

Electric polarisation in materials

Lecture 3

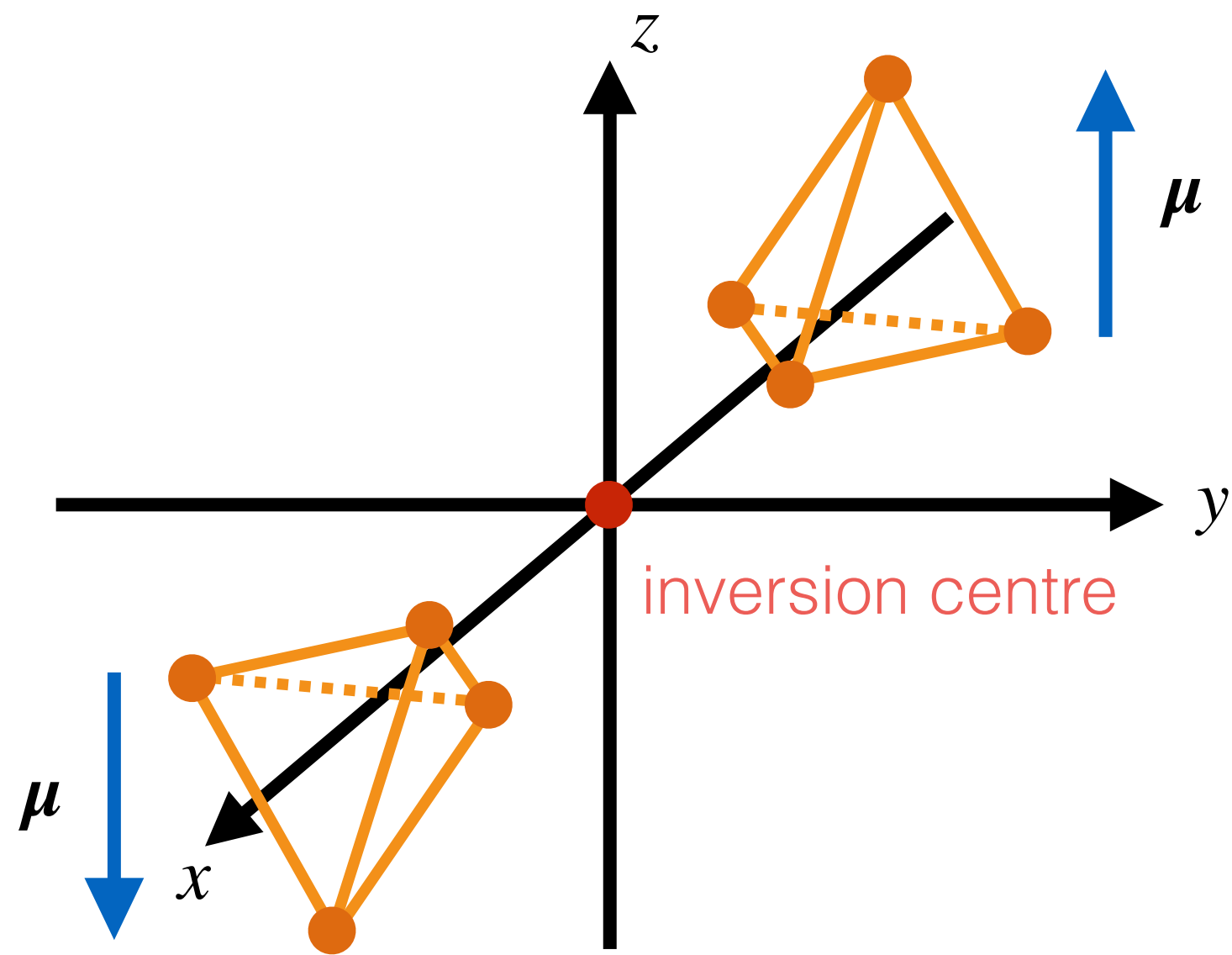
Bartomeu Monserrat
Course B: Materials for Devices

 Professor M does Science

 <http://www.tcm.phy.cam.ac.uk/~bm418/>

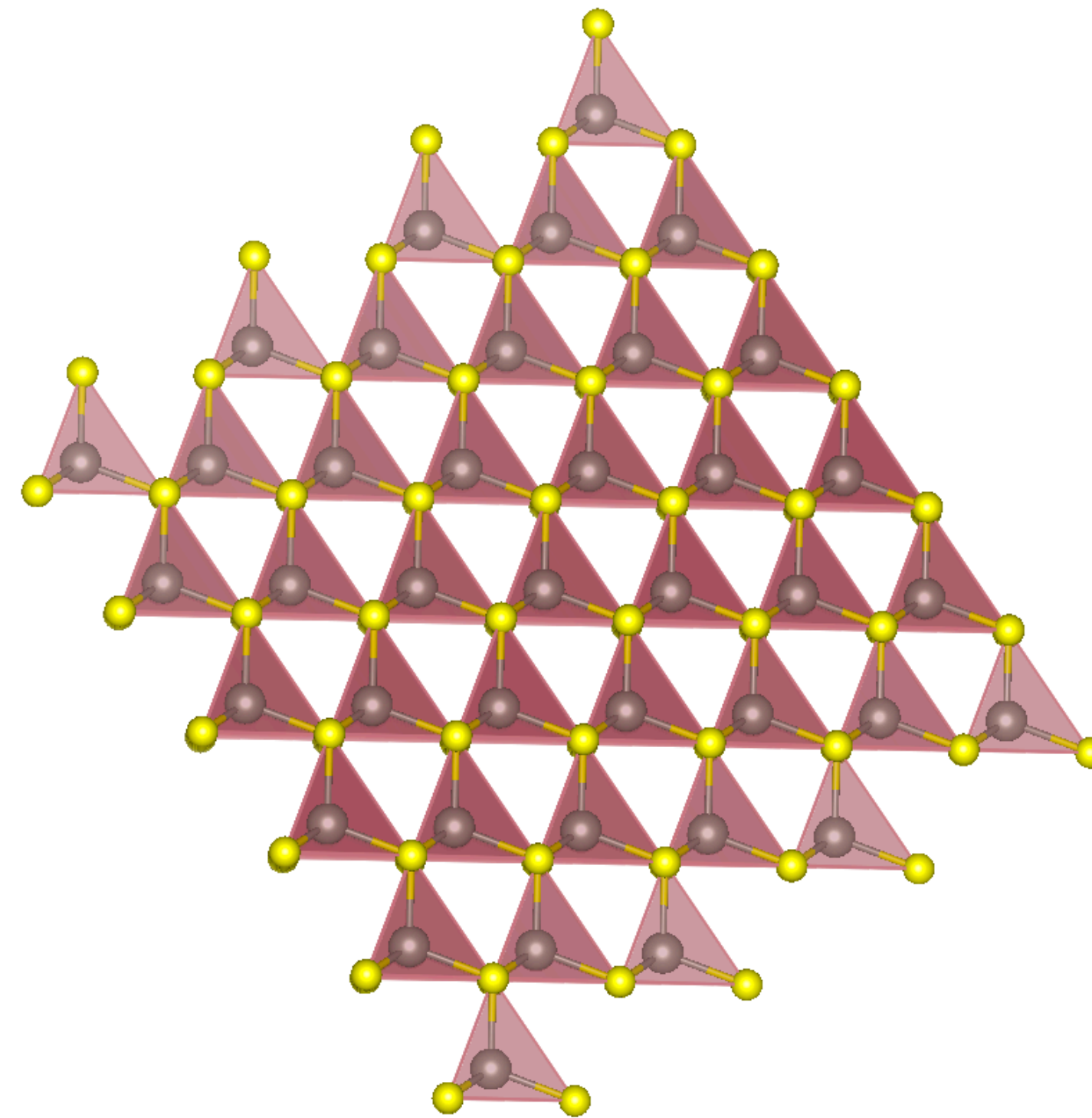
centrosymmetric crystal

non-polar

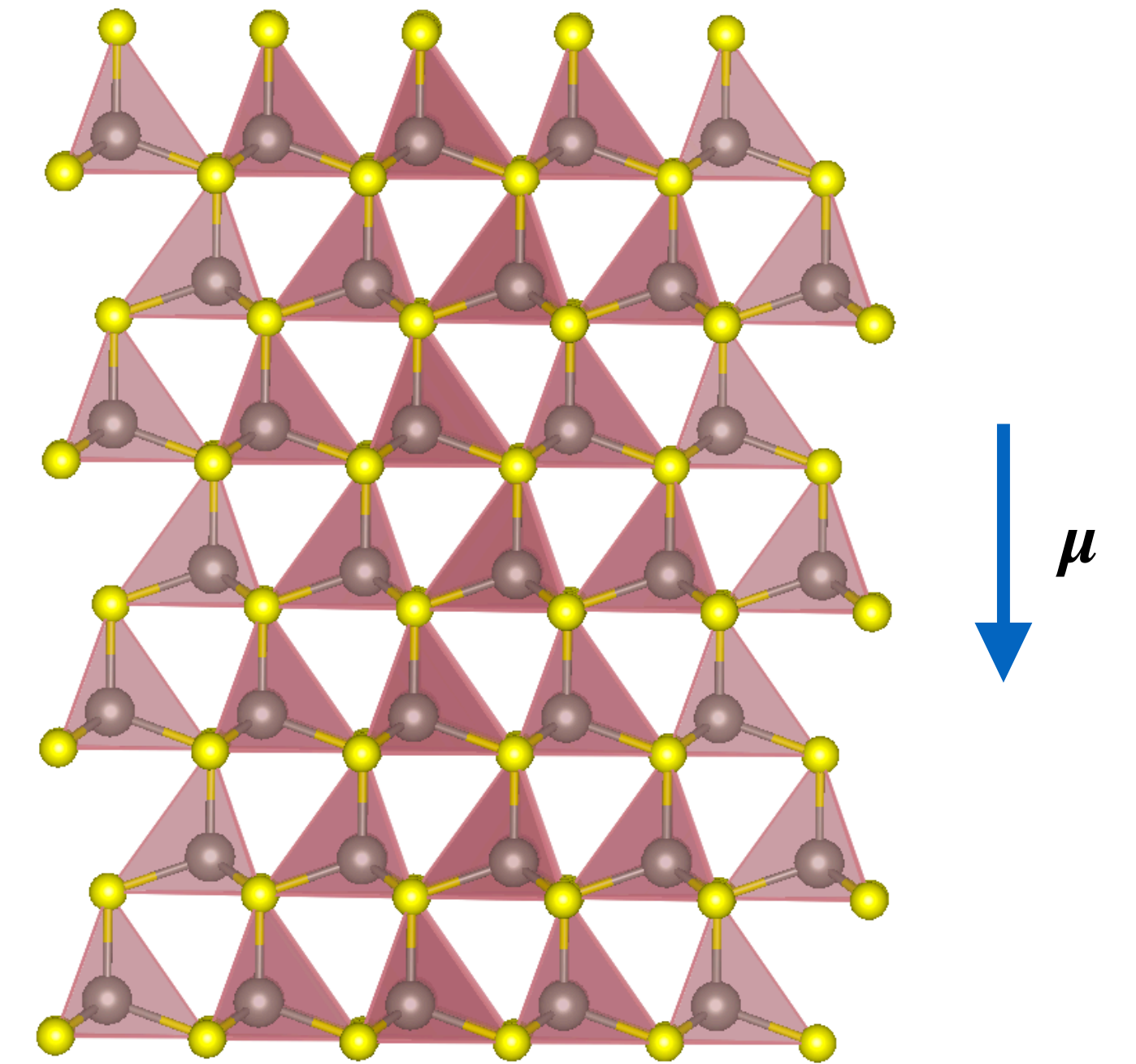


noncentrosymmetric crystal

non-polar

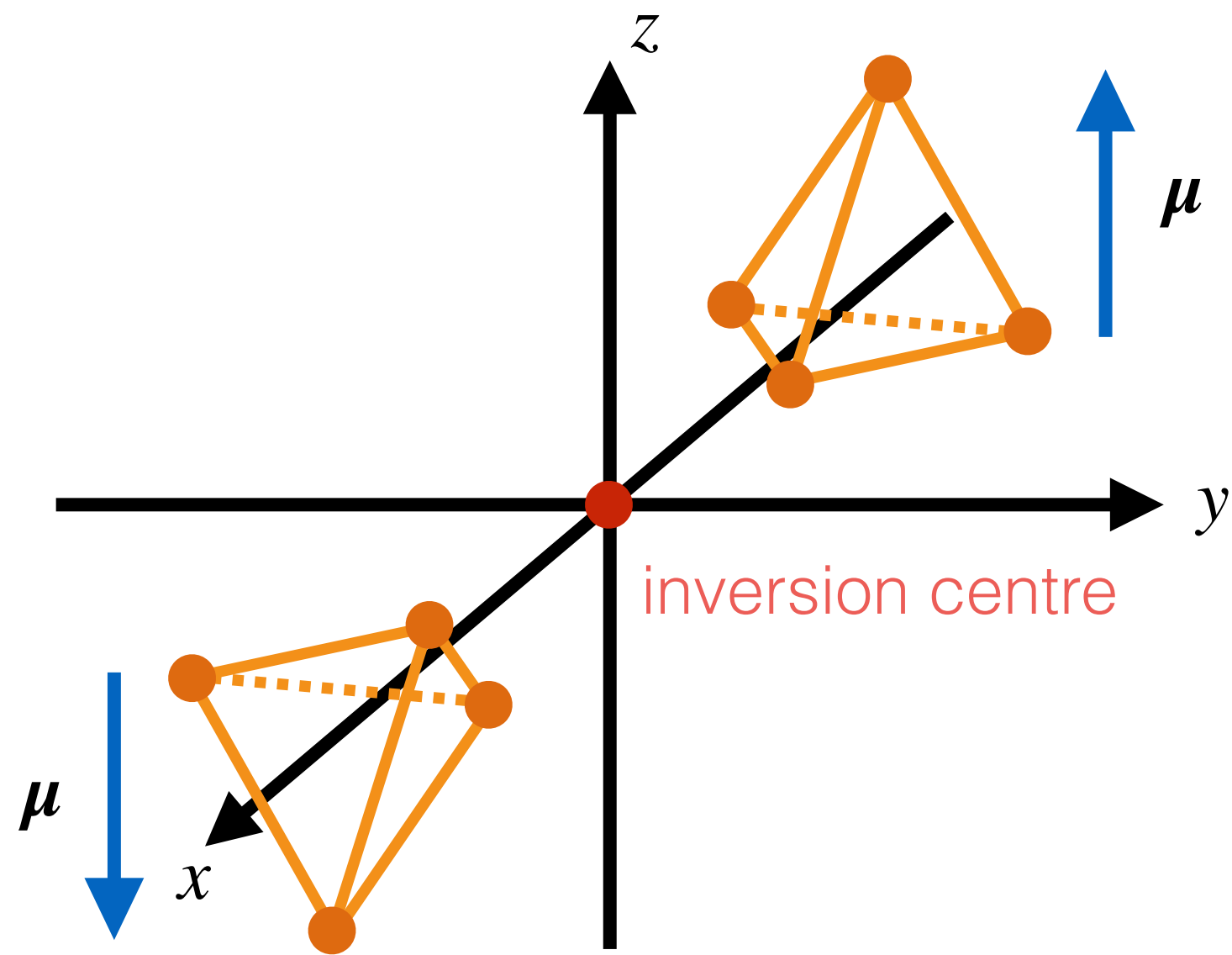


polar



centrosymmetric crystal

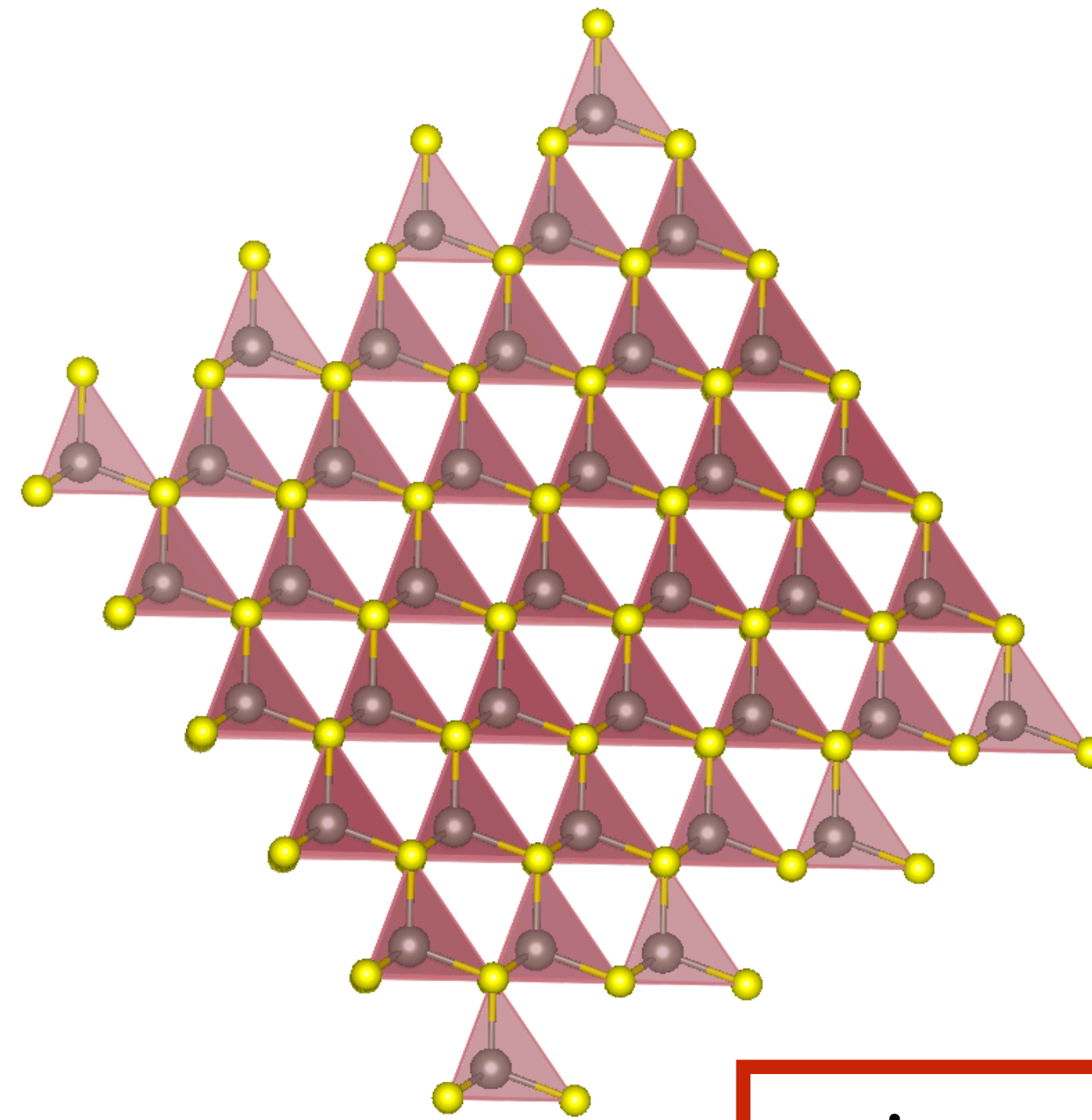
non-polar



no piezoelectricity

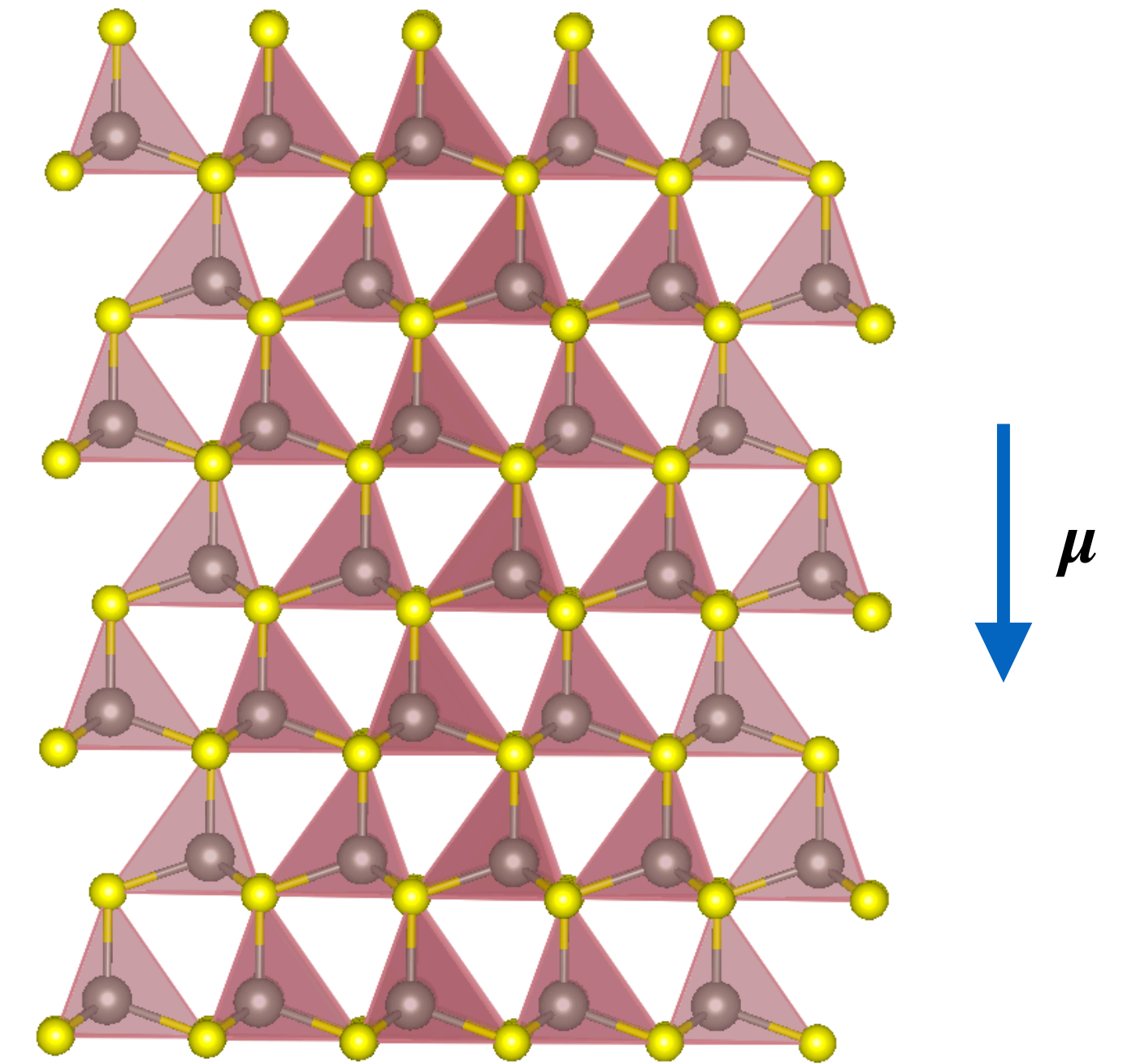
noncentrosymmetric crystal

non-polar



piezoelectricity*

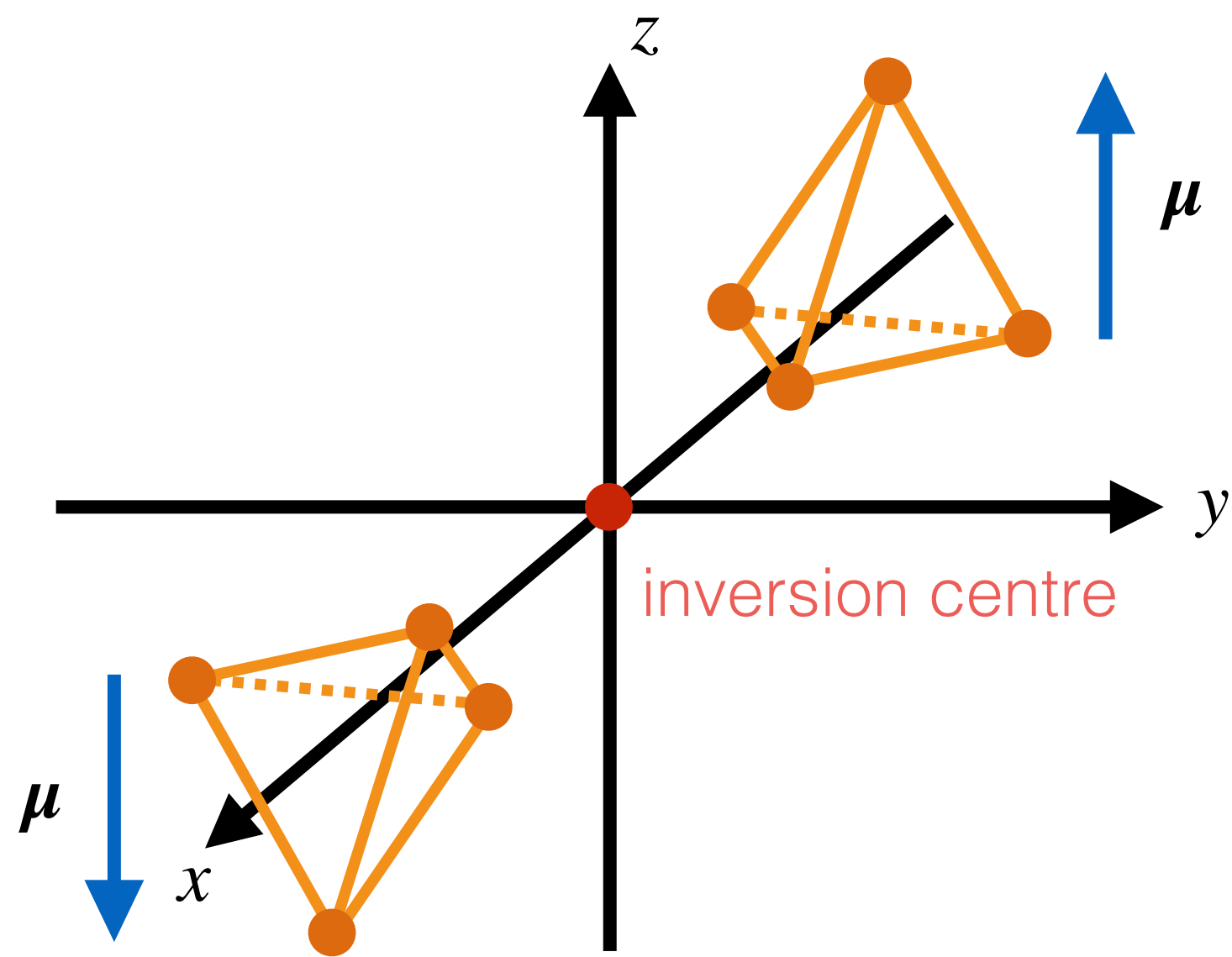
polar



* Cubic crystal class 432 exception

**centrosymmetric
crystal**

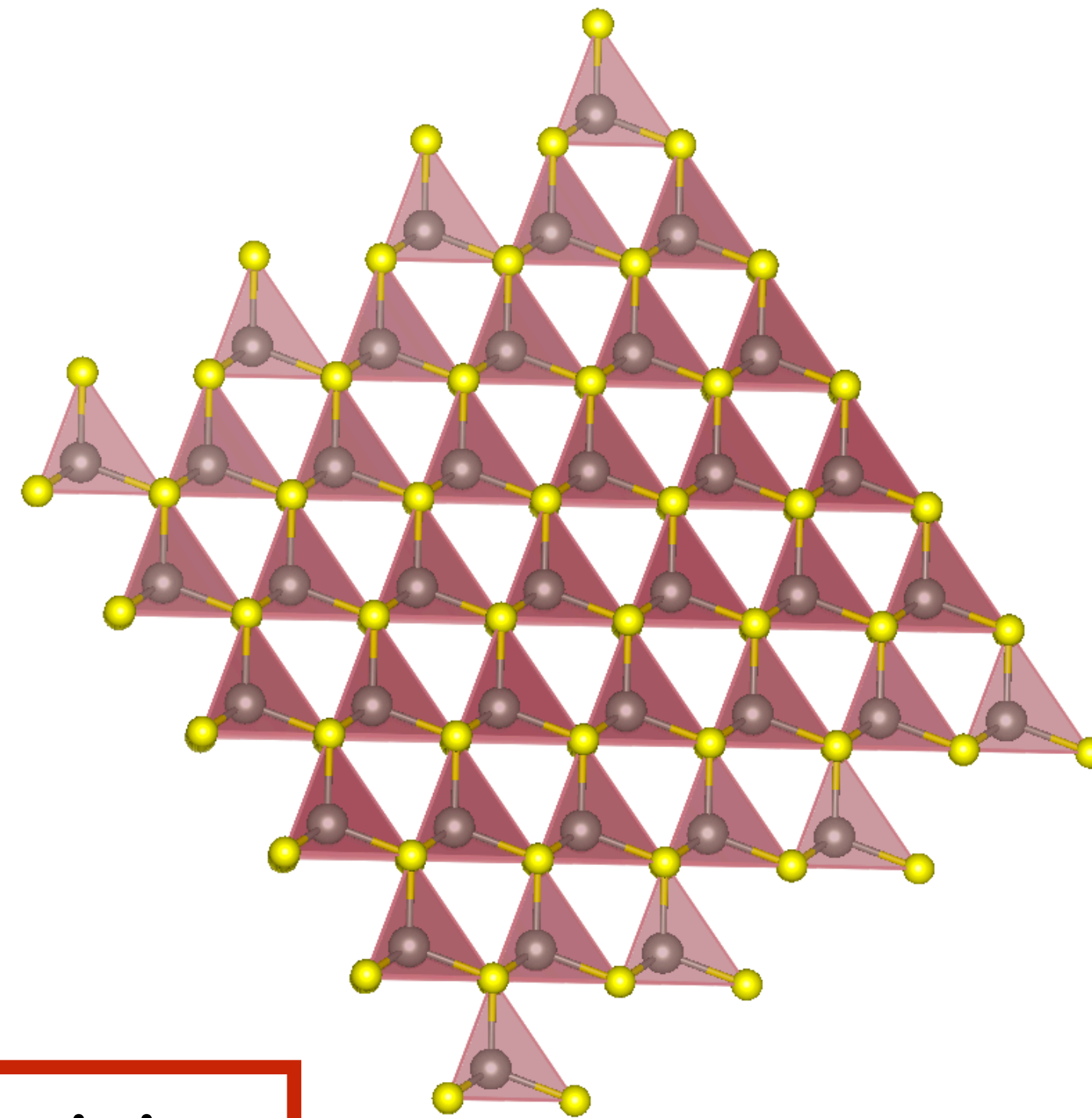
non-polar



no pyroelectricity

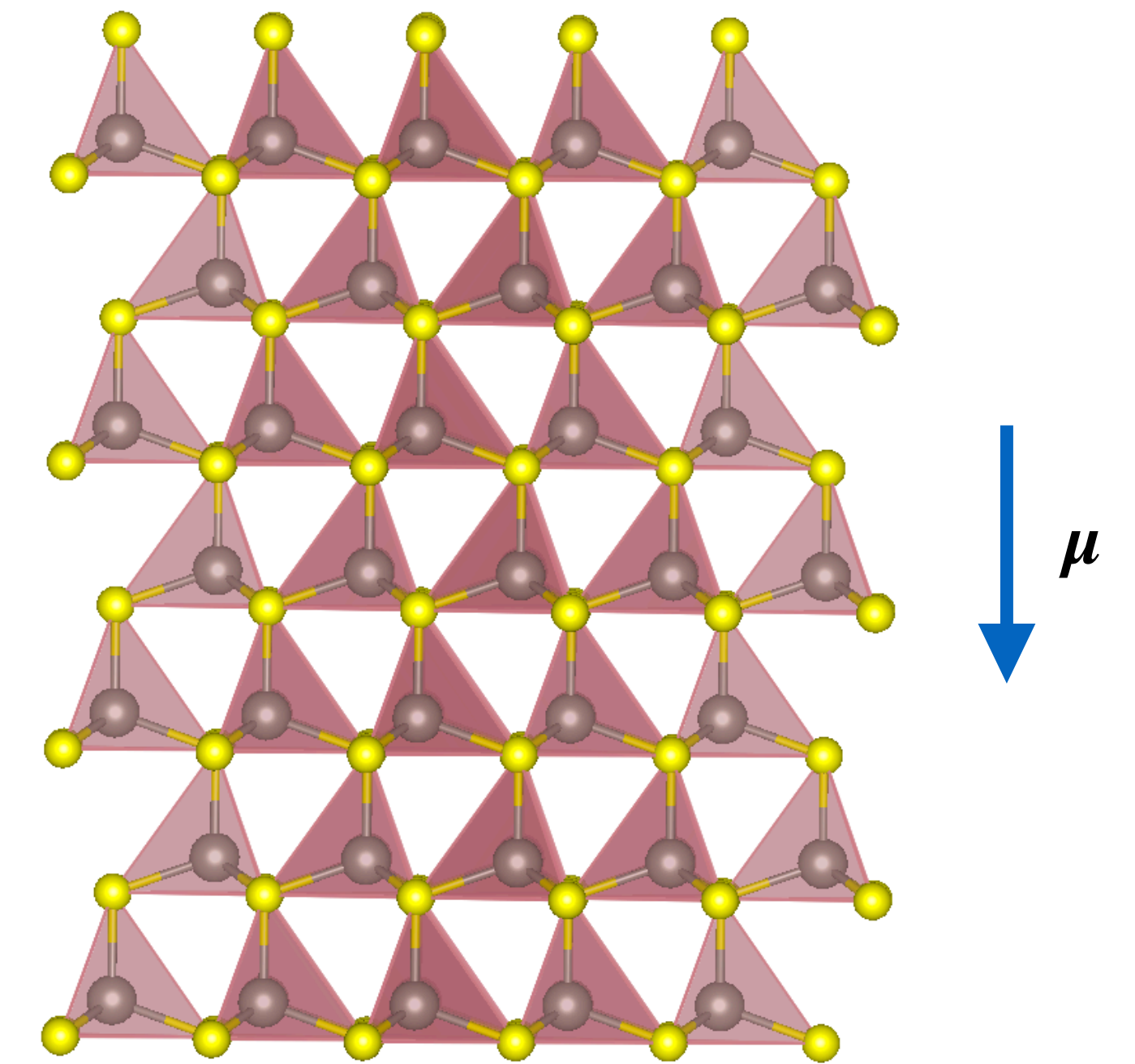
**noncentrosymmetric
crystal**

non-polar

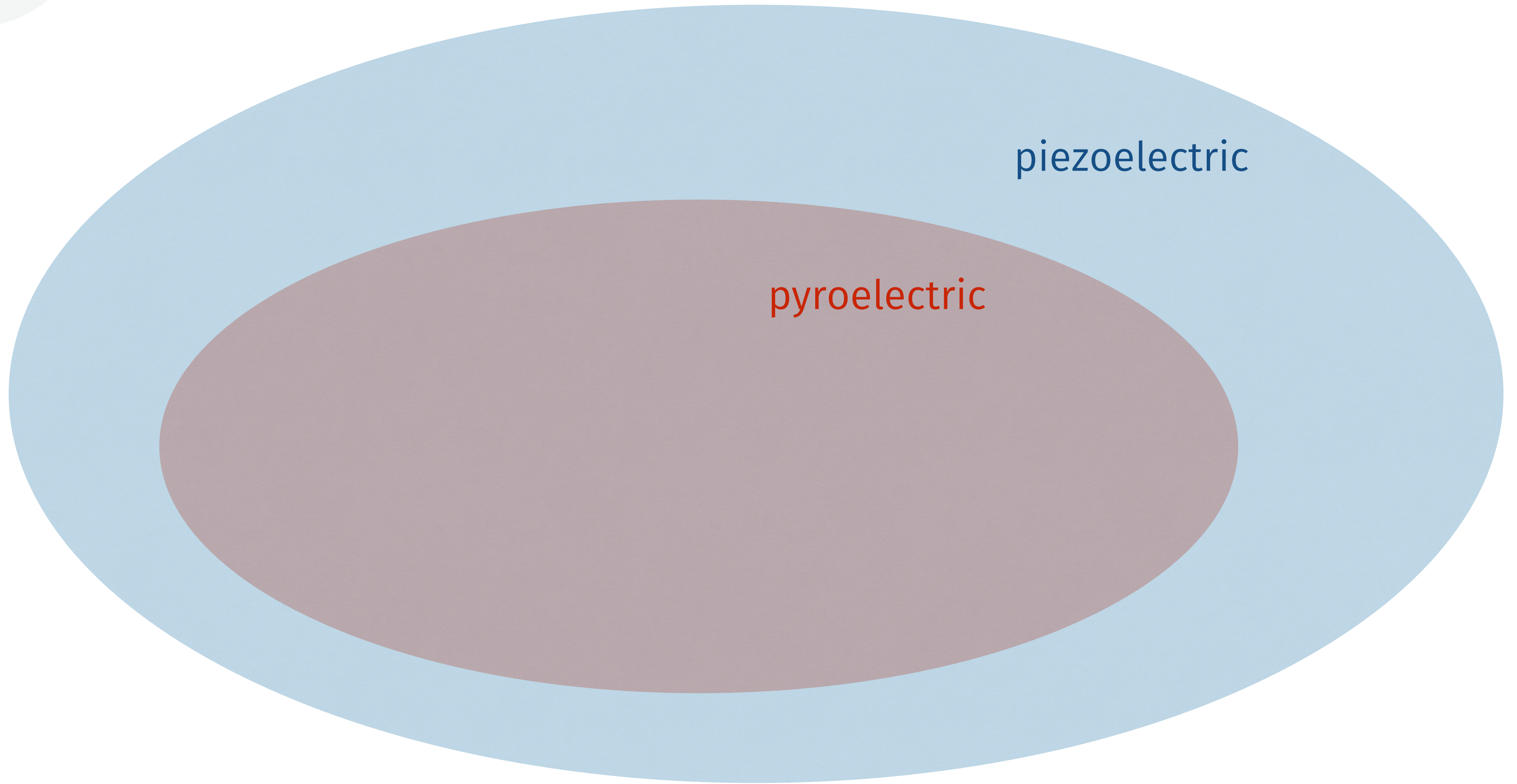
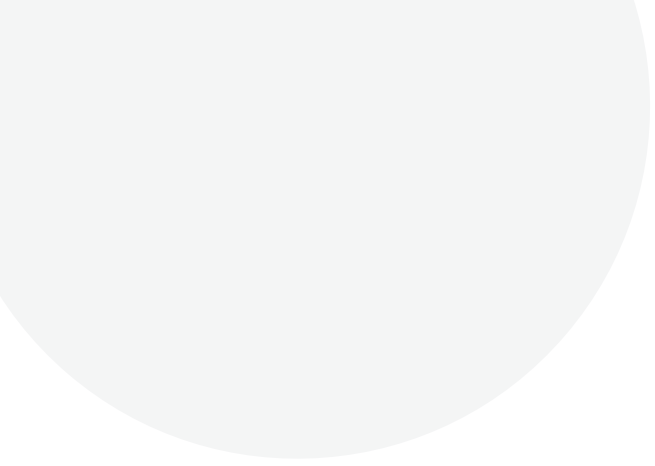


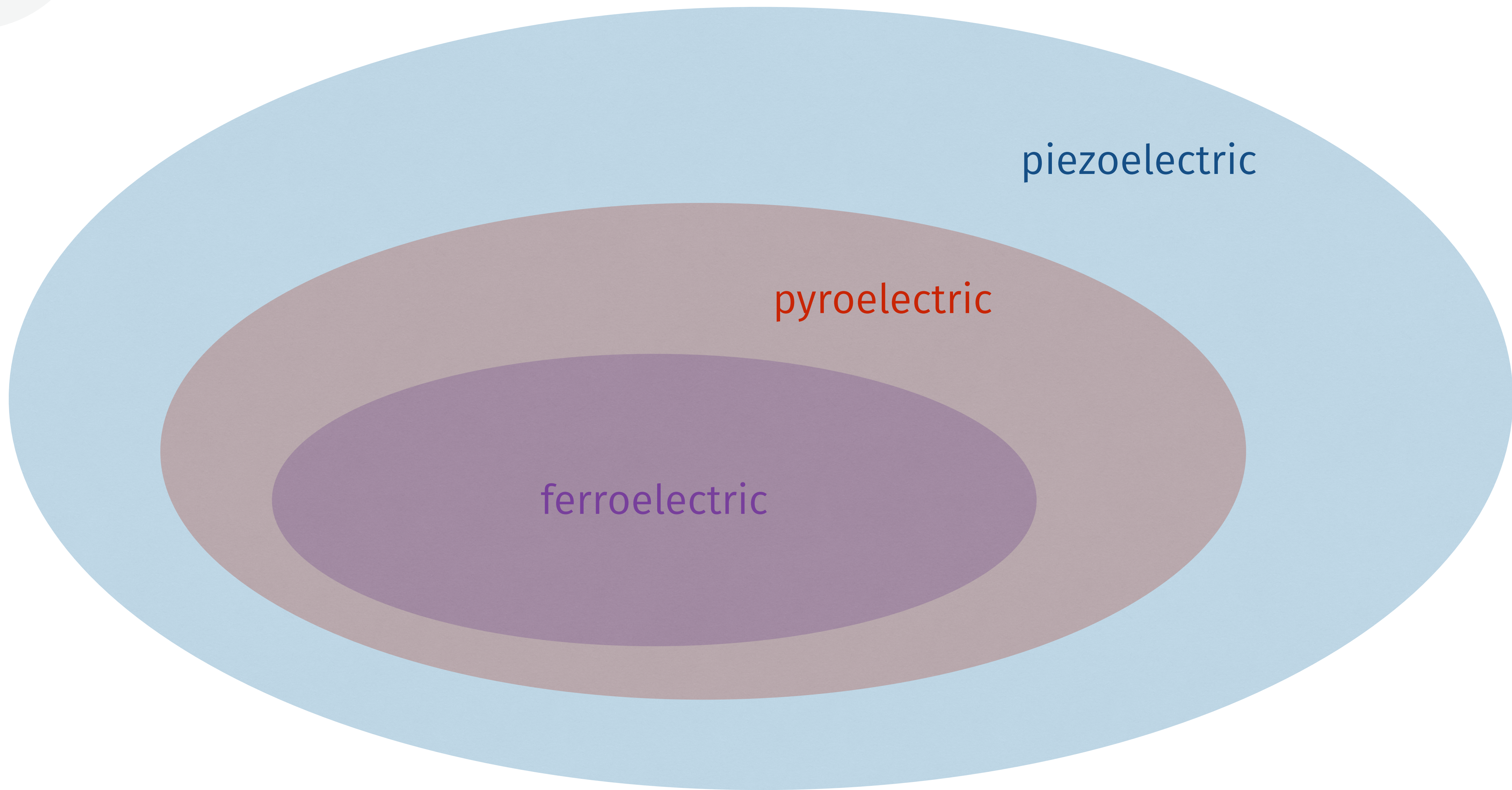
4

polar



pyroelectricity



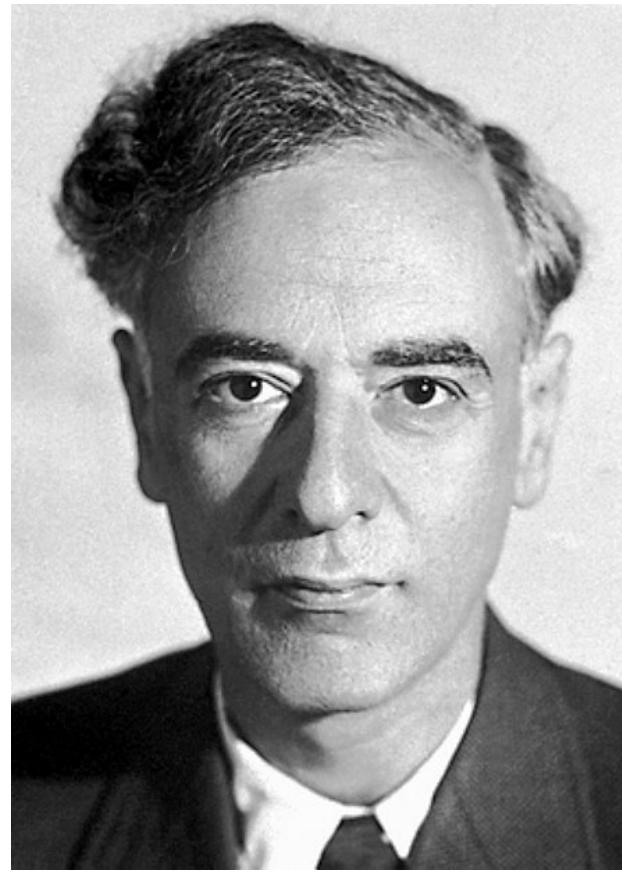


piezoelectric

pyroelectric

ferroelectric

Landau theory



Lev Landau

$$\mathcal{F}(P, T) = a(T - T_c)P^2 + \frac{b}{2}P^4 - EP$$

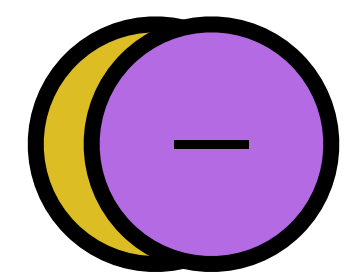


Nobel Prize in Physics 1962

“for pioneering theories for condensed matter, especially liquid helium”

Landau theory

$$\mu = 0$$



$$x = 0$$

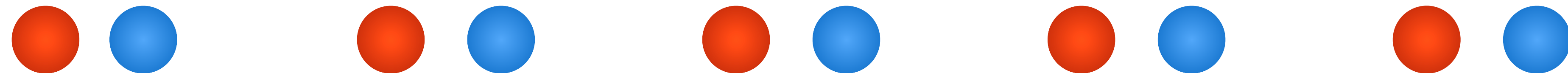
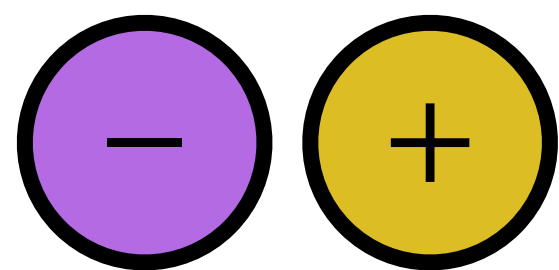
A^-

B^+

x

0

$$\mu$$

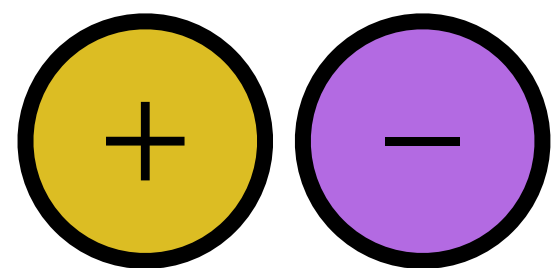


$$x < 0$$

x

0

$$\mu$$



$$x > 0$$

x

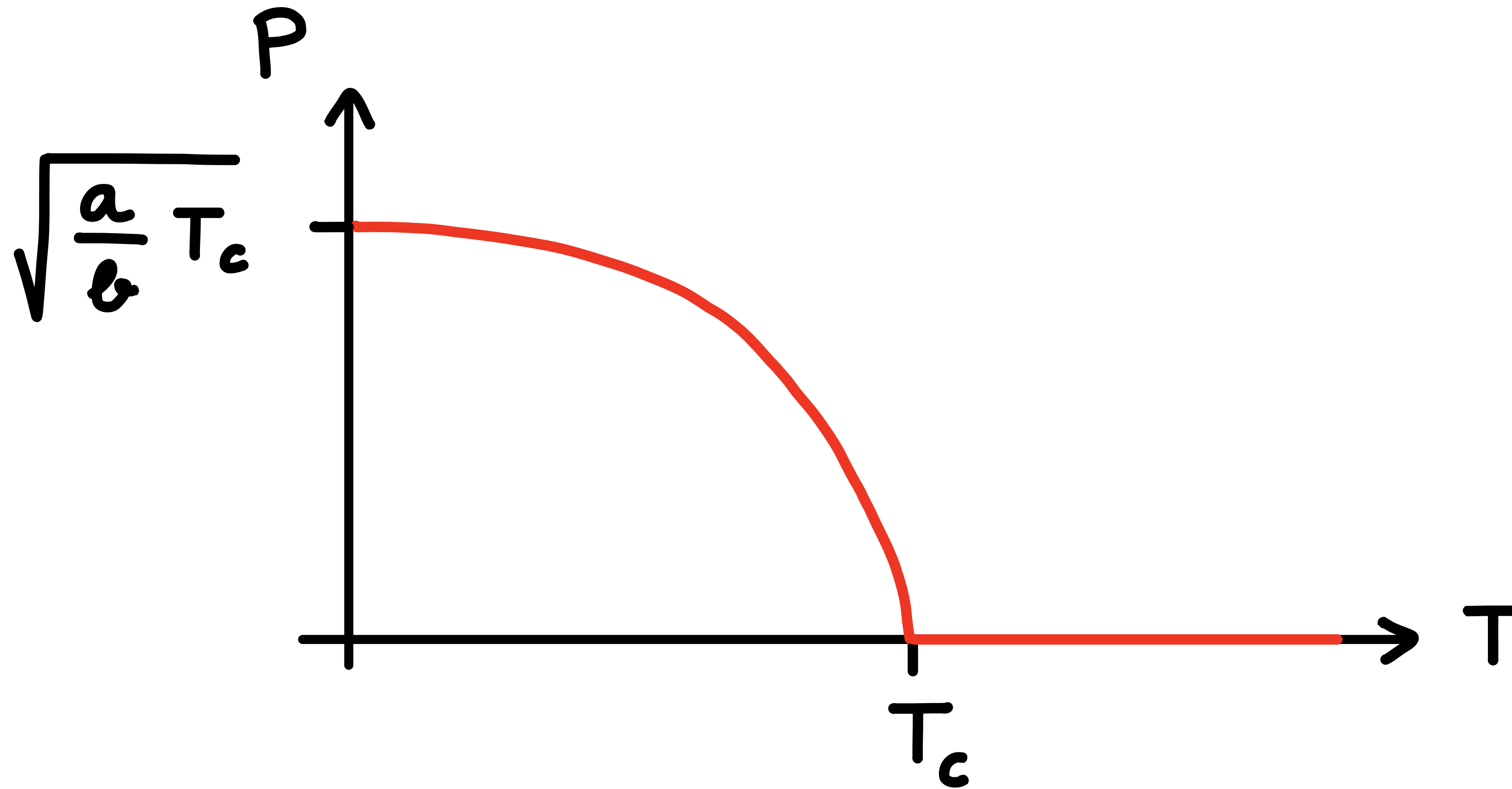
0

Landau theory

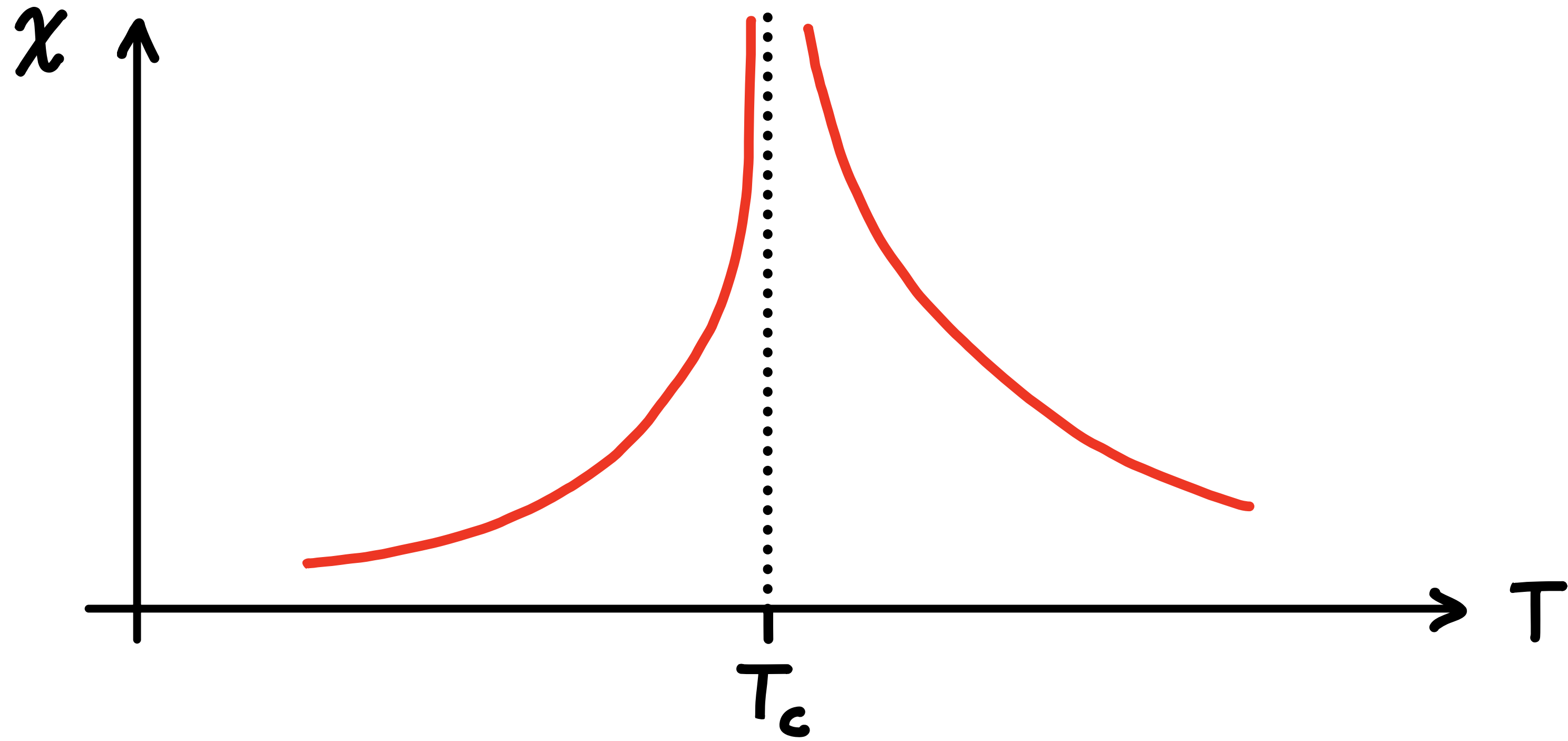
- *See discussion of Landau theory*

$$\mathcal{F}(P, T) = a(T - T_c)P^2 + \frac{b}{2}P^4 - EP$$

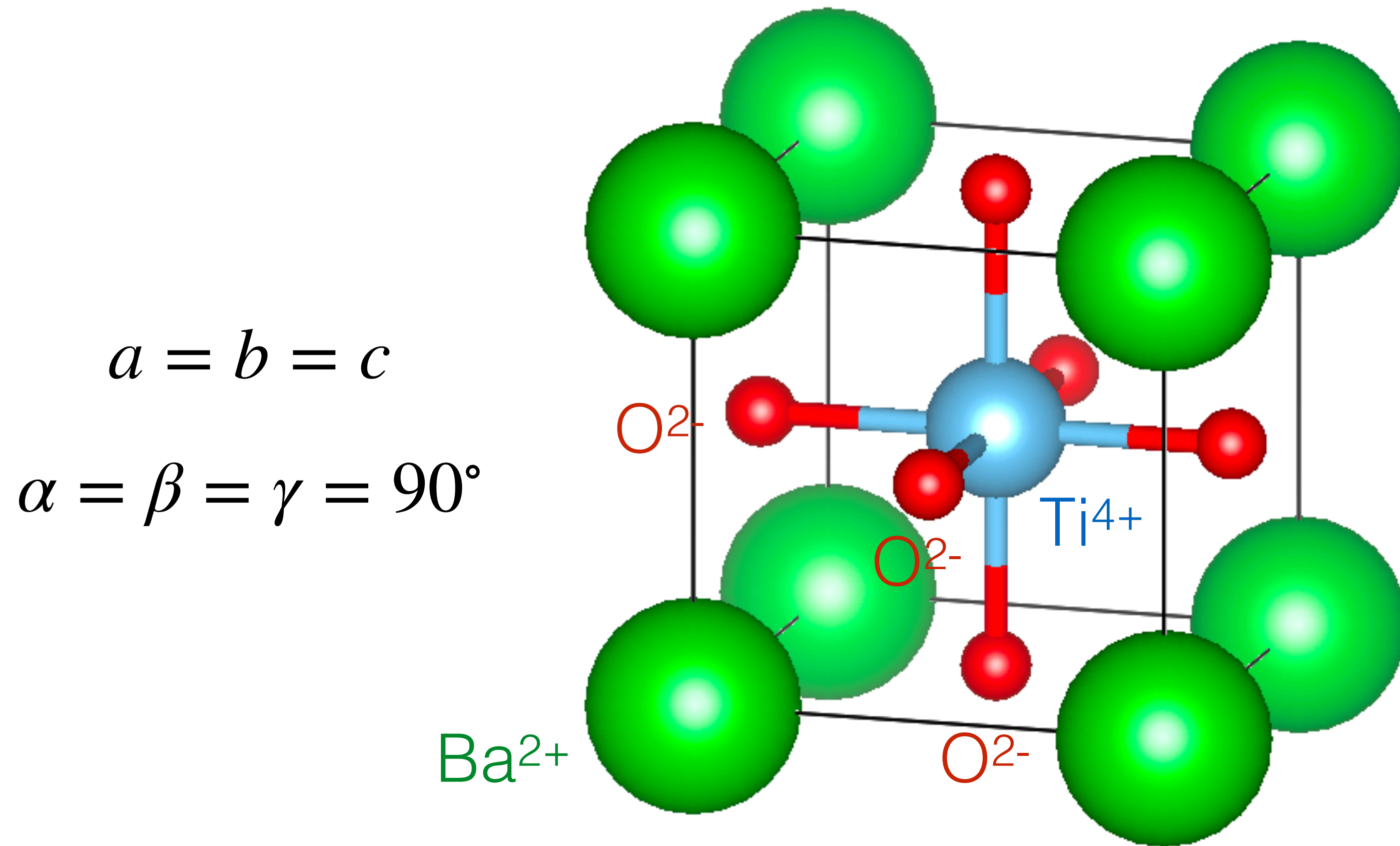
Landau theory



Landau theory



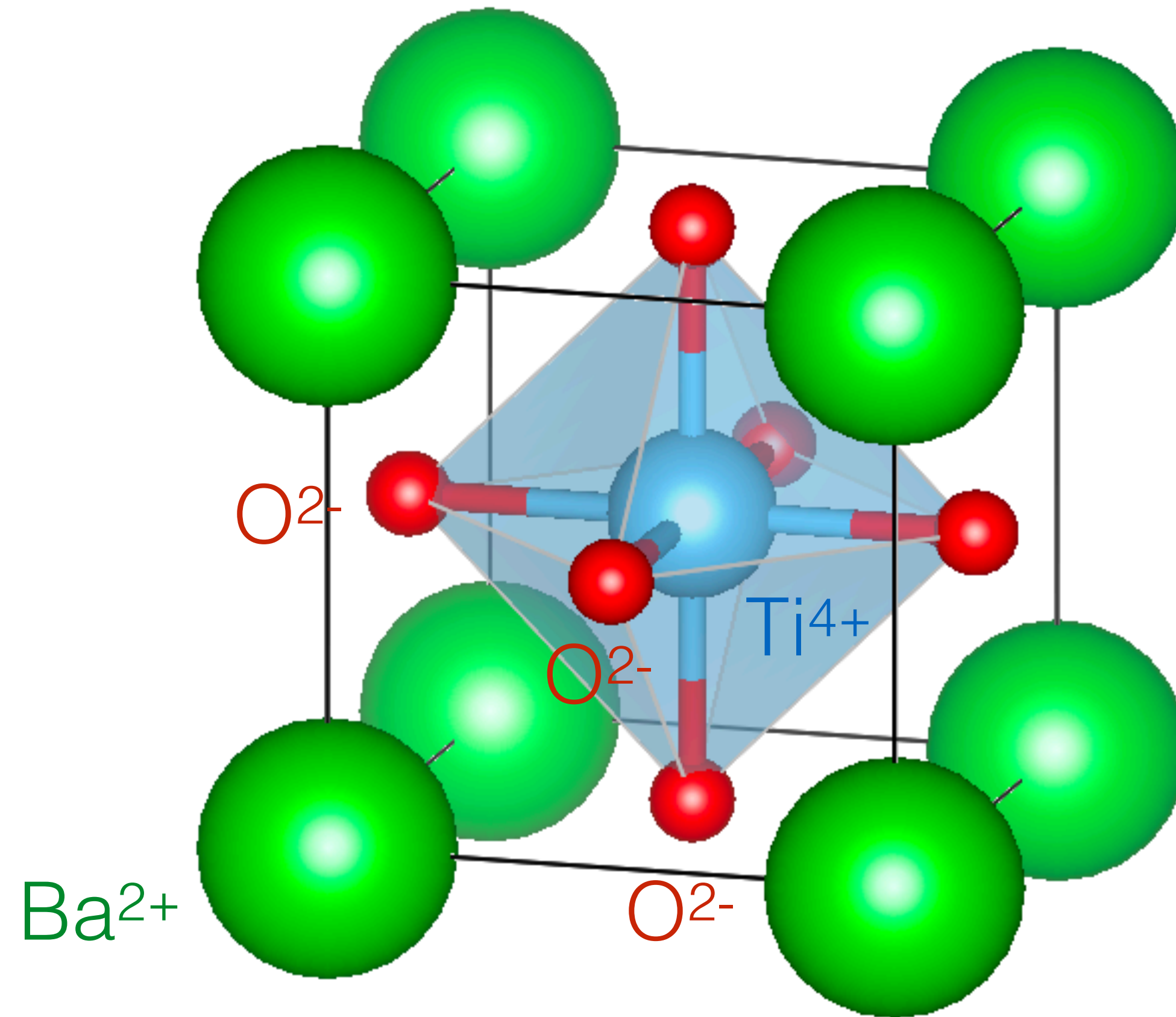
Perovskite structure ABX_3



- ▶ $BaTiO_3$
- ▶ Cubic
- ▶ Five-atom basis
- ▶ Centrosymmetric
- ▶ Course A

▶ *See structure model in 3D*

Perovskite structure ABX_3



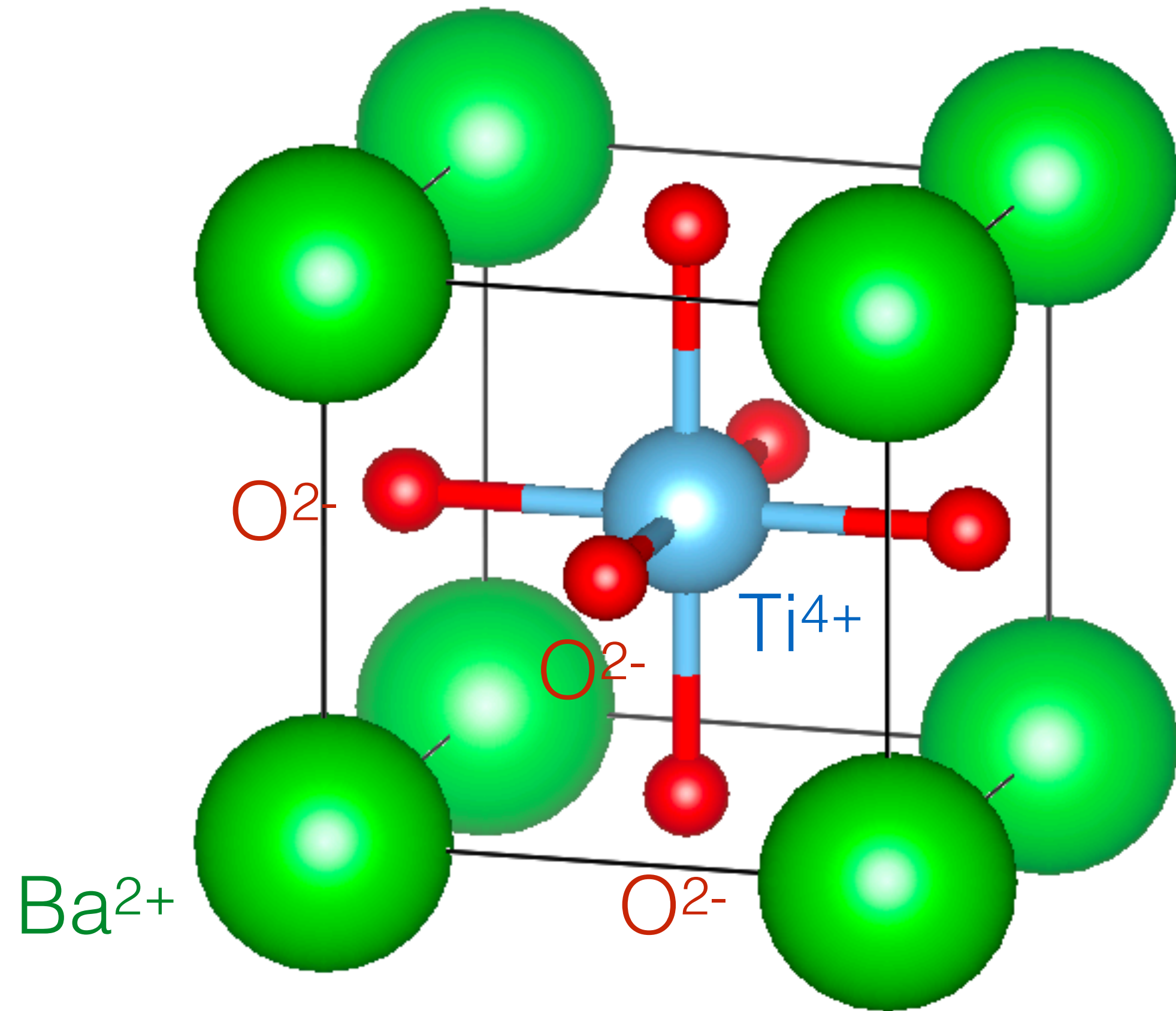
- ▶ $BaTiO_3$
- ▶ Cubic
- ▶ Five-atom basis
- ▶ Centrosymmetric
- ▶ Course A

Goldschmidt tolerance factor for ABX_3 perovskite

- *See Problem 3*

$$t = \frac{r_A + r_X}{\sqrt{2}(r_B + r_X)}$$

Goldschmidt tolerance factor for BaTiO₃ perovskite



$$t = \frac{r_A + r_X}{\sqrt{2}(r_B + r_X)}$$

$$r_A = r_{\text{Ba}^{2+}} = 1.75 \text{ \AA}$$

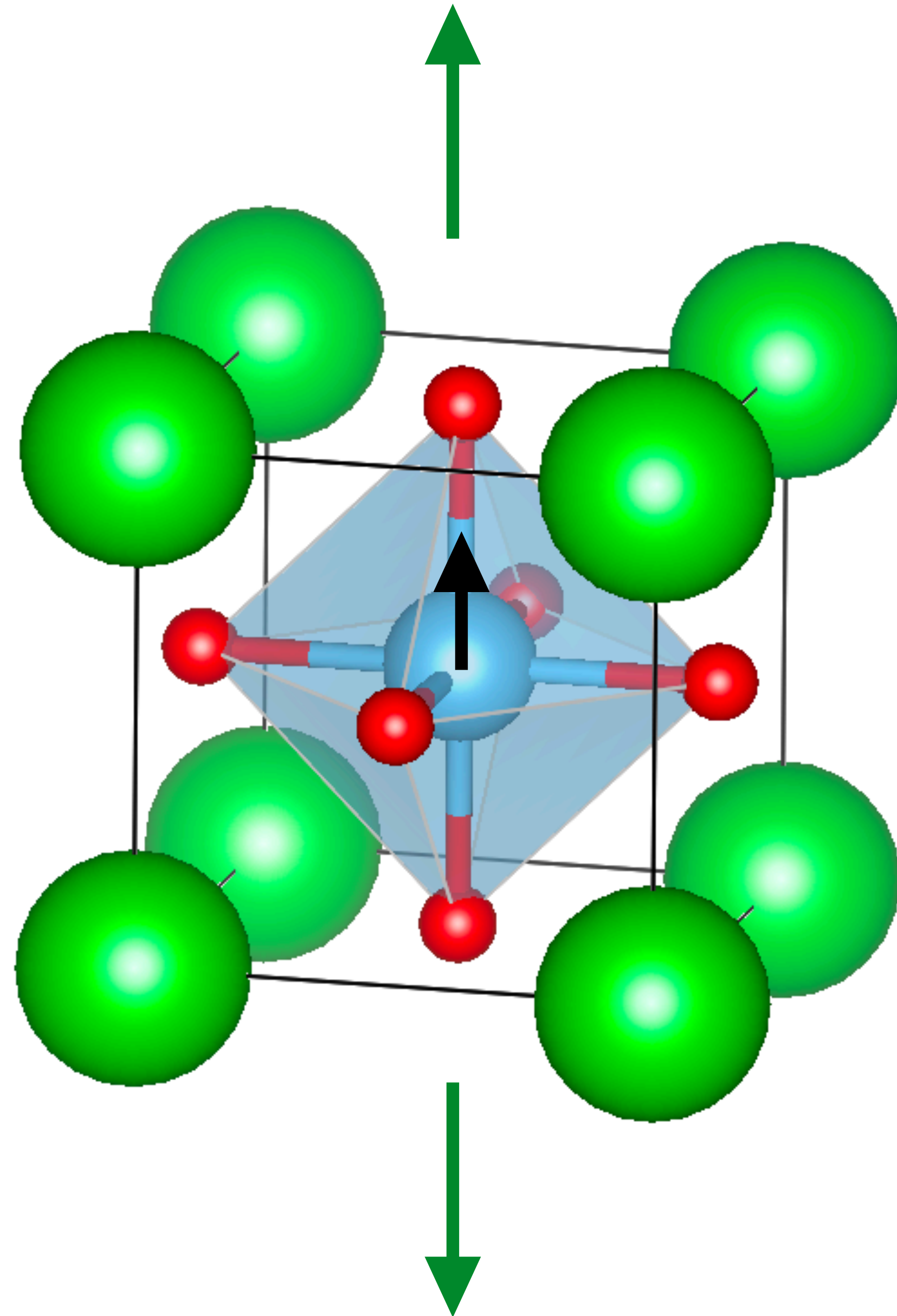
$$r_B = r_{\text{Ti}^{4+}} = 0.75 \text{ \AA}$$

$$r_X = r_{\text{O}^{2-}} = 1.21 \text{ \AA}$$

$$t = \frac{r_{\text{Ba}^{2+}} + r_{\text{O}^{2-}}}{\sqrt{2}(r_{\text{Ti}^{4+}} + r_{\text{O}^{2-}})} \simeq 1.07$$

Perovskite structure ABO_3

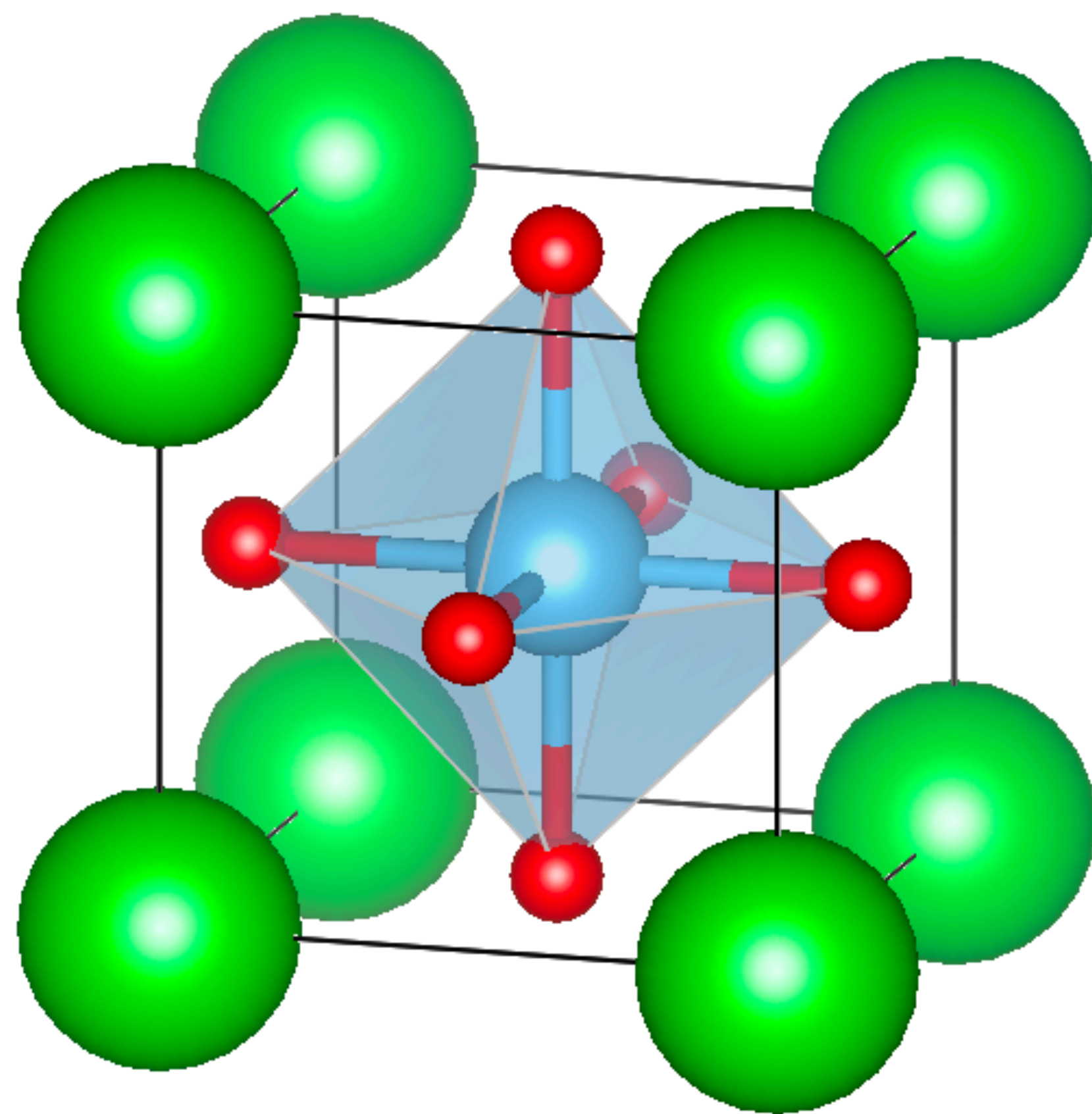
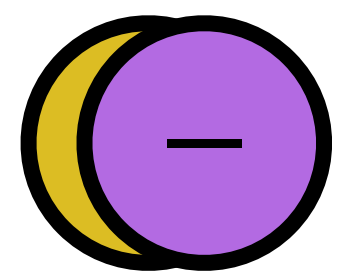
$$a = b < c$$
$$\alpha = \beta = \gamma = 90^\circ$$



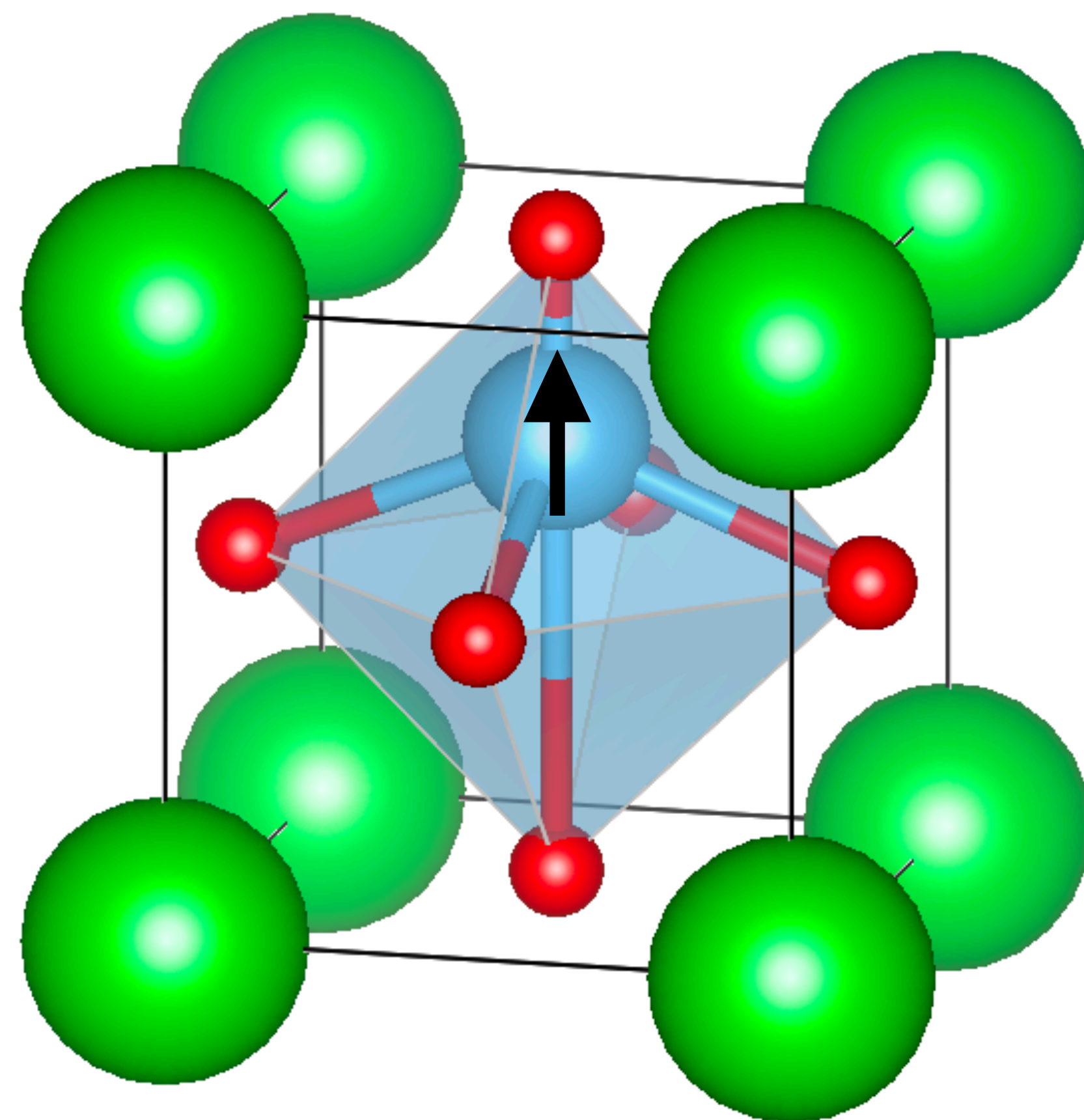
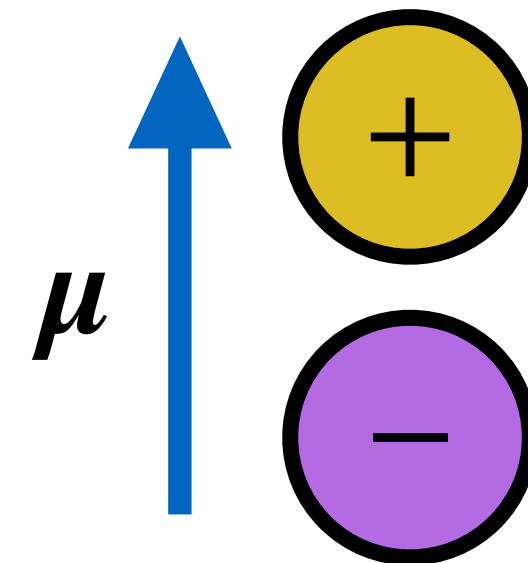
- ▶ $BaTiO_3$
- ▶ Tetragonal
- ▶ Five-atom basis
- ▶ Non-centrosymmetric

Perovskite structure ABO_3

$$\mu = 0$$



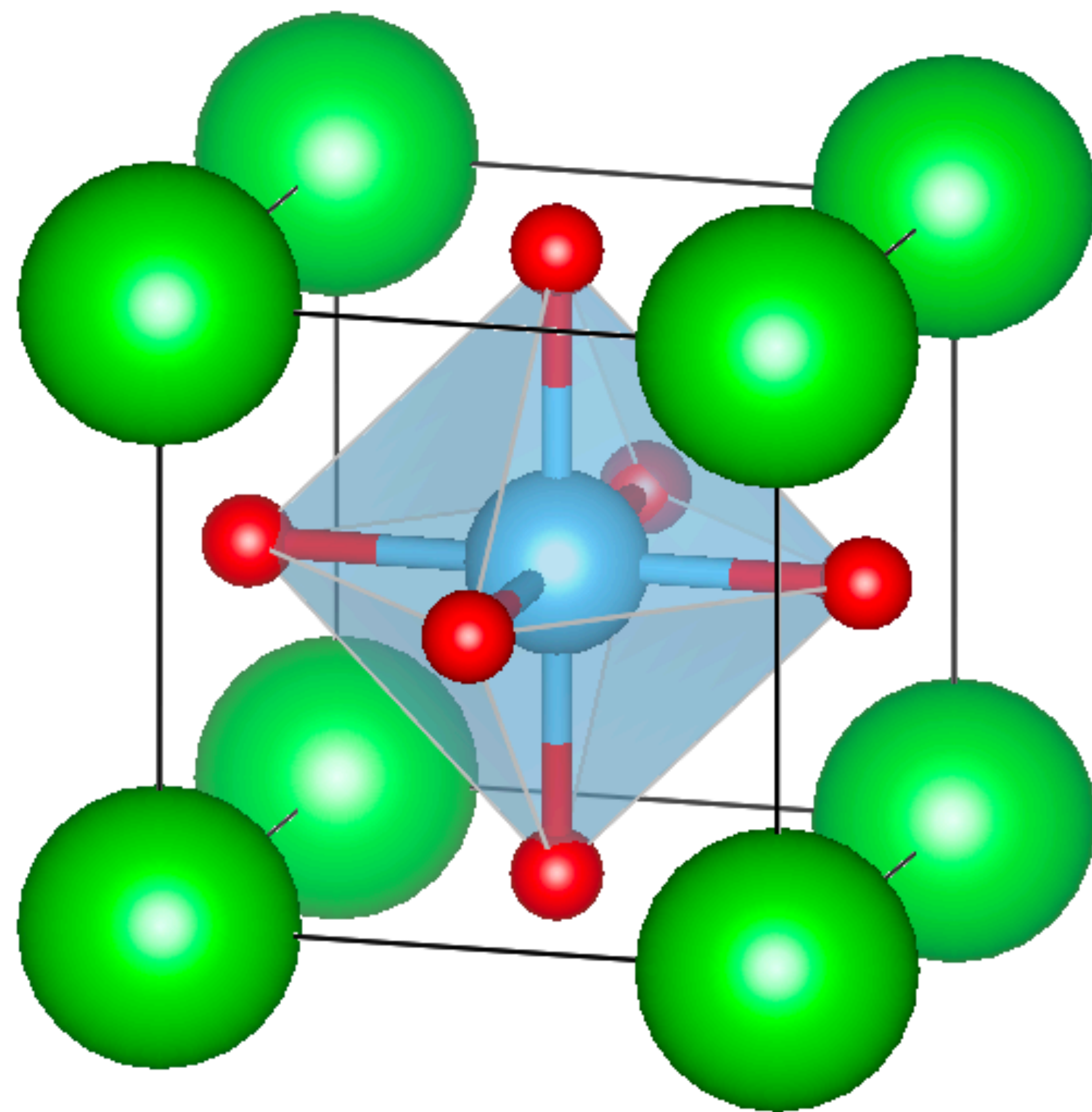
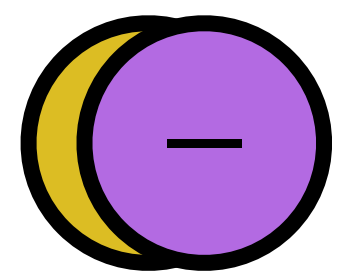
cubic



tetragonal

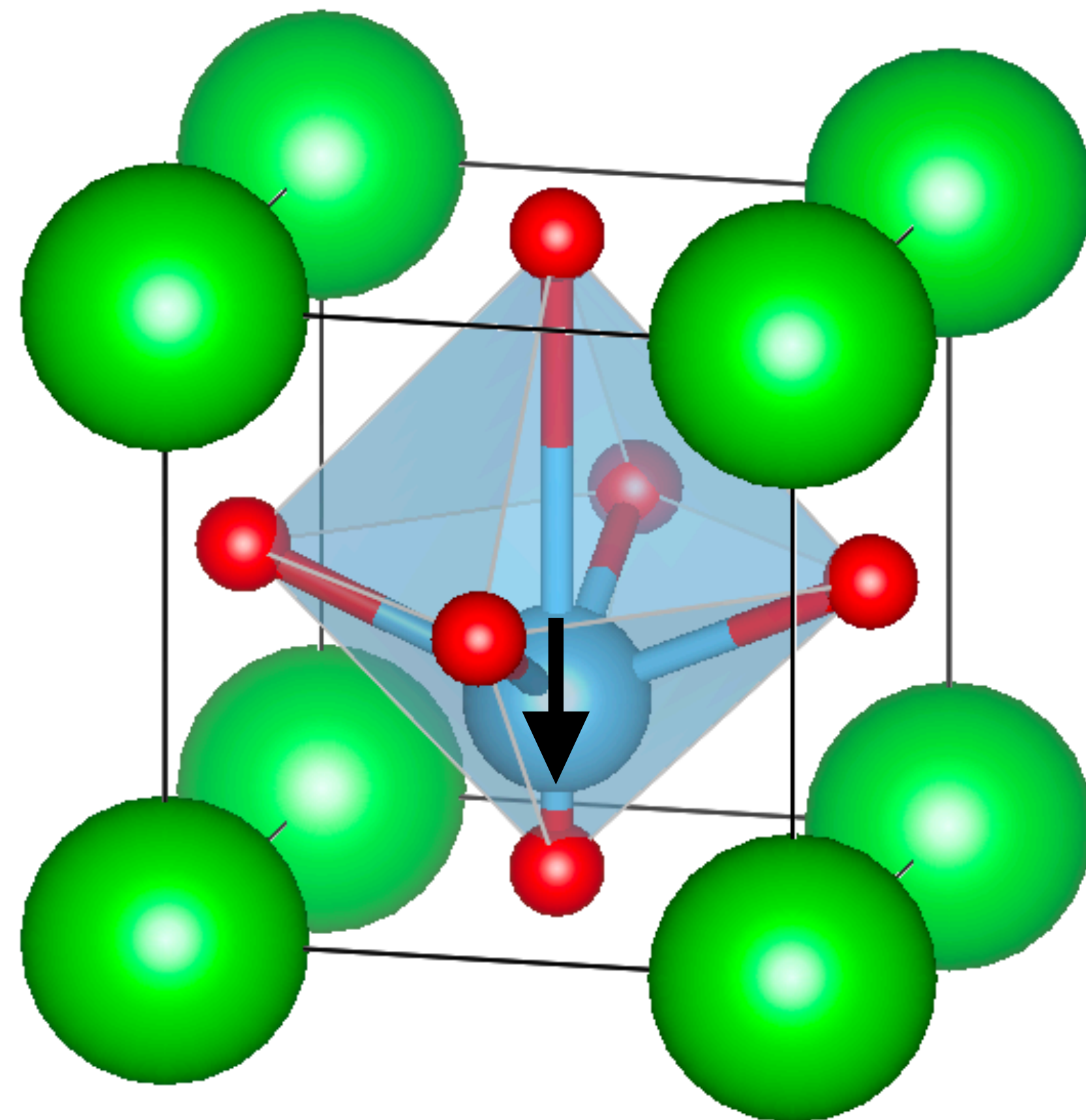
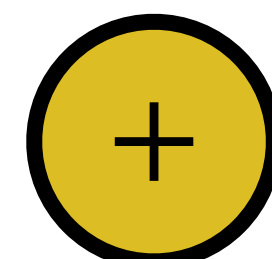
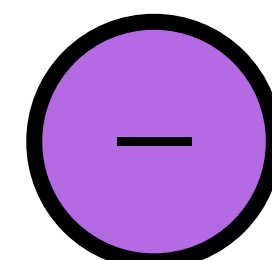
Perovskite structure ABO_3

$$\mu = 0$$



cubic

$$\mu$$

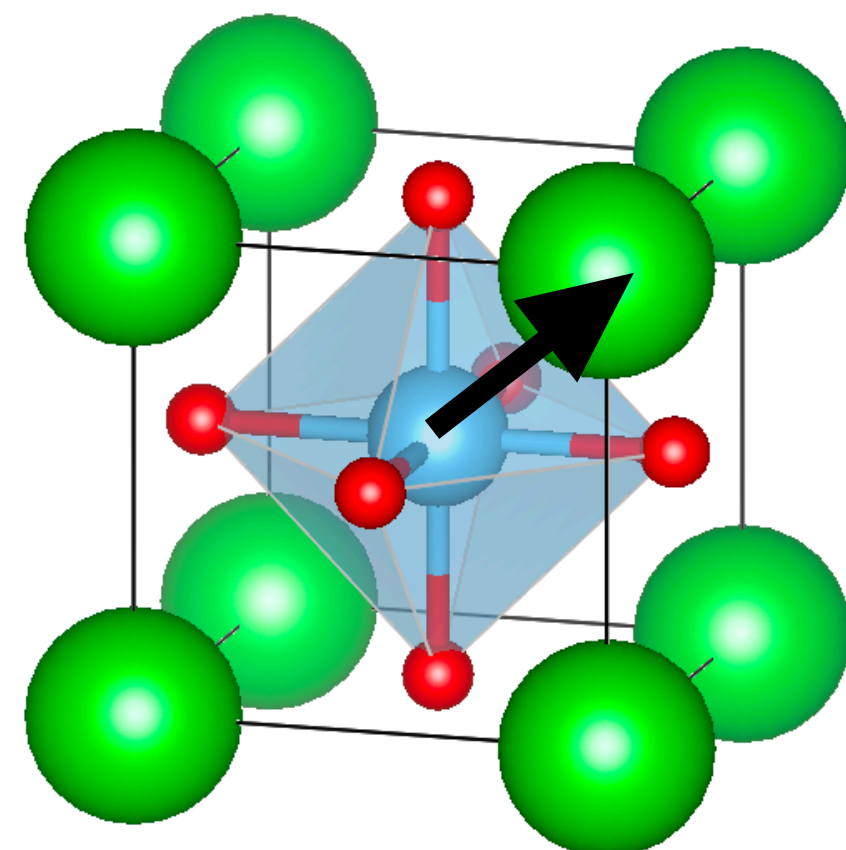


tetragonal

Phase diagram of BaTiO₃

rhombohedral

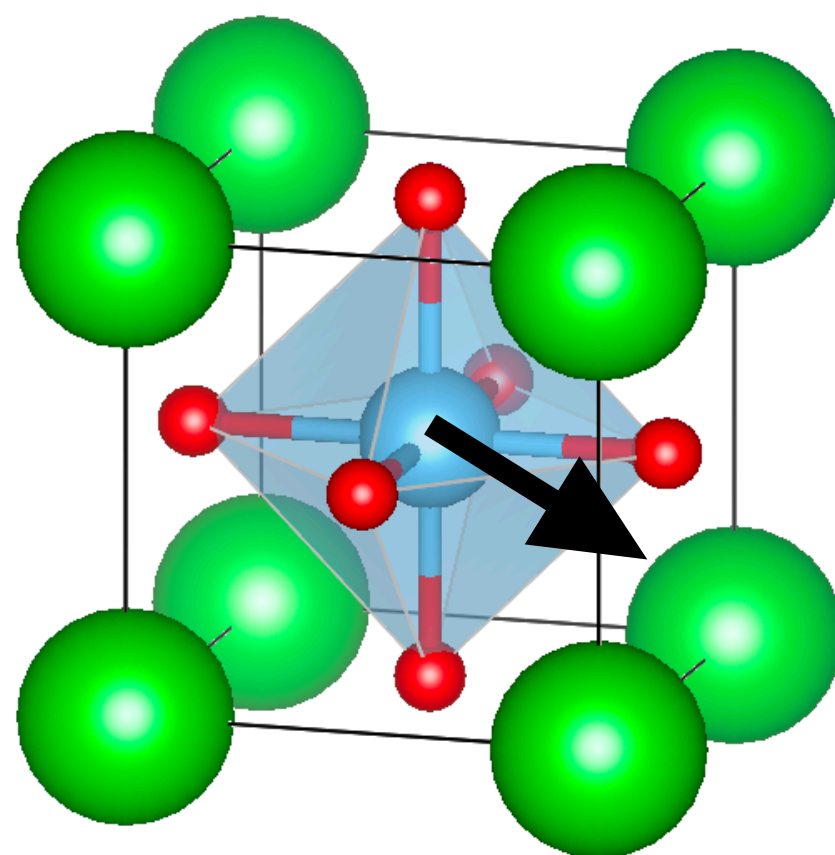
$$a = b = c$$
$$\alpha = \beta = \gamma \neq 90^\circ$$



$\langle 111 \rangle$ distortion

orthorhombic

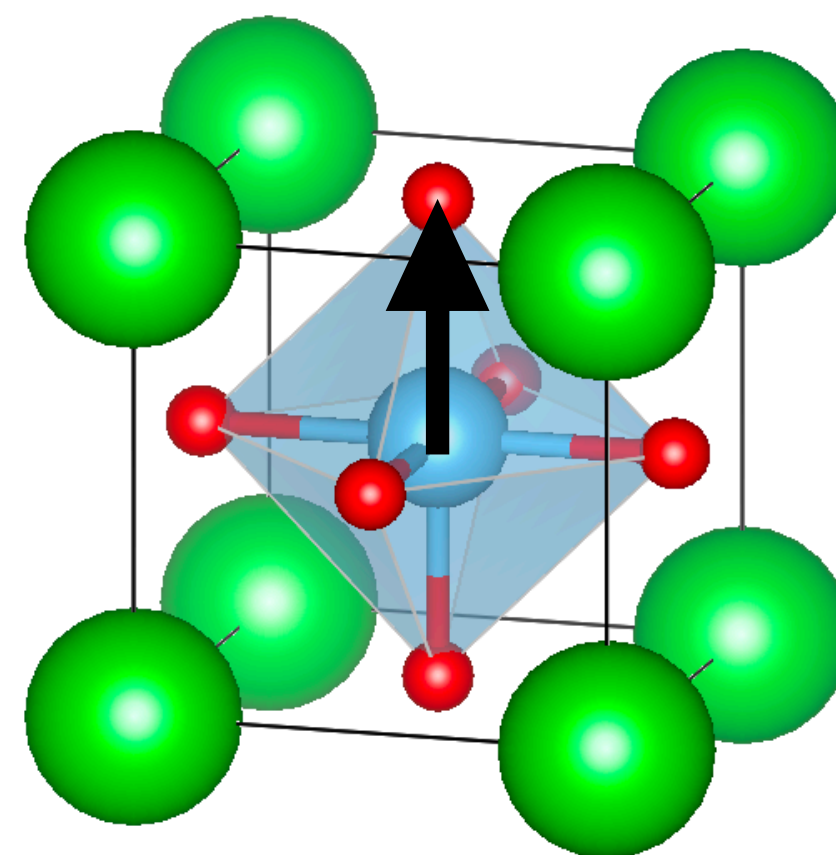
$$a \neq b \neq c$$
$$\alpha = \beta = \gamma = 90^\circ$$



$\langle 110 \rangle$ distortion

tetragonal

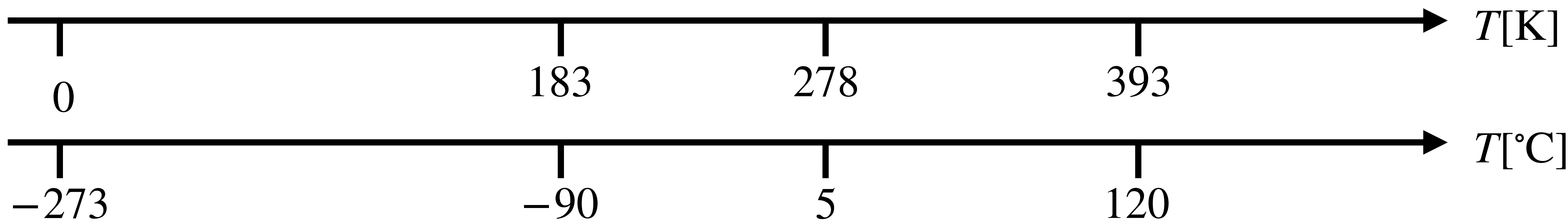
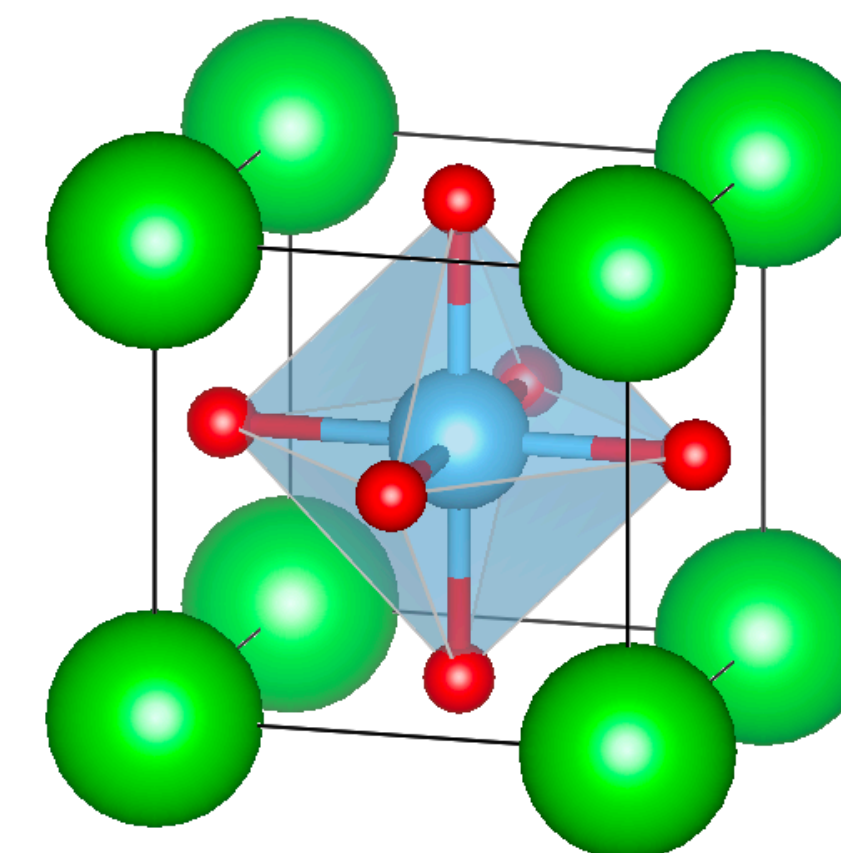
$$a = b \neq c$$
$$\alpha = \beta = \gamma = 90^\circ$$



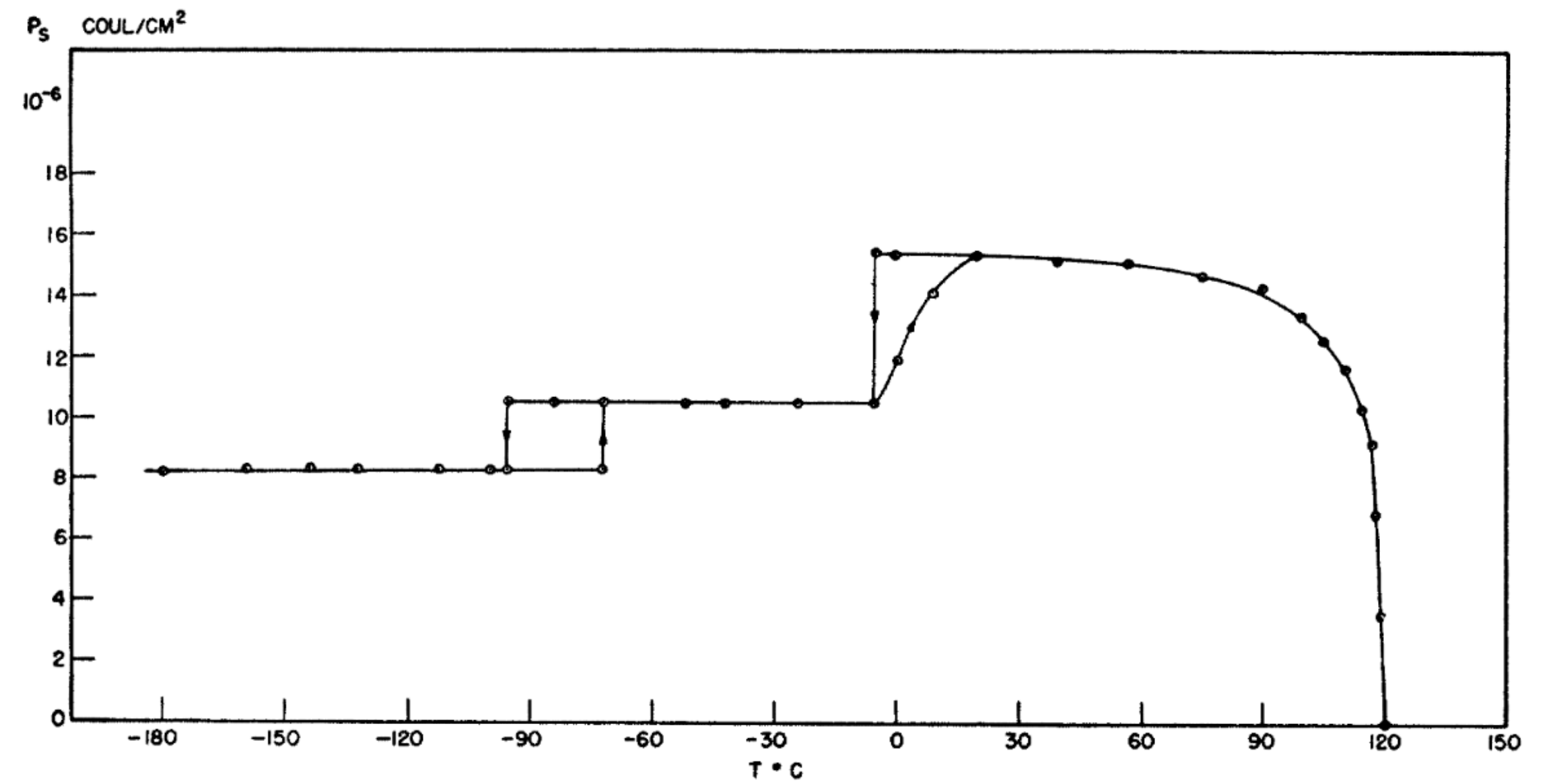
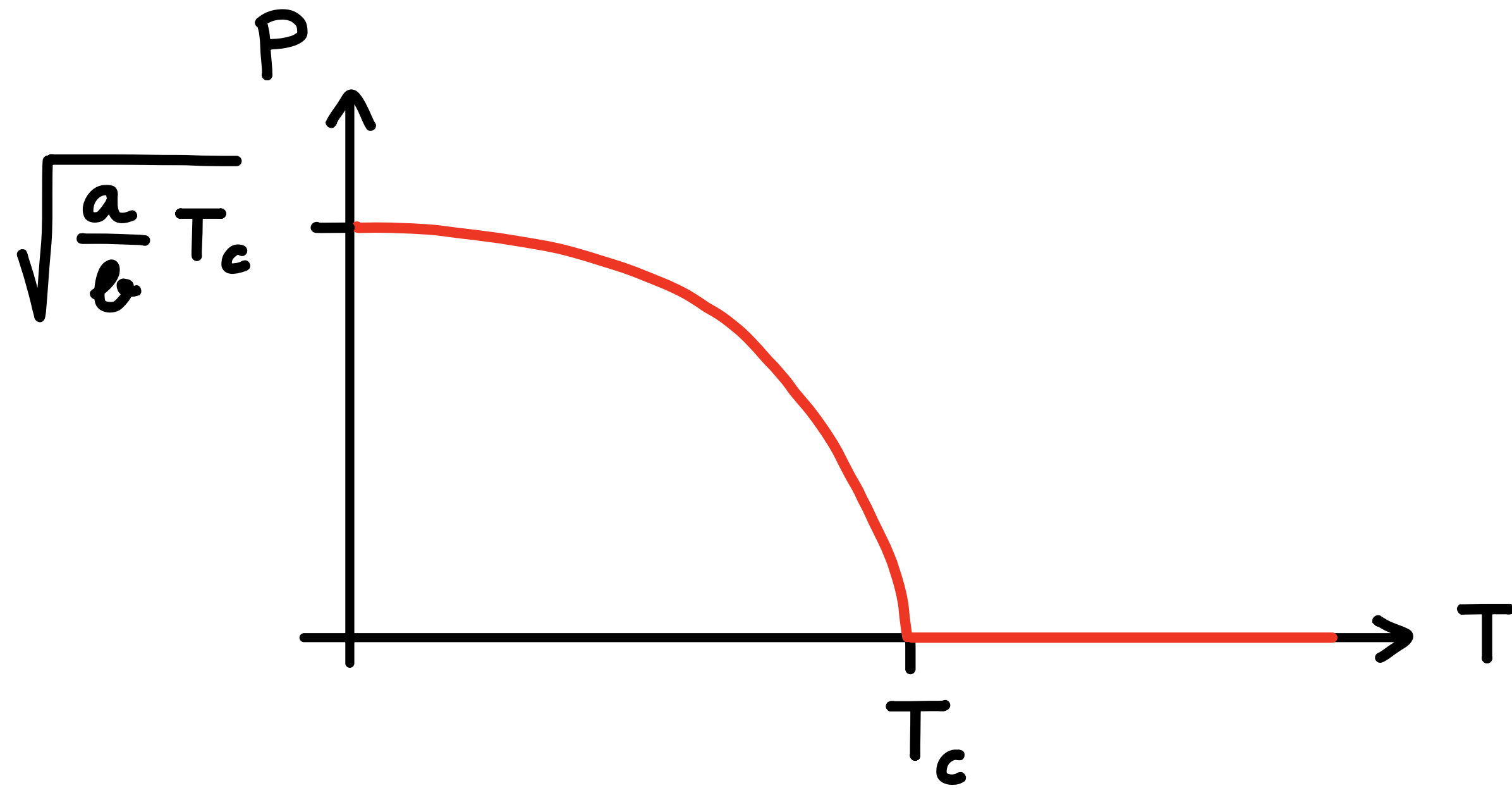
$\langle 100 \rangle$ distortion

cubic

$$a = b = c$$
$$\alpha = \beta = \gamma = 90^\circ$$

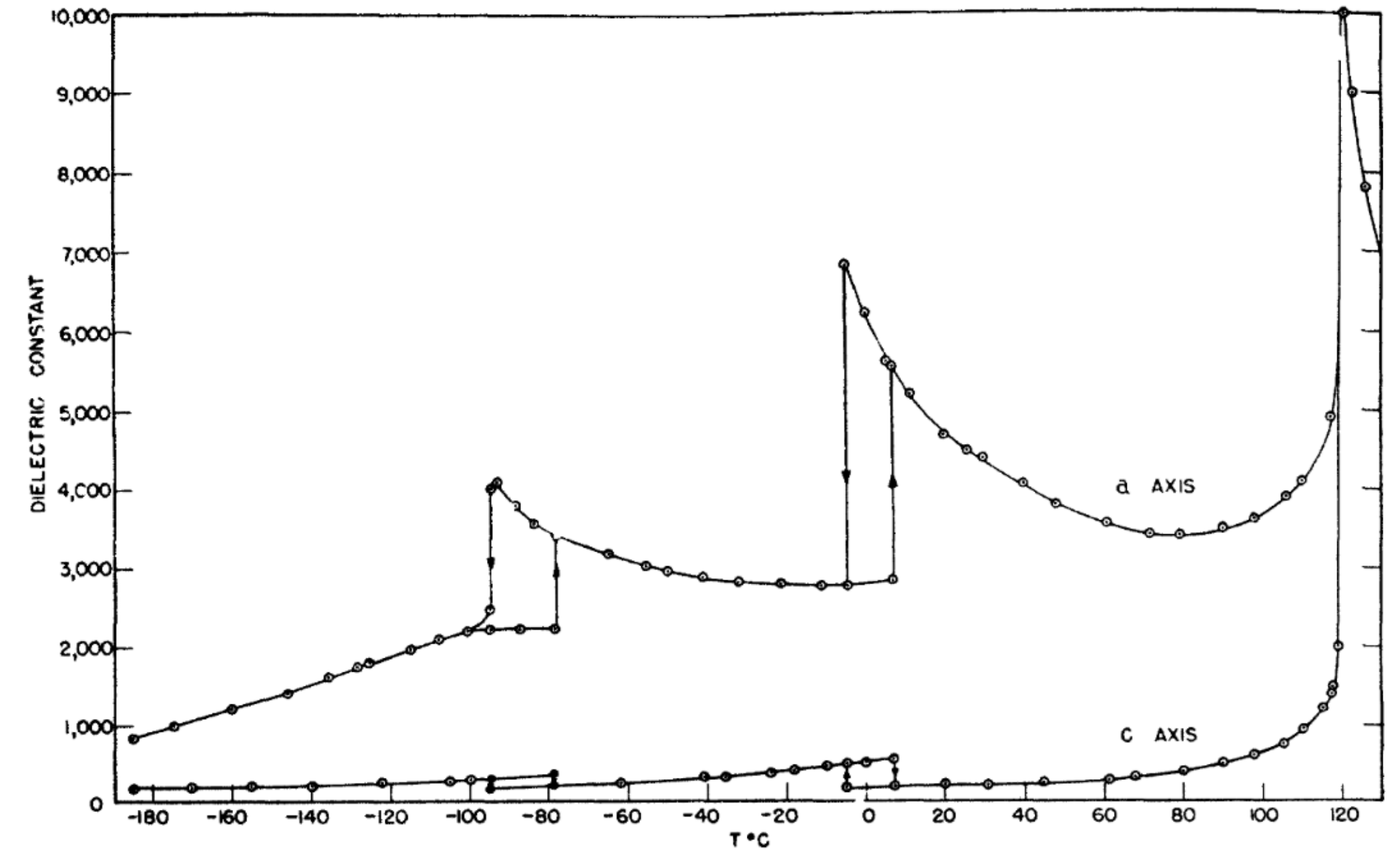
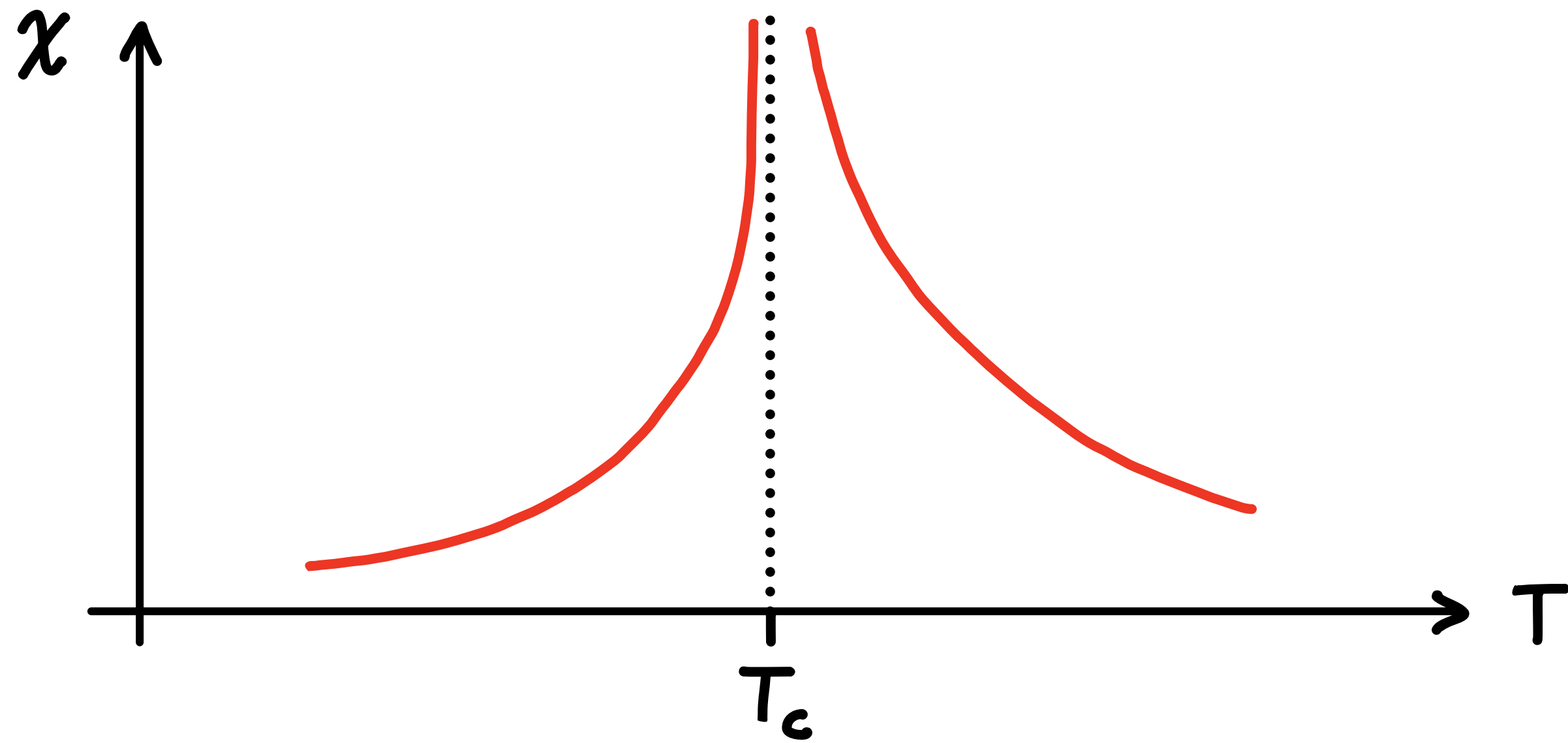


Experimental data for BaTiO₃



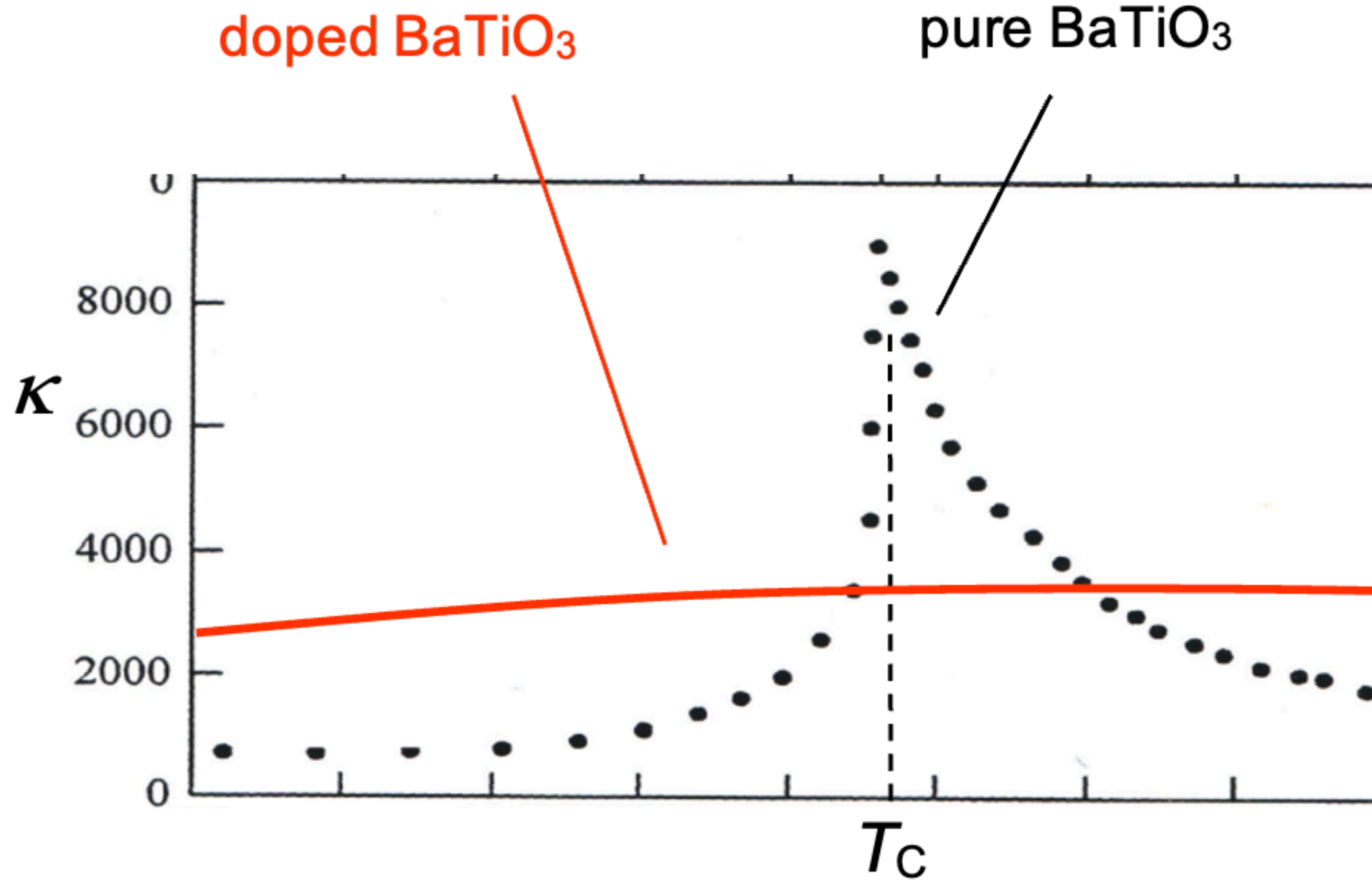
Merz, Physical Review 76, 1221 (1949)

Experimental data for BaTiO₃



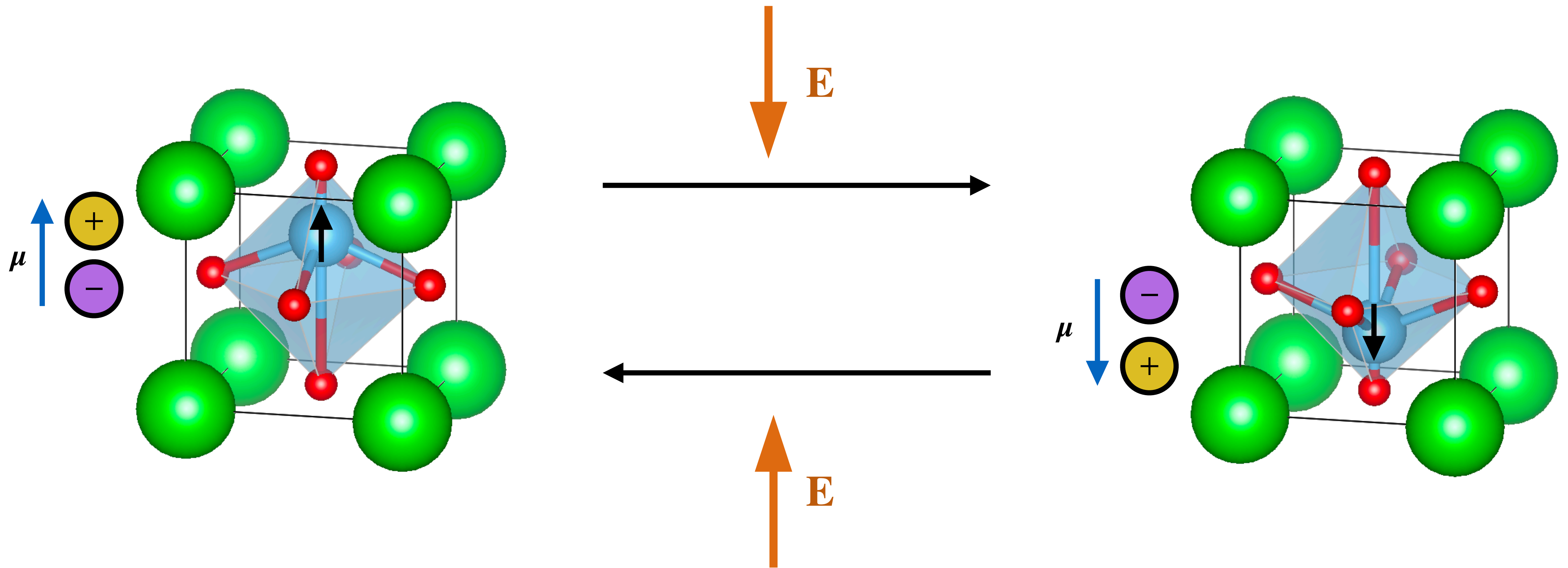
Merz, Physical Review 76, 1221 (1949)

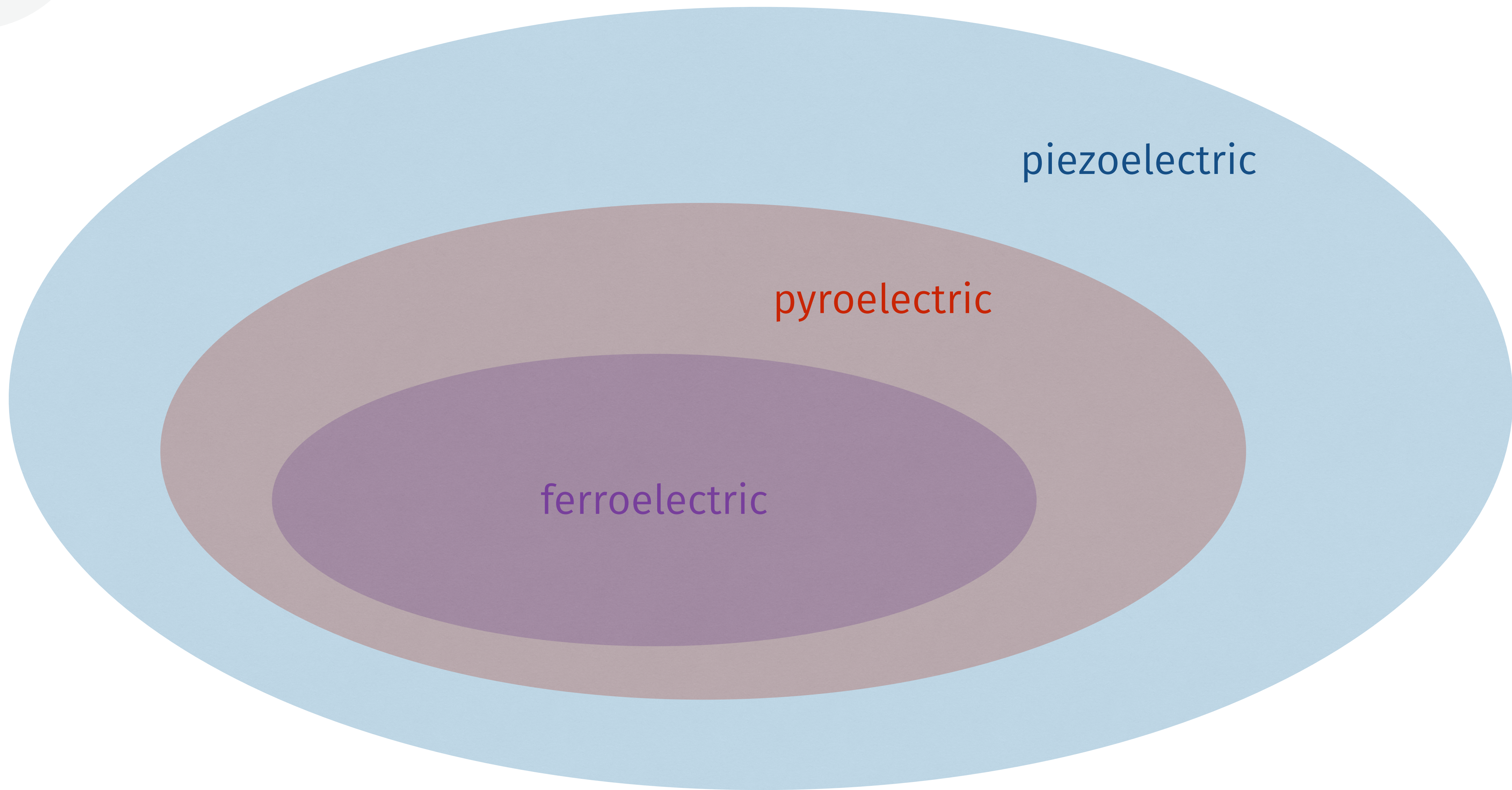
Experimental data for BaTiO₃



Ferroelectricity

- ▶ Ferroelectricity: spontaneous polarisation that can be reversed by electric field





piezoelectric

pyroelectric

ferroelectric