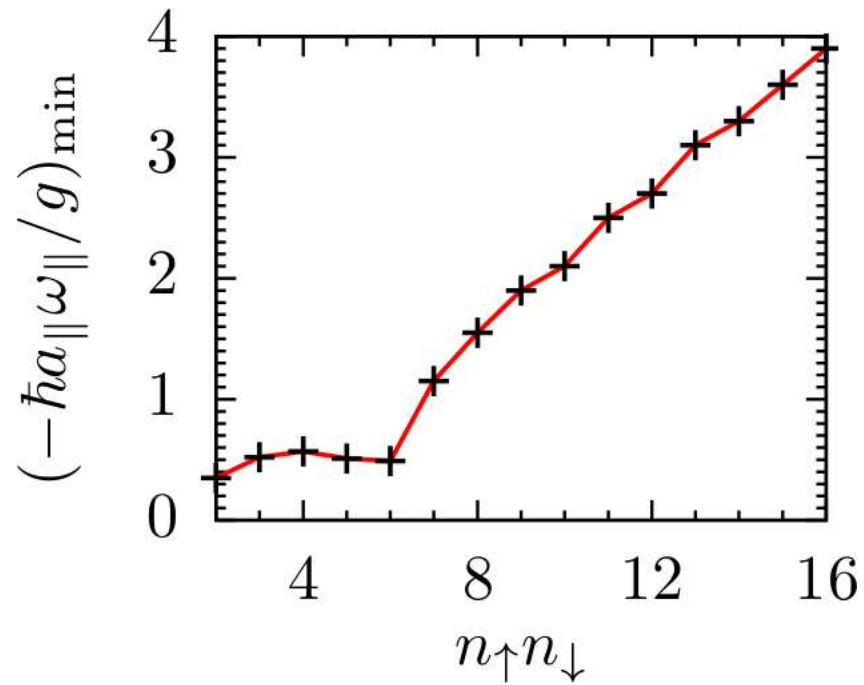
$$n_{\uparrow}n_{\downarrow} = 4$$



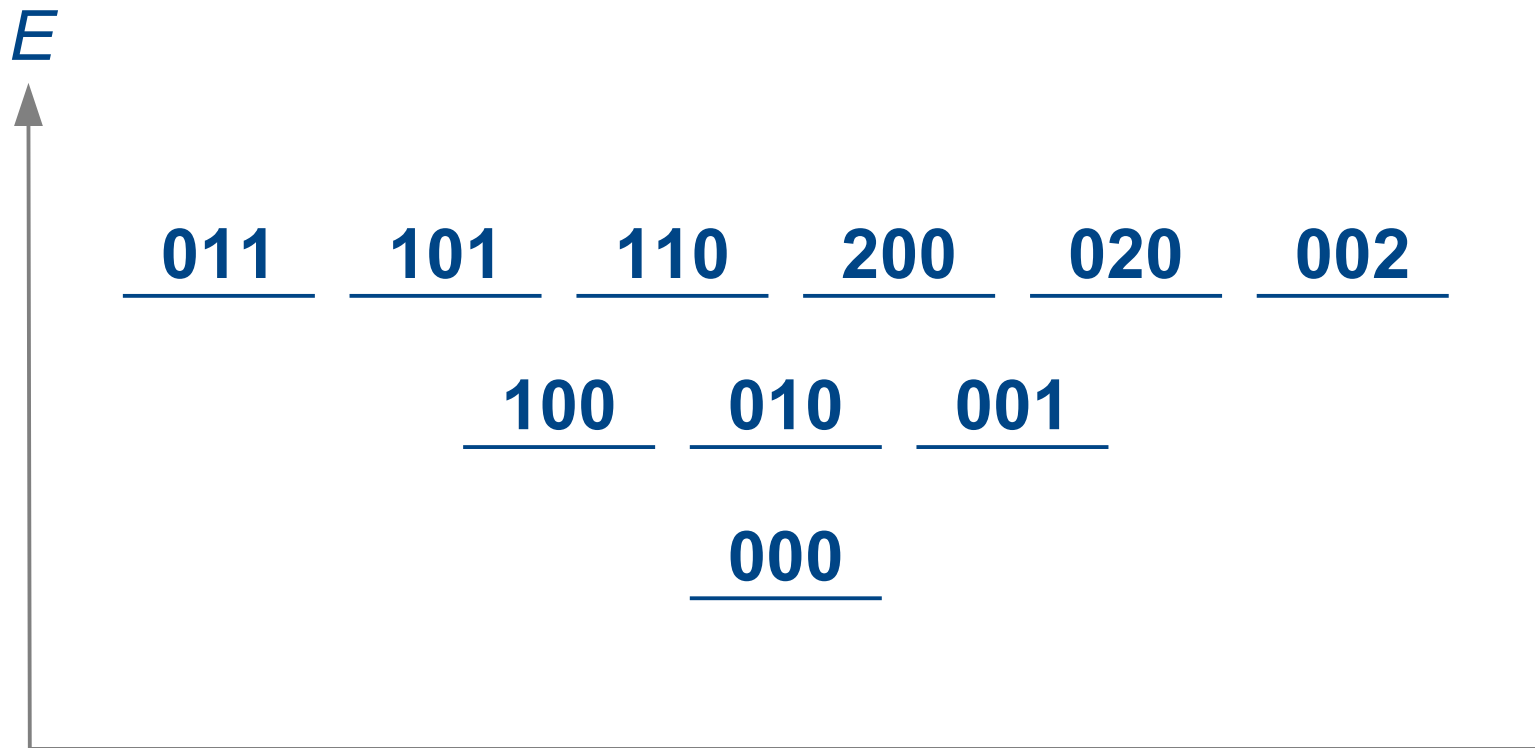
$$n_{\uparrow}n_{\downarrow} = 8$$



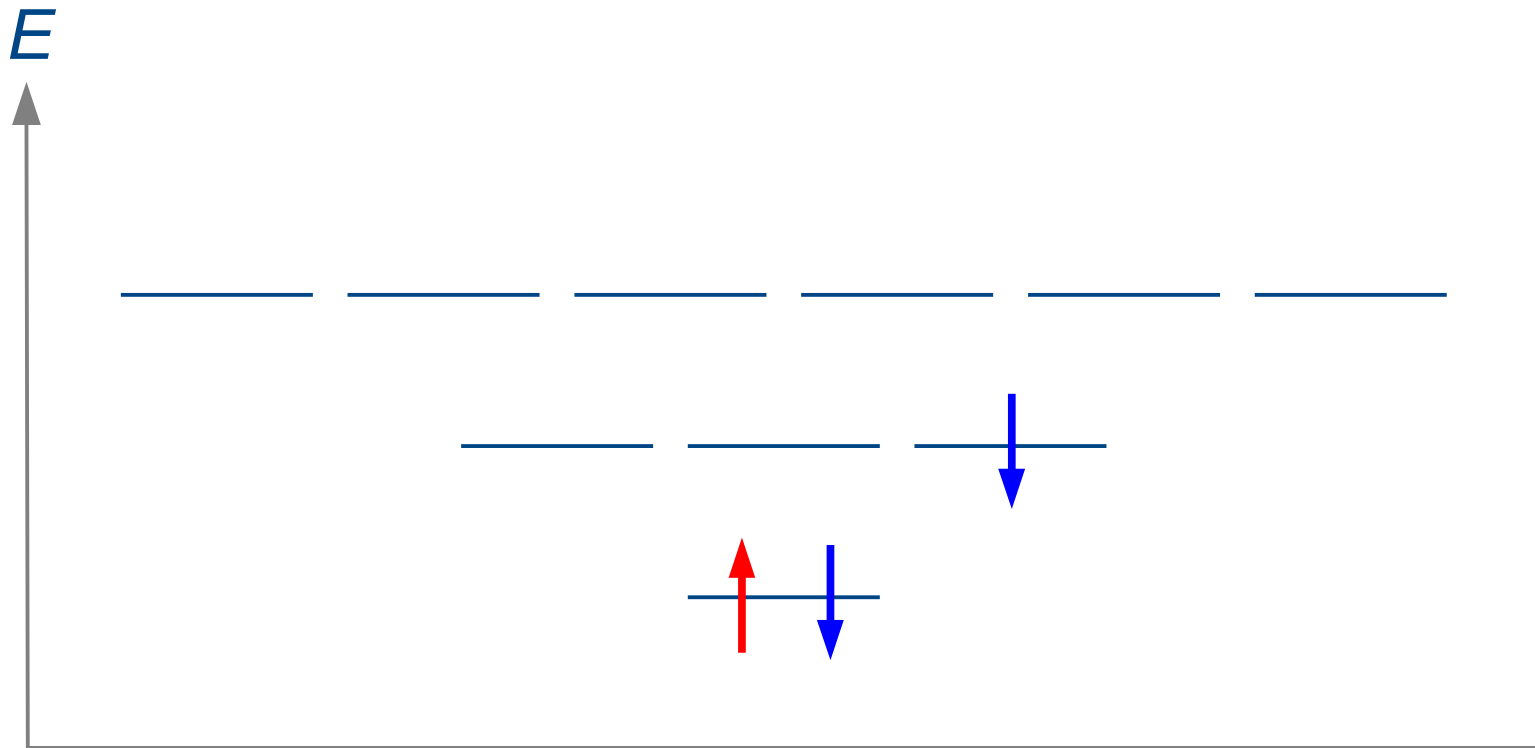
Band crossings



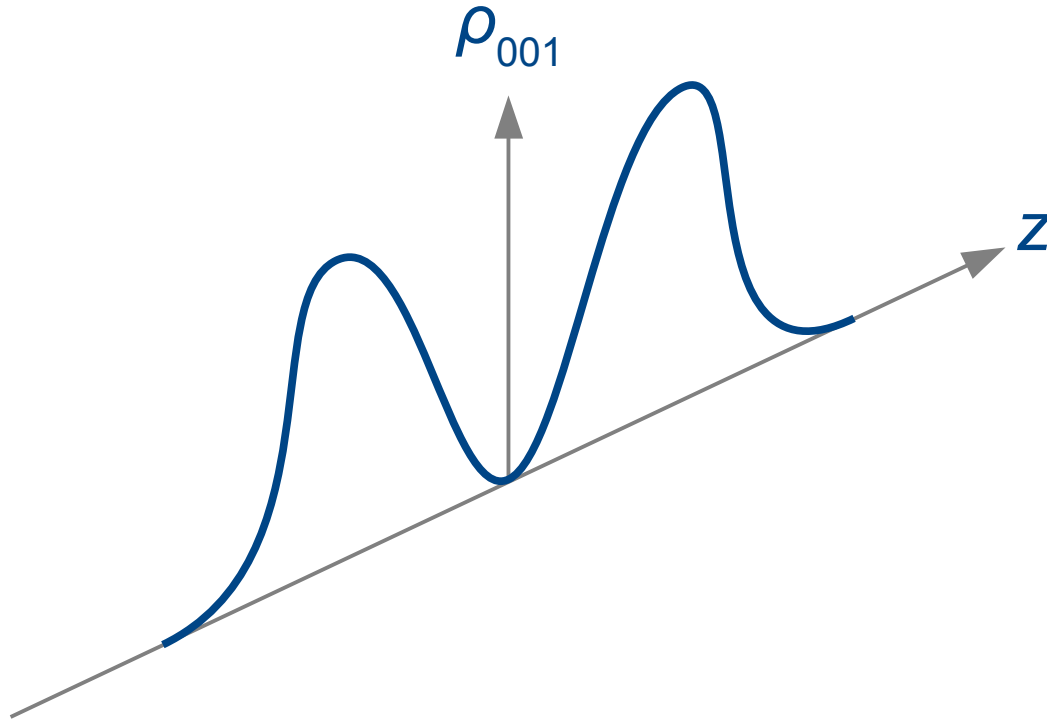
Inhomogeneous pairing



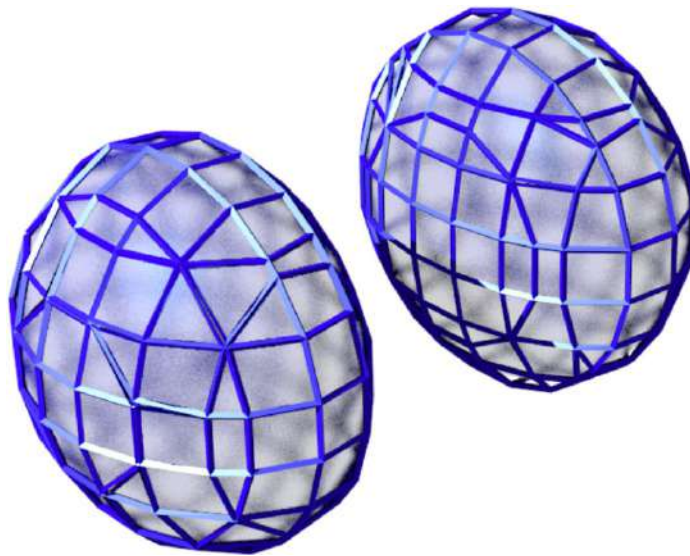
Inhomogeneous pairing



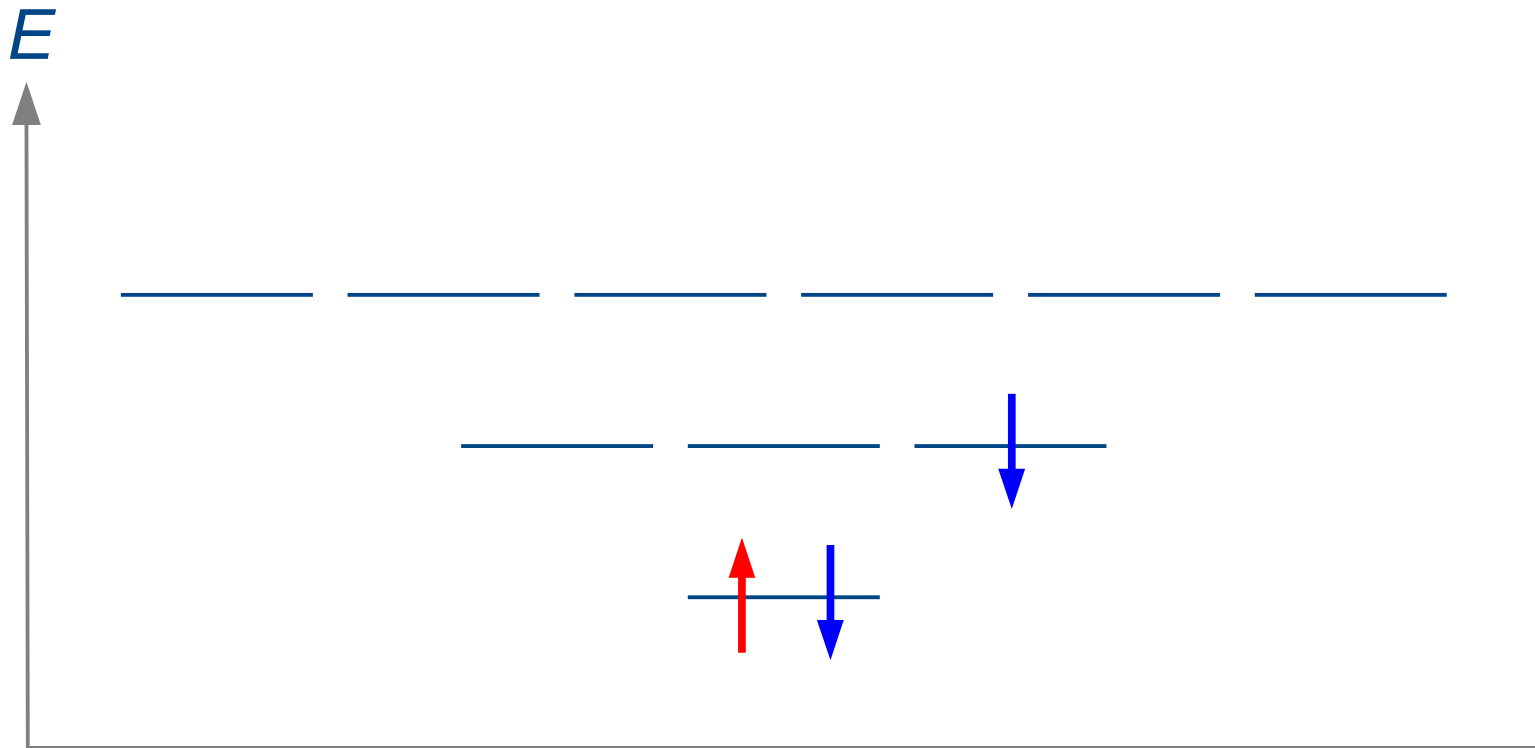
Inhomogeneous pairing



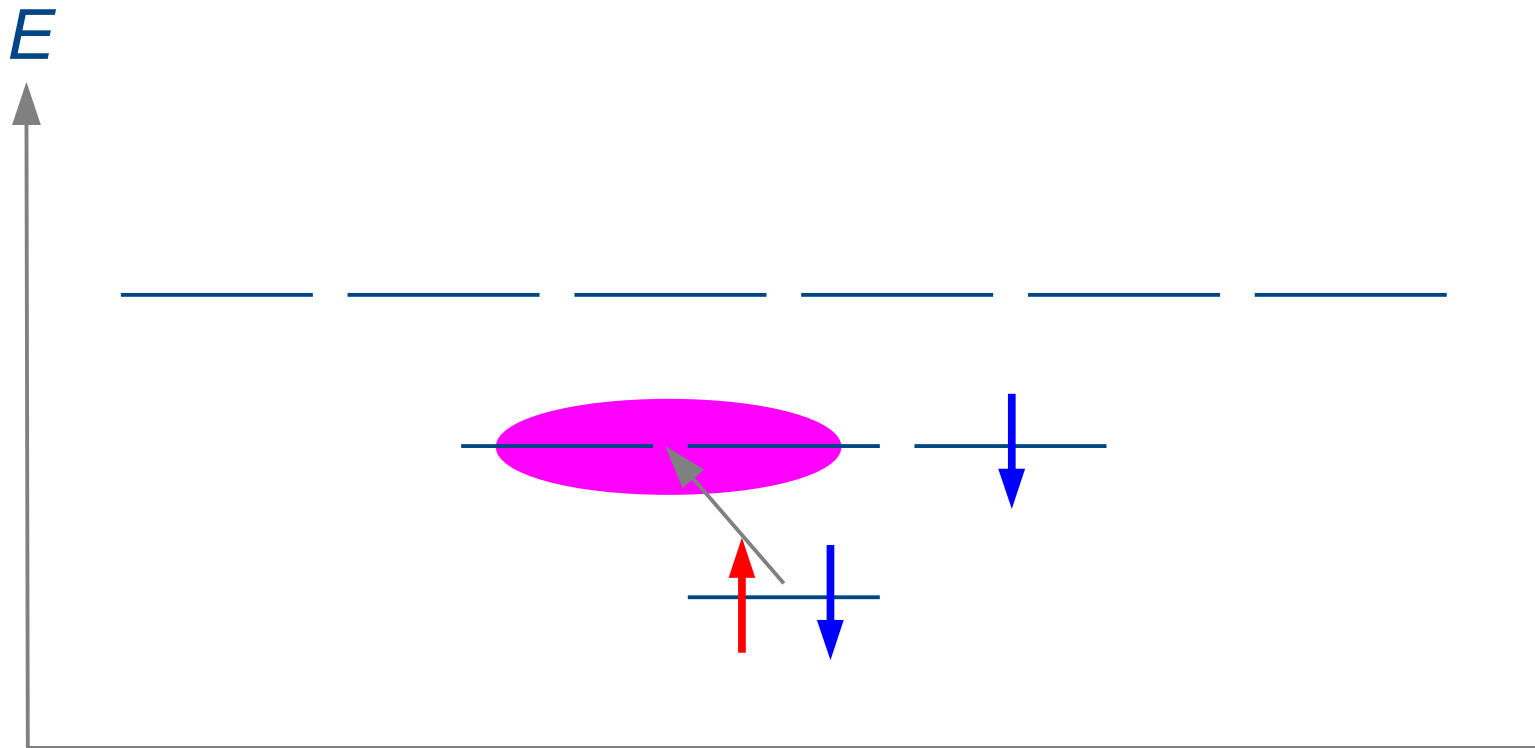
Inhomogeneous pairing



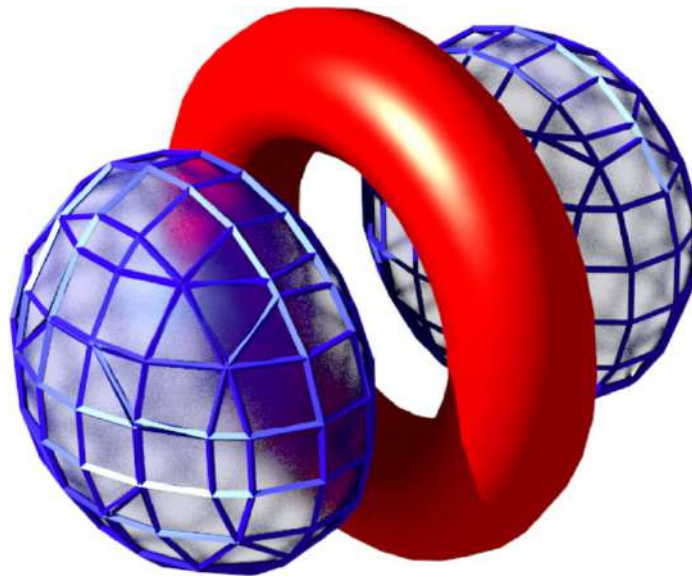
Inhomogeneous pairing



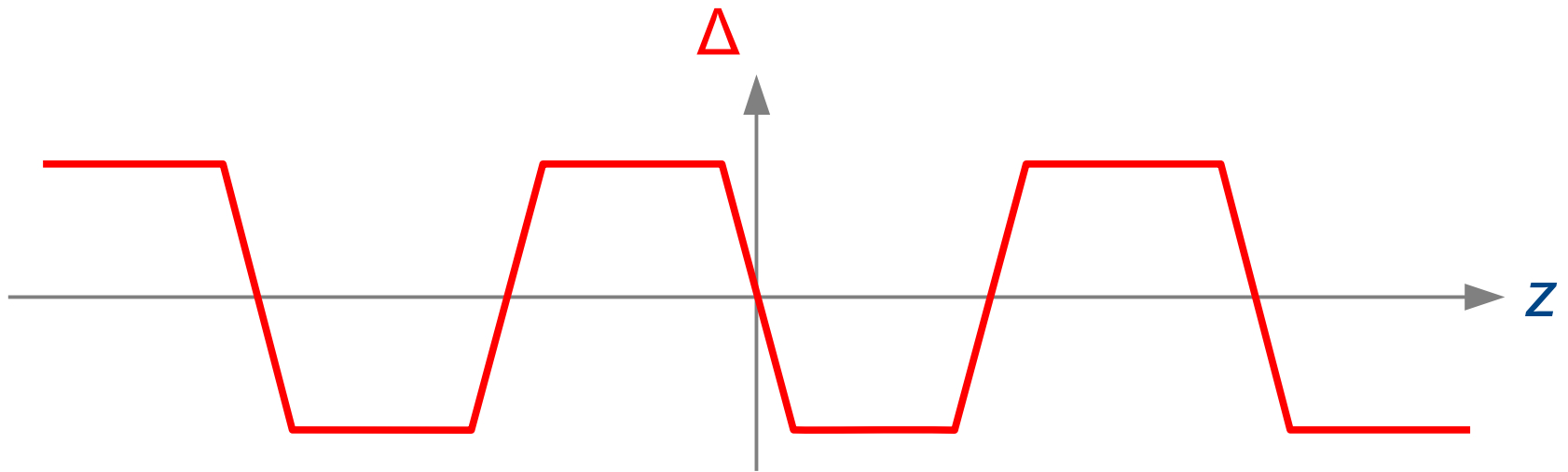
Inhomogeneous pairing



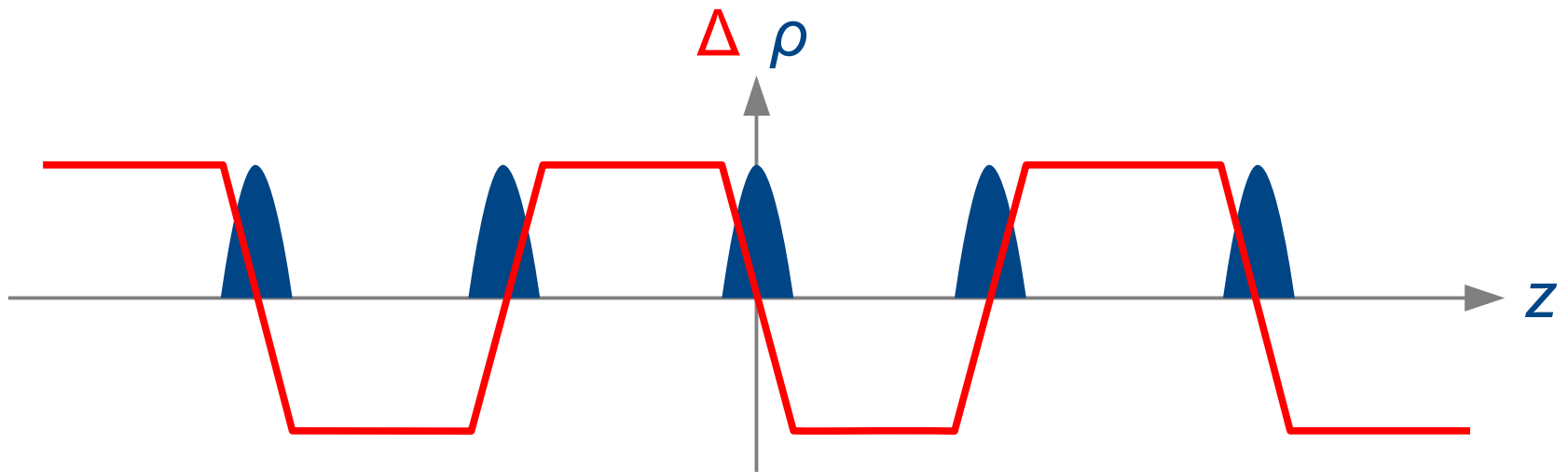
Inhomogeneous pairing



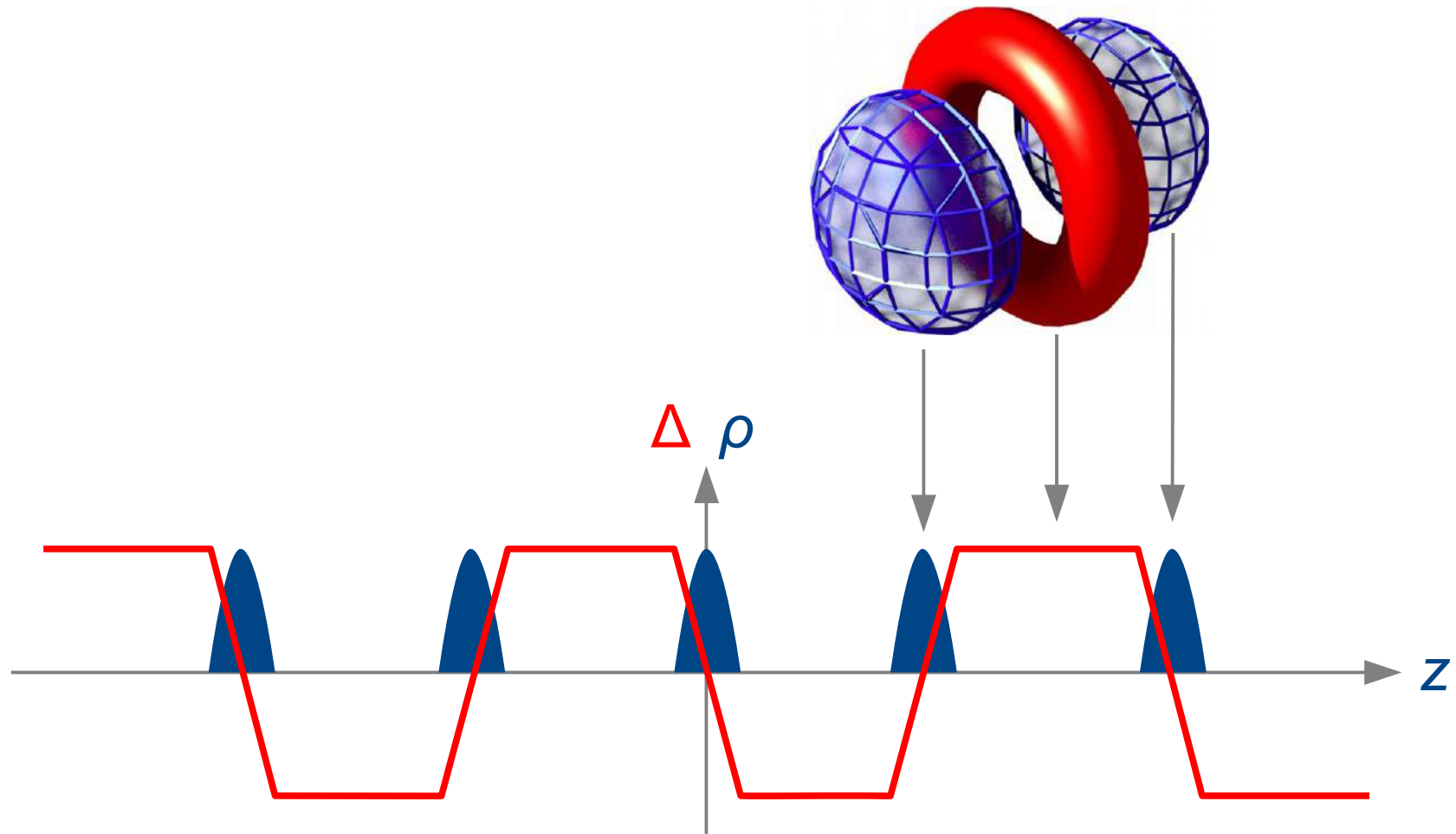
Inhomogeneous pairing



Inhomogeneous pairing



Inhomogeneous pairing

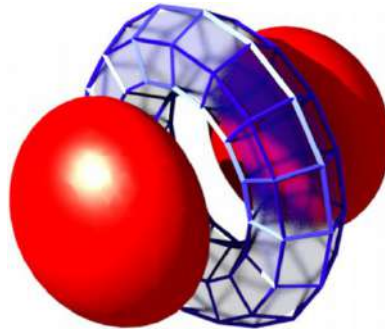


Inhomogeneous pairing

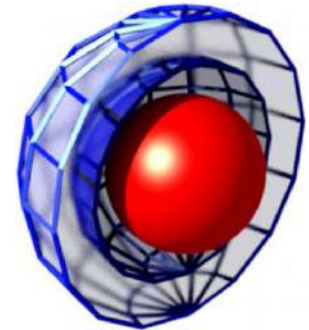
$(2,1)$ $(3,2)$ $(4,3)$



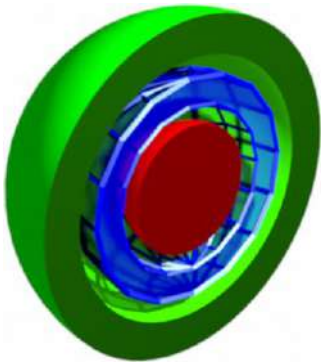
$(3,1)$ $(4,2)$



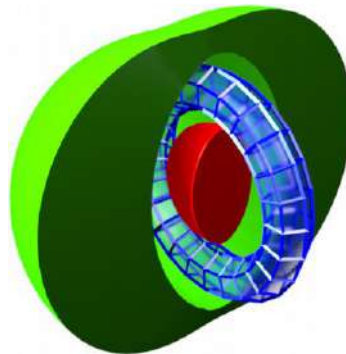
$(4,1)$



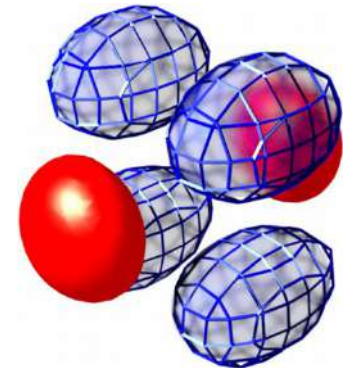
$(2,1)^s$ $(5,1)$



$(2,1)^d$ $(5,2)$

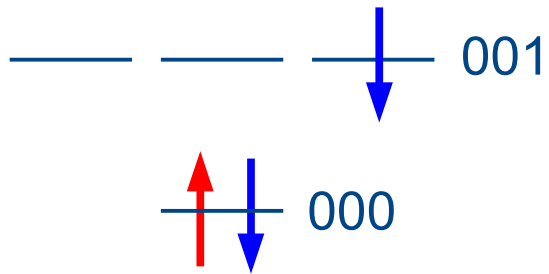


$(2,1)^g$

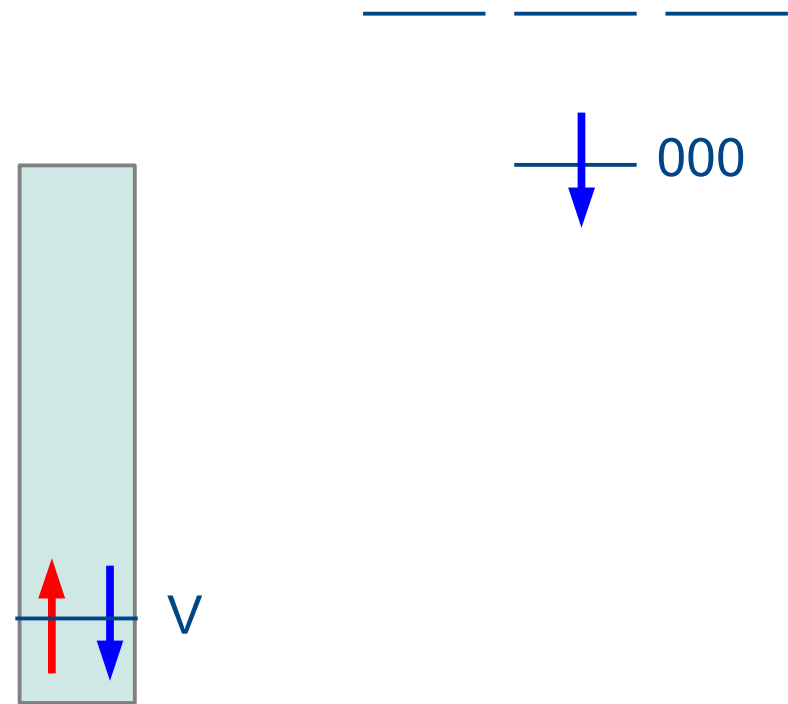


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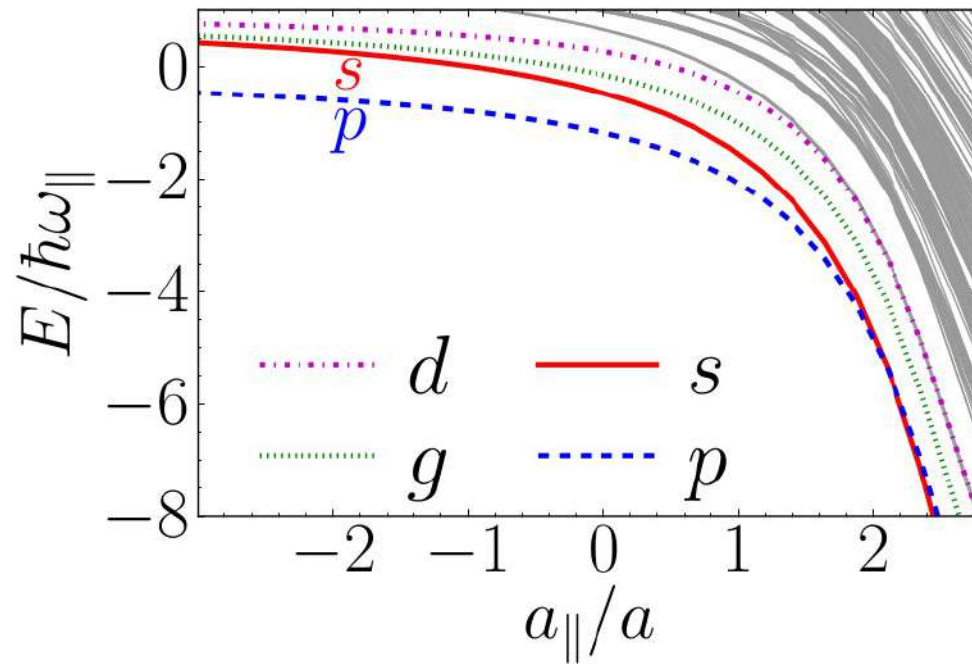
Weak interactions



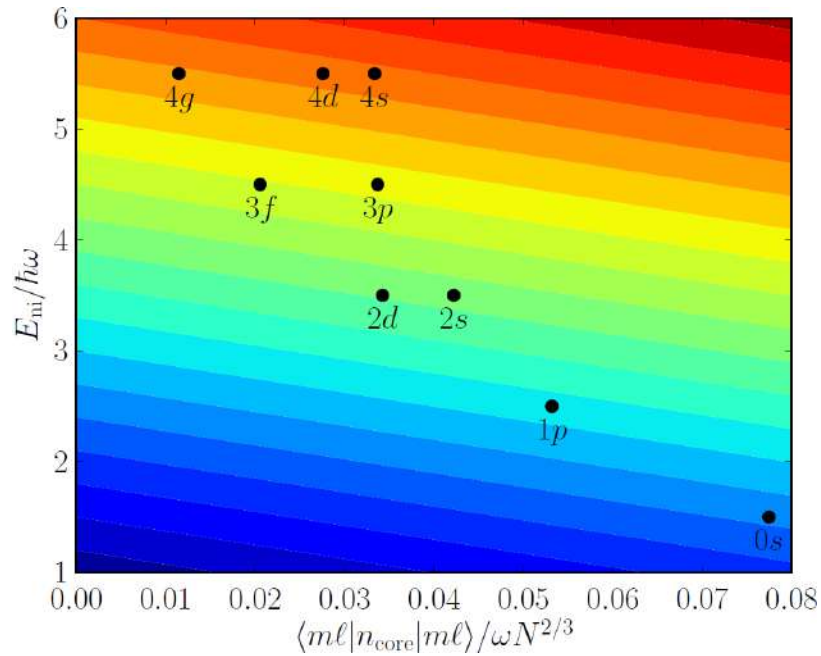
Strong interactions



Inhomogeneous pairing

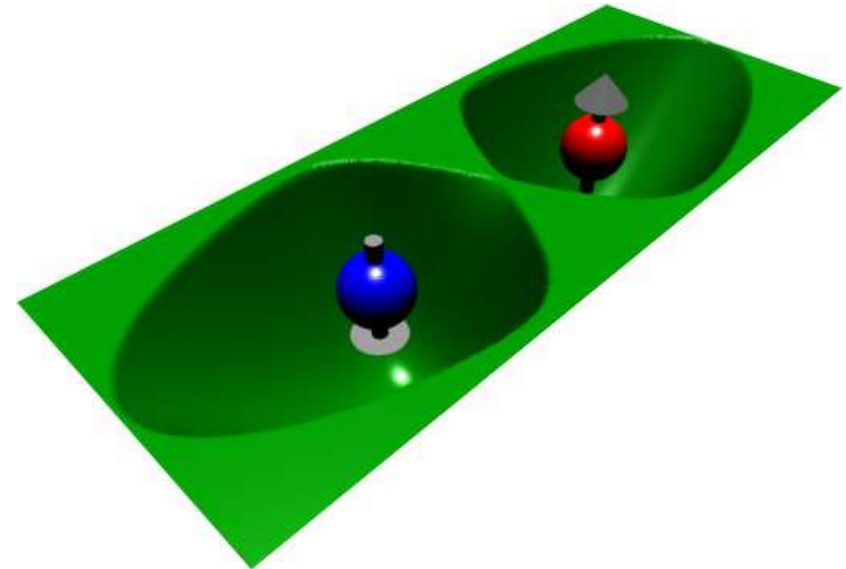


Other phenomena



Hund's rules

P.O. Bugnion, J.A. Lofthouse & GJC



Exchange interactions

P.O. Bugnion & GJC
Phys. Rev. A **88**, 013601 (2013)

Summary

A few-fermion system provides insight into many-body physics

Discretization of energy levels means that losses occur in narrow range of interaction strengths

Observation of Fermi surface and magnetic correlations